

Solar Corona

Jaroslav Dudík

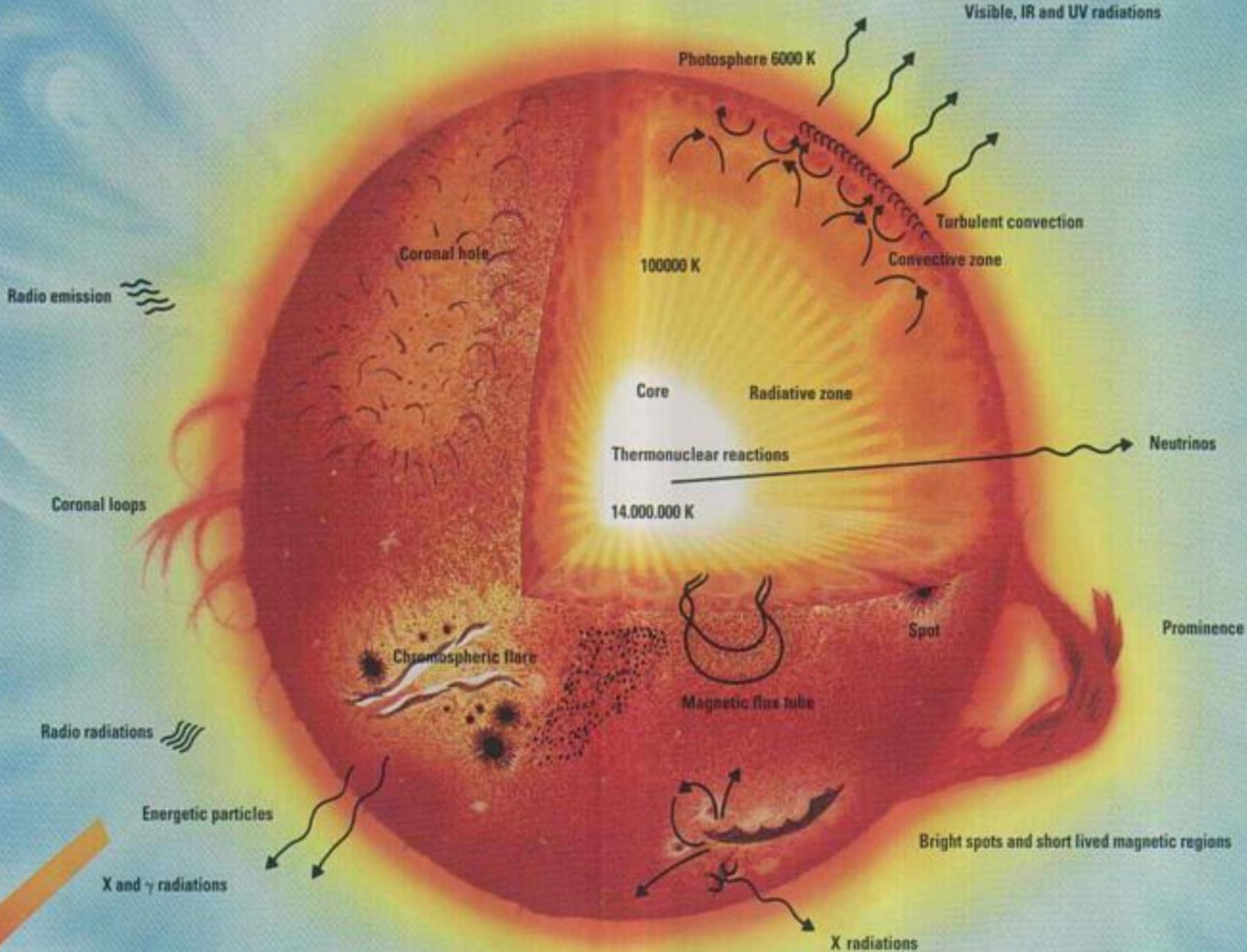


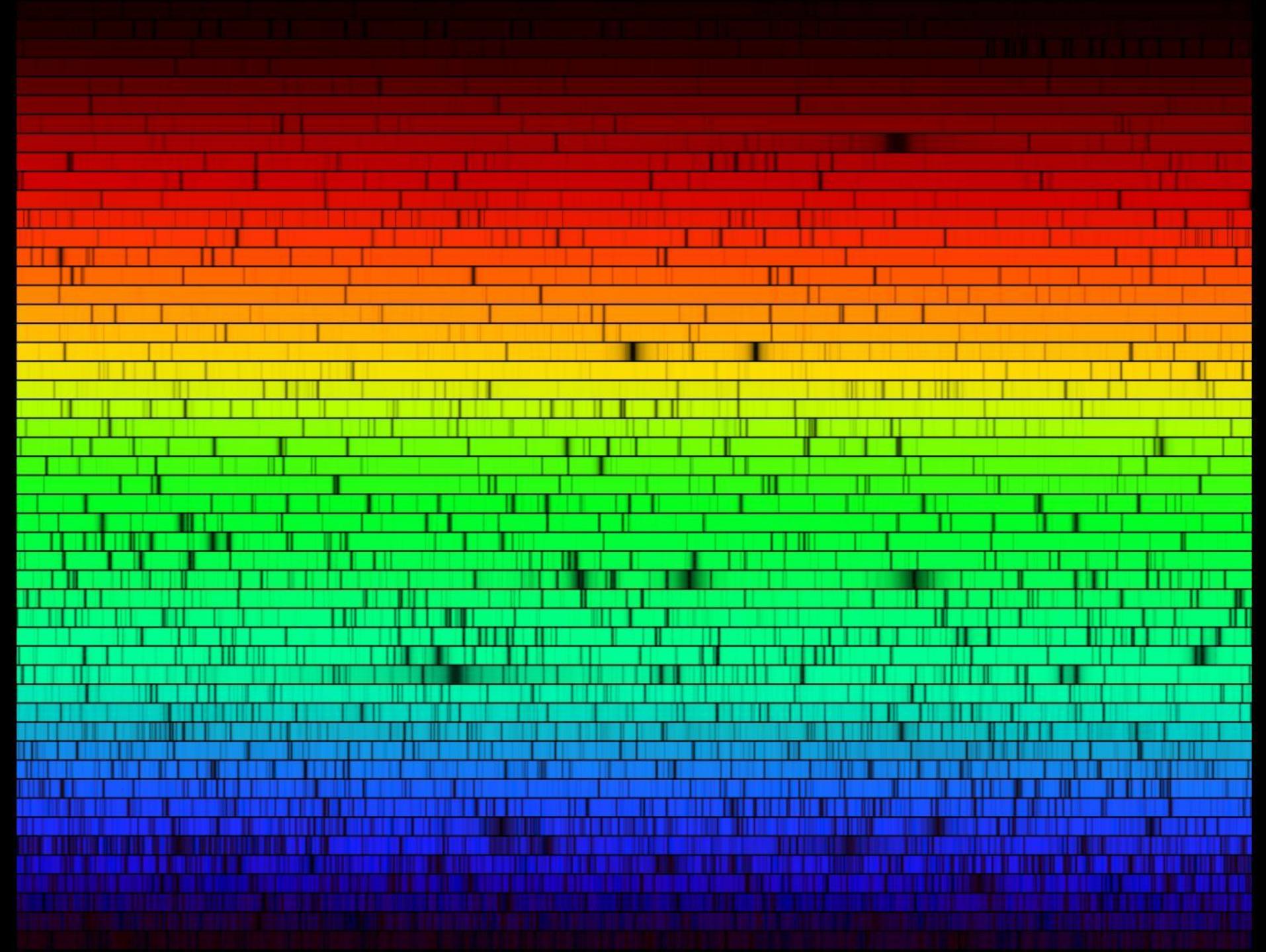
Astronomical
Institute
of the Czech Academy
of Sciences

Lecture 1

Selected Chapters in Astrophysics

Faculty of Mathematics and Physics, Charles University, 2018-10-22



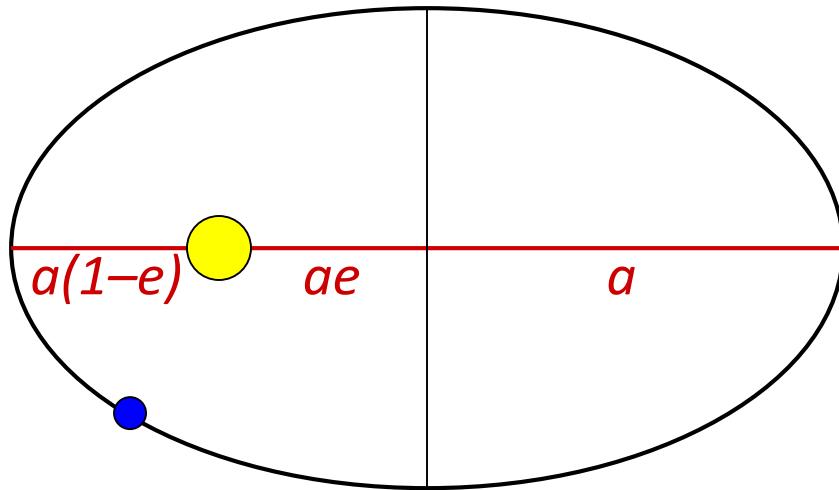


Motivation: Irradiance

The Solar “Constant”

- Energy flux budget at Earth

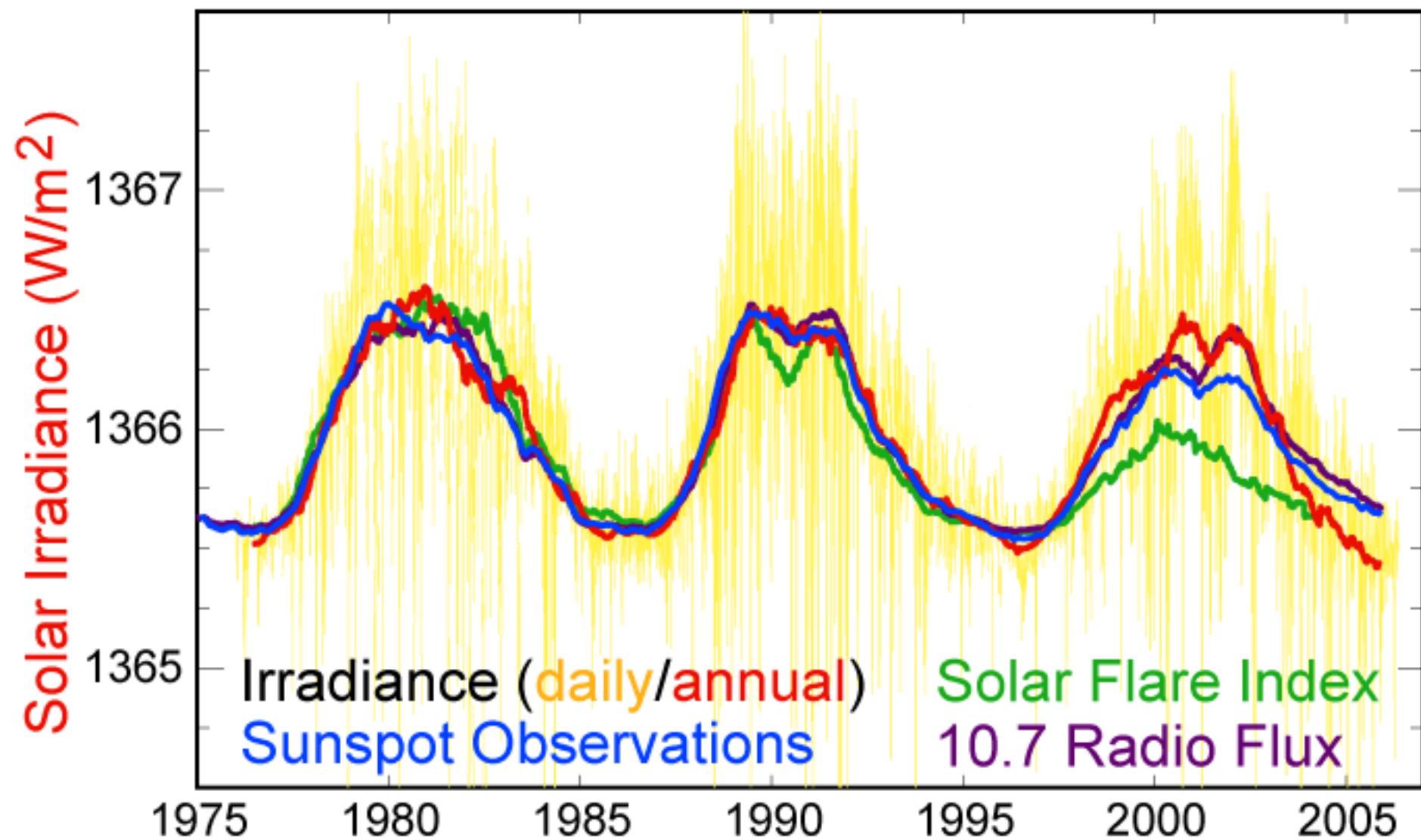
$$F = \frac{L_{\odot}}{4\pi(1 \text{ AU})^2} = \frac{3.846 \times 10^{26} \text{ W}}{4\pi(1.49597 \times 10^{11} \text{ m})^2} = 1367.6 \text{ Wm}^{-2}$$



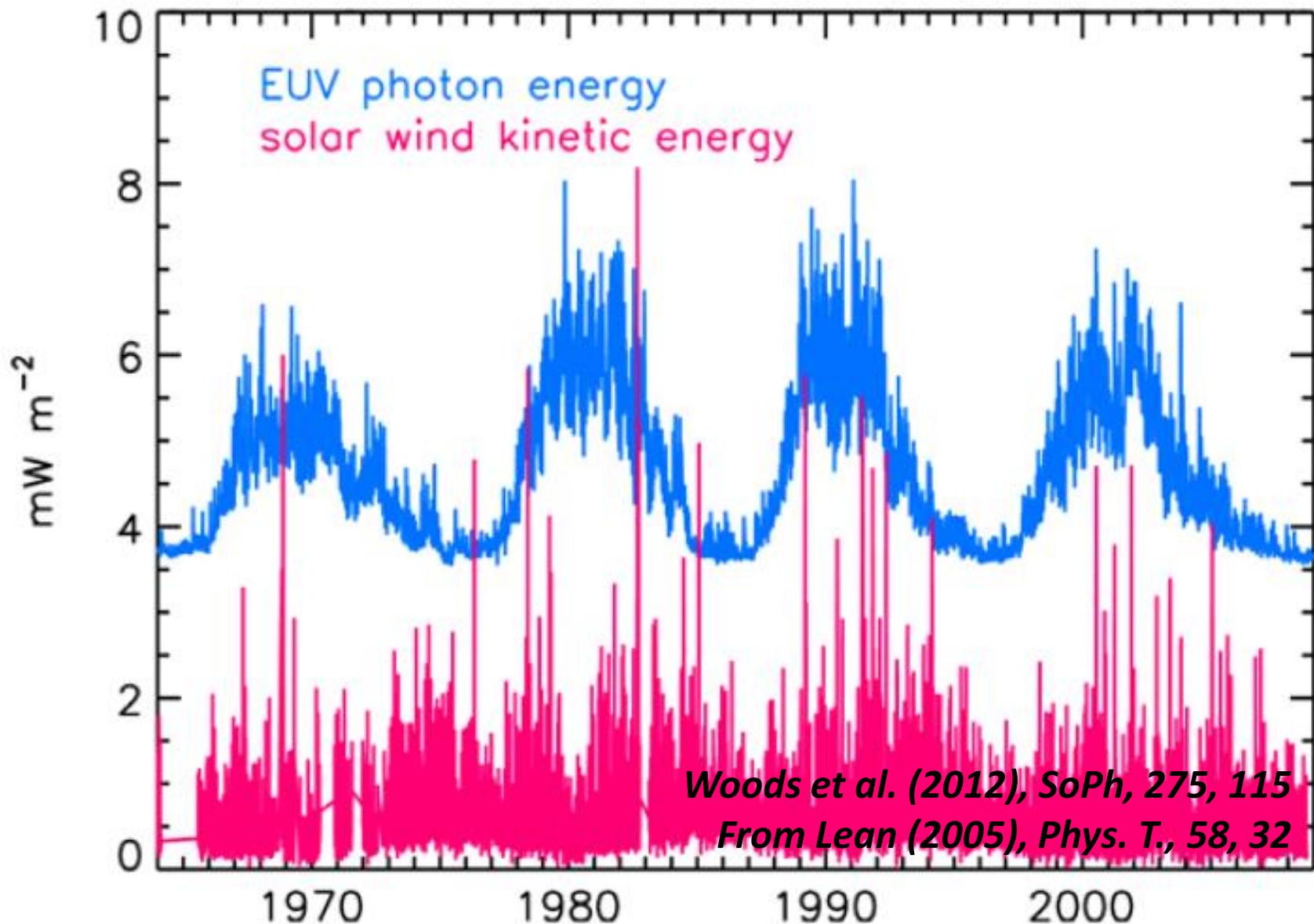
- Variations due to ellipticity of the Earth's orbit ($e = 0,0167$)
 - perihelion: $\sim 1414,4 \text{ Wm}^{-2}$ (+3,3%)
 - aphelion: $\sim 1323,0 \text{ Wm}^{-2}$ (-3,3%)
- Earth's albedo $A = 0,367$ (but clouds etc.)
⇒ mean temperature at Earth

$$\pi R_{\odot}^2 (1 - A) F = 4\pi R_{\odot}^2 \sigma T_{\odot}^4 \left(\frac{100}{119}\right)^4$$

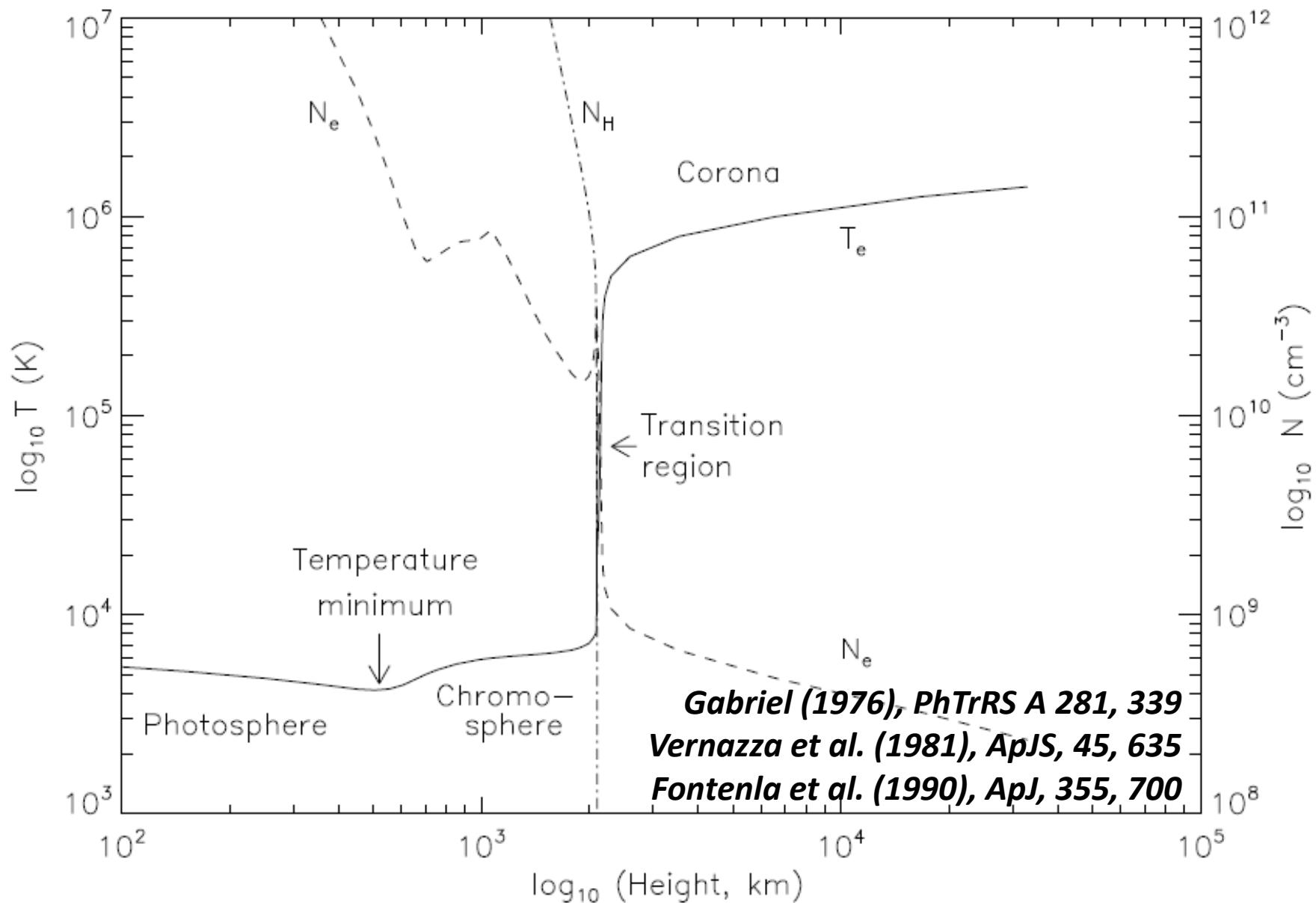
Solar Cycle Variations



Irradiance at EUV wavelengths



Chromosphere and Corona: $T(z)$



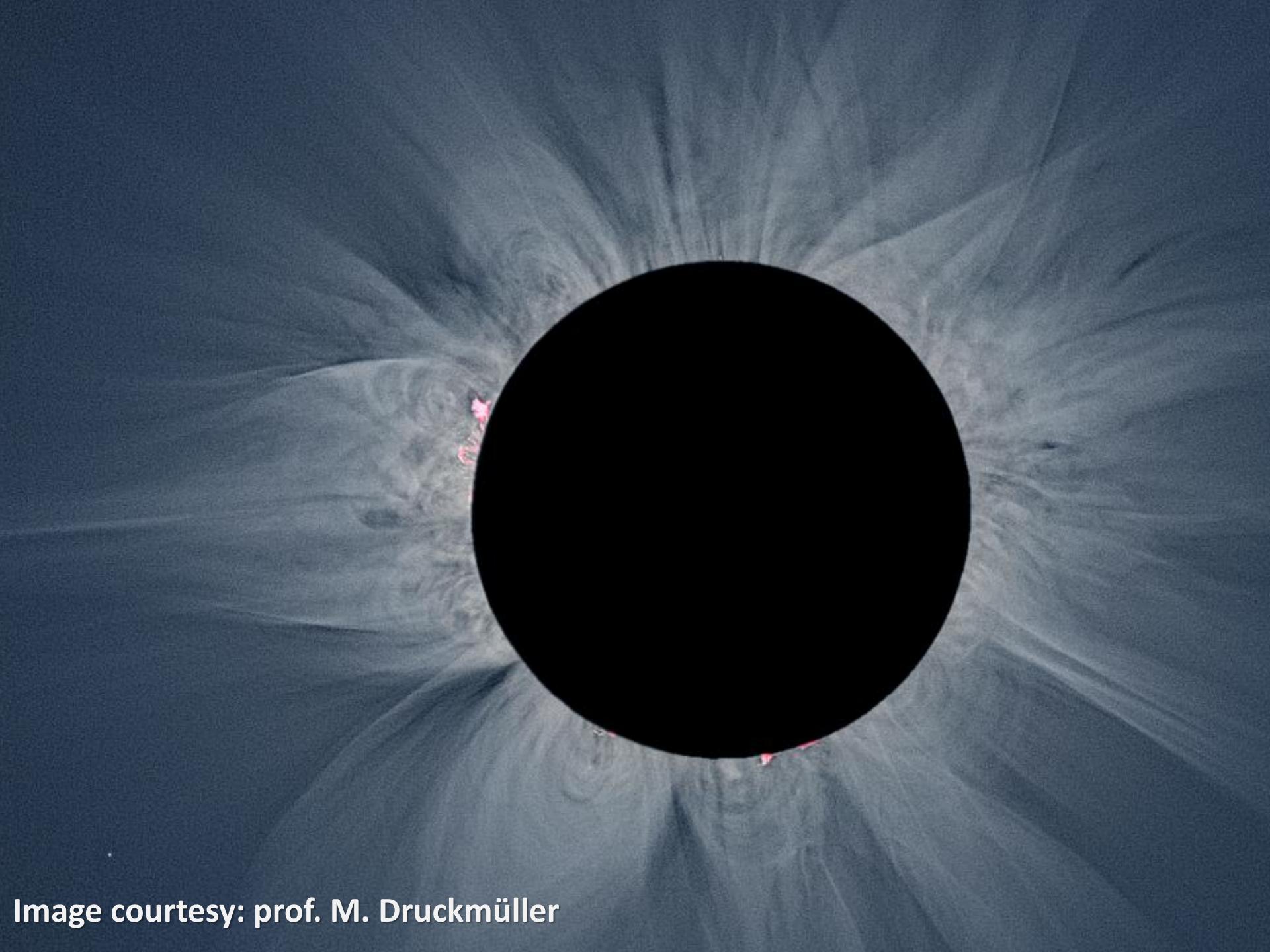


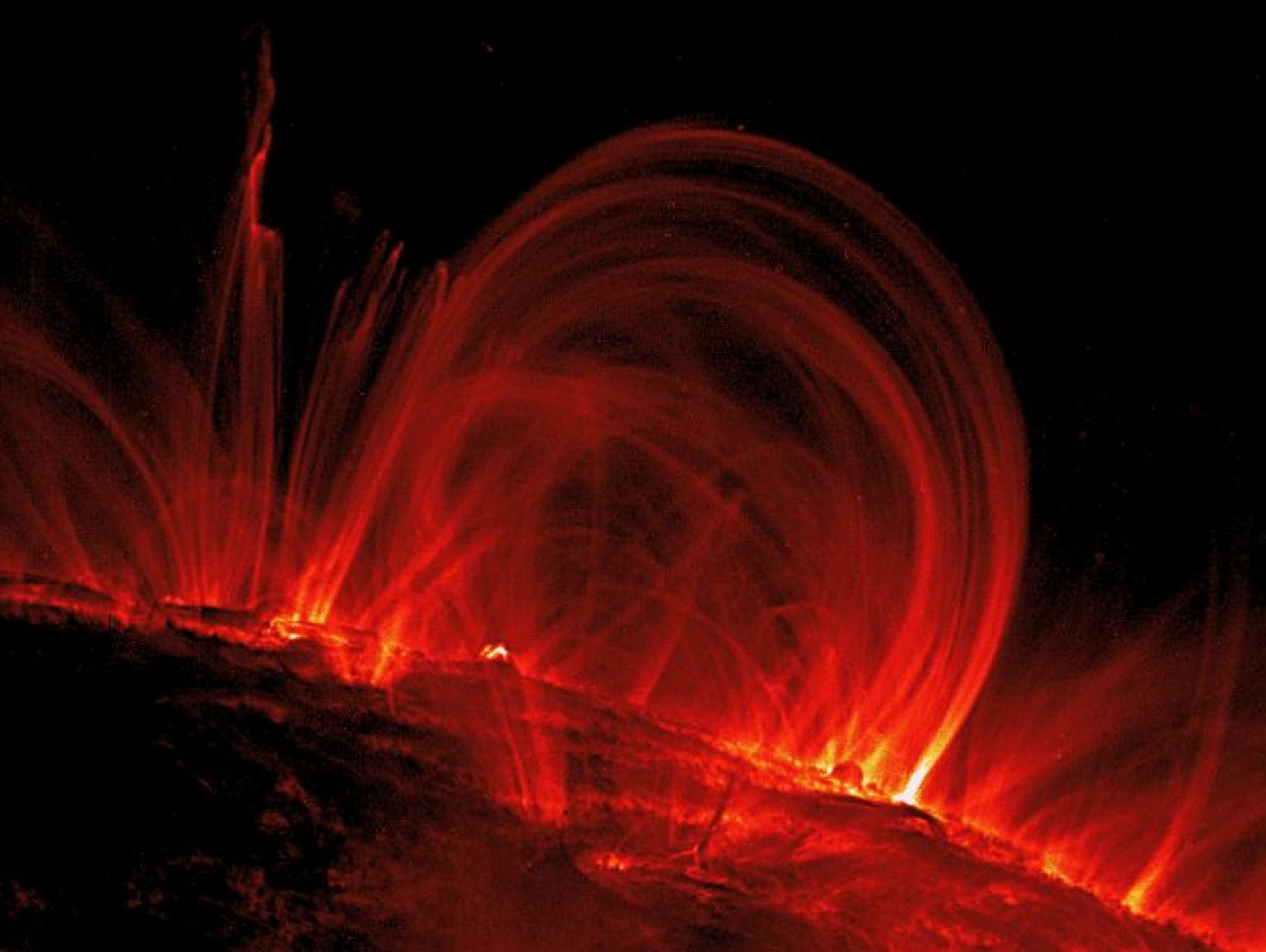
Image courtesy: prof. M. Druckmüller



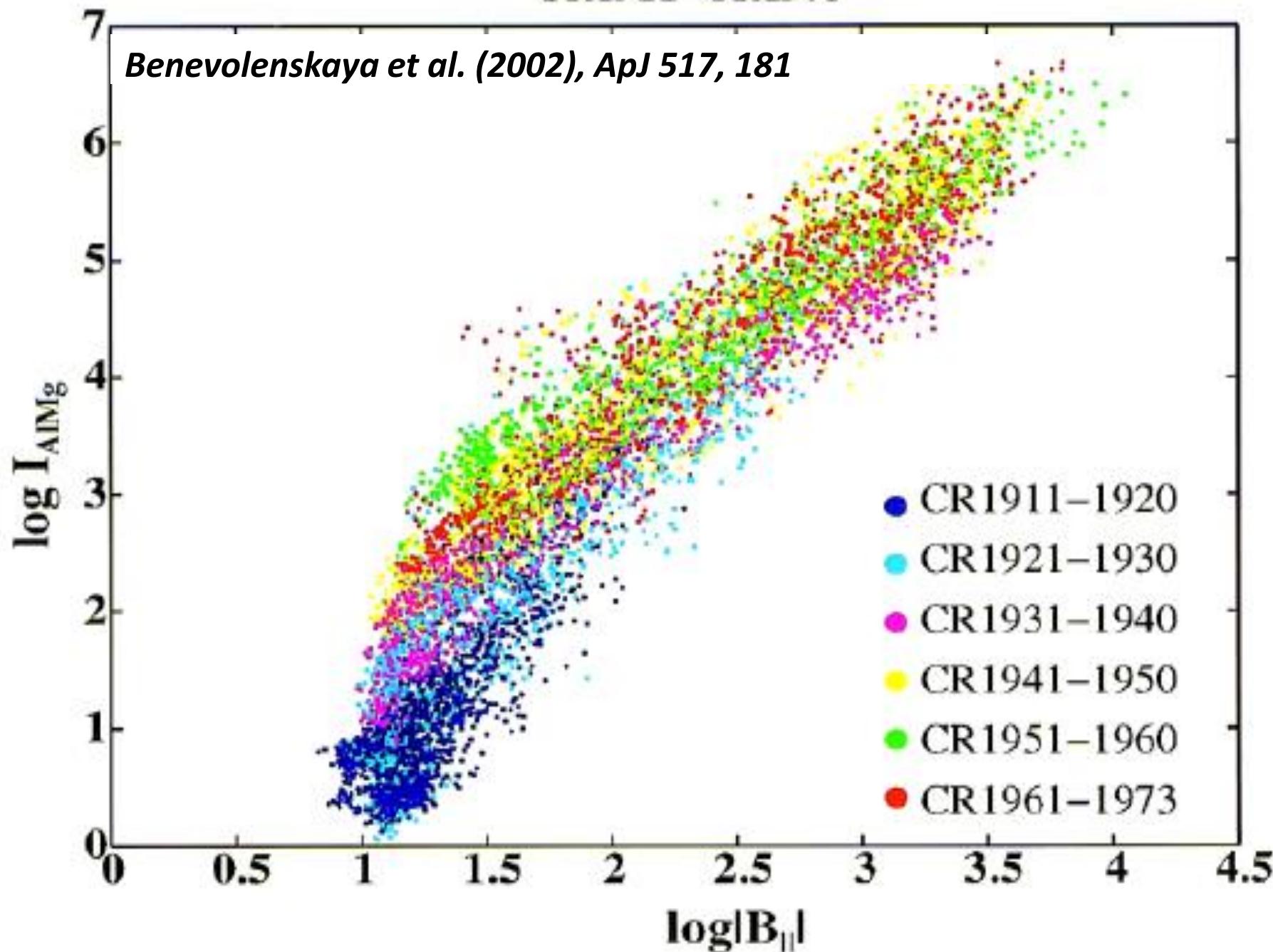
Image courtesy: prof. M. Druckmüller



Image courtesy: prof. M. Druckmüller



CR1911–CR1973



Optically Thin Spectroscopy

- Optically thin = negligible absorption (no radiative transfer)
– everything emitted along the LOS will reach the observer
- The emissivity ε_{ij} of a spectral line λ_{ij} produced by transitions from level i to level j in a k -times ionized atom of element X is given by

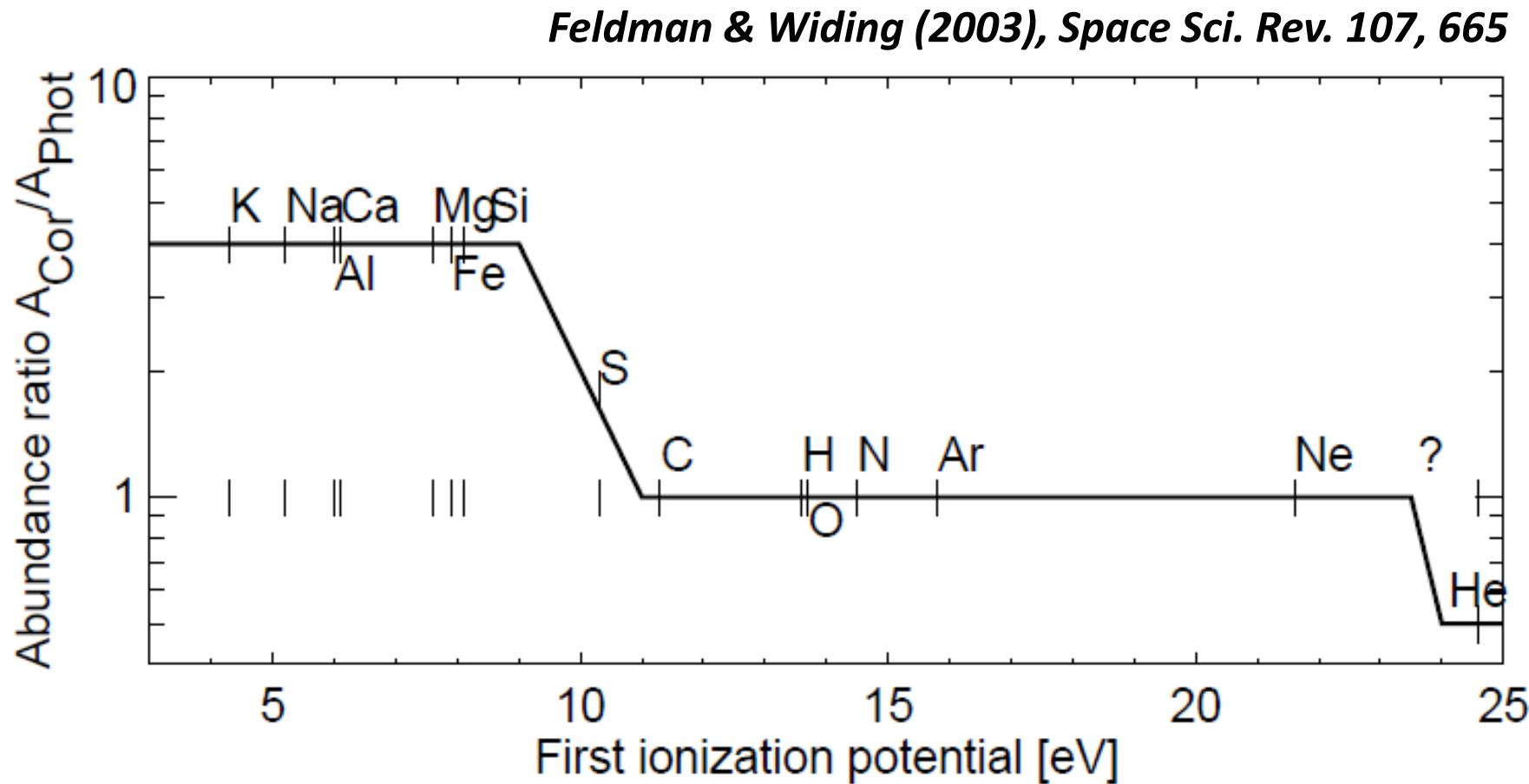
$$\begin{aligned}\varepsilon_{ij} &= \frac{hc}{\lambda_{ij}} A_{ij} n(X_i^{+k}) = \frac{hc}{\lambda_{ij}} \frac{A_{ij}}{n_e} \frac{n(X_i^{+k})}{n(X^{+k})} \frac{n(X^{+k})}{n(X)} \frac{n(X)}{n(H)} n(H) n_e \\ &= \frac{hc}{\lambda_{ij}} C_{ji} \frac{n(X_i^{+k})}{n(X^{+k})} \frac{n(X^{+k})}{n(X)} \frac{n(X)}{n(H)} n(H) n_e \\ &= G(T, n_e) n(H) n_e\end{aligned}$$

- Assume ionization equilibrium and excitation equilibrium can be treated separately (“coronal approximation”)
- Intensity I_{ij} of this emission line from optically thin plasma of volume V along the line of sight:

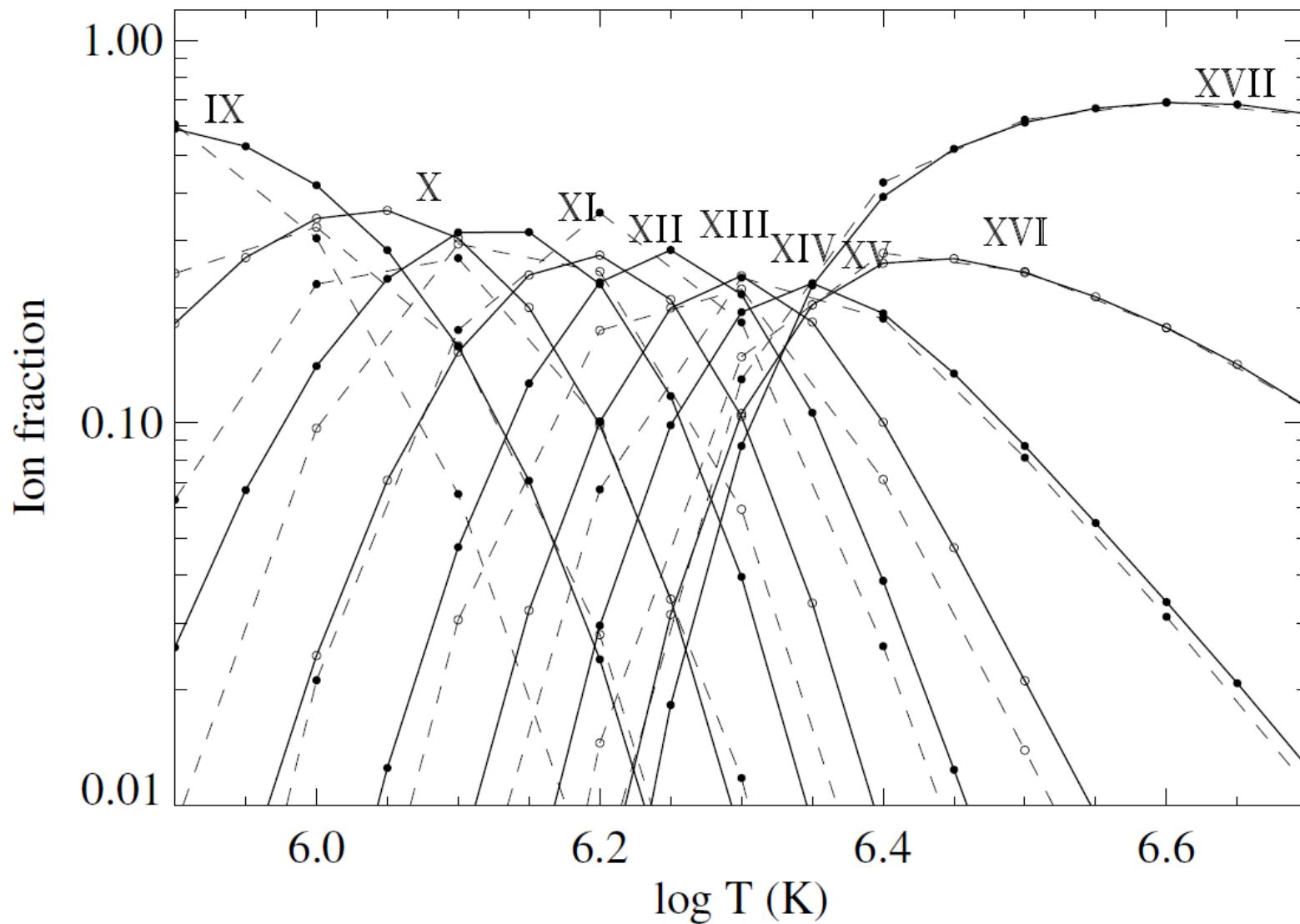
$$I_{ij} = \int G(T, n_e) n(H) n_e dV$$

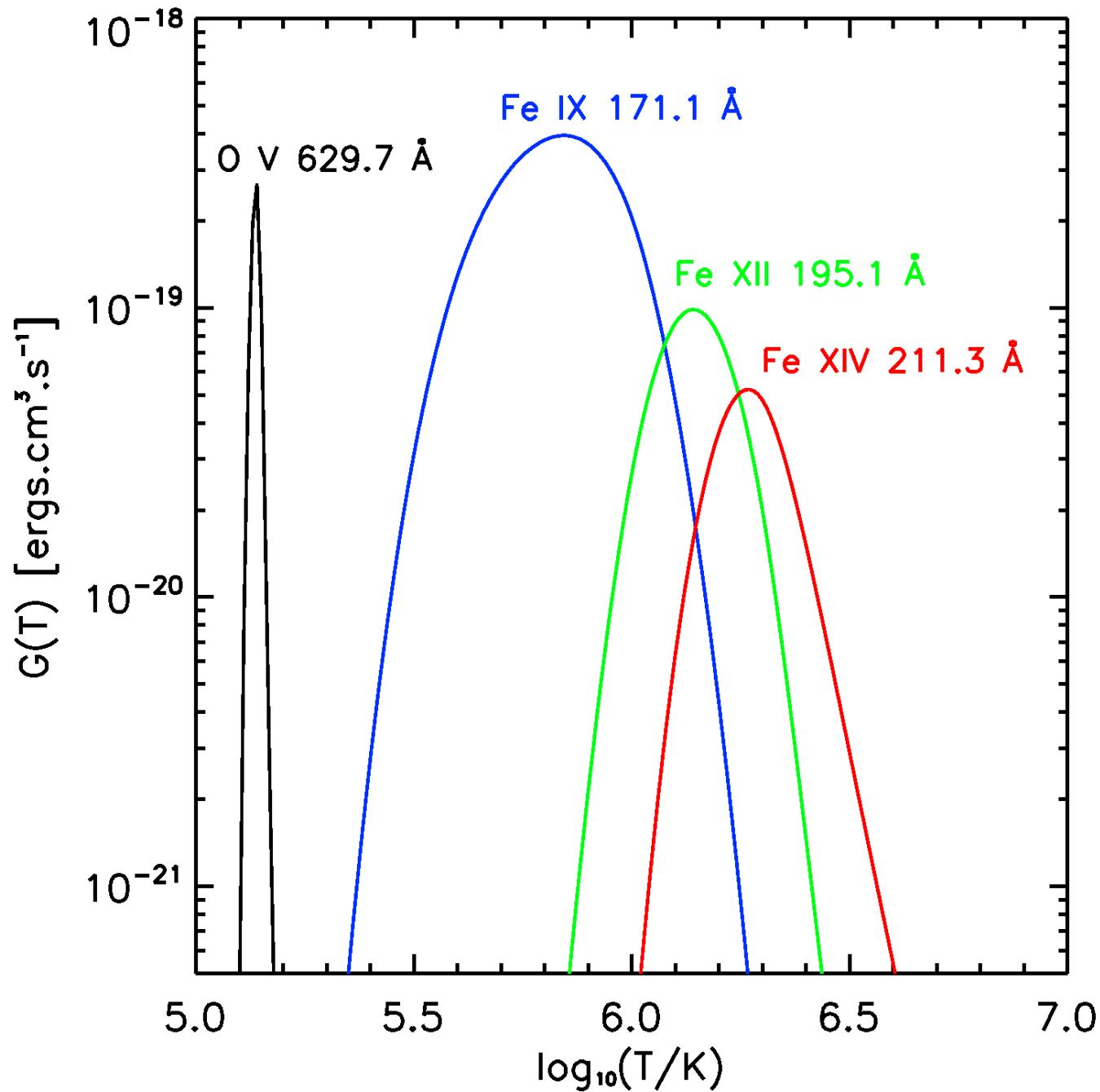
FIP Effect – Coronal Abundances

- Elements with first ionization potential smaller than 10 keV have greatly enhanced abundances in the corona: FIP effect

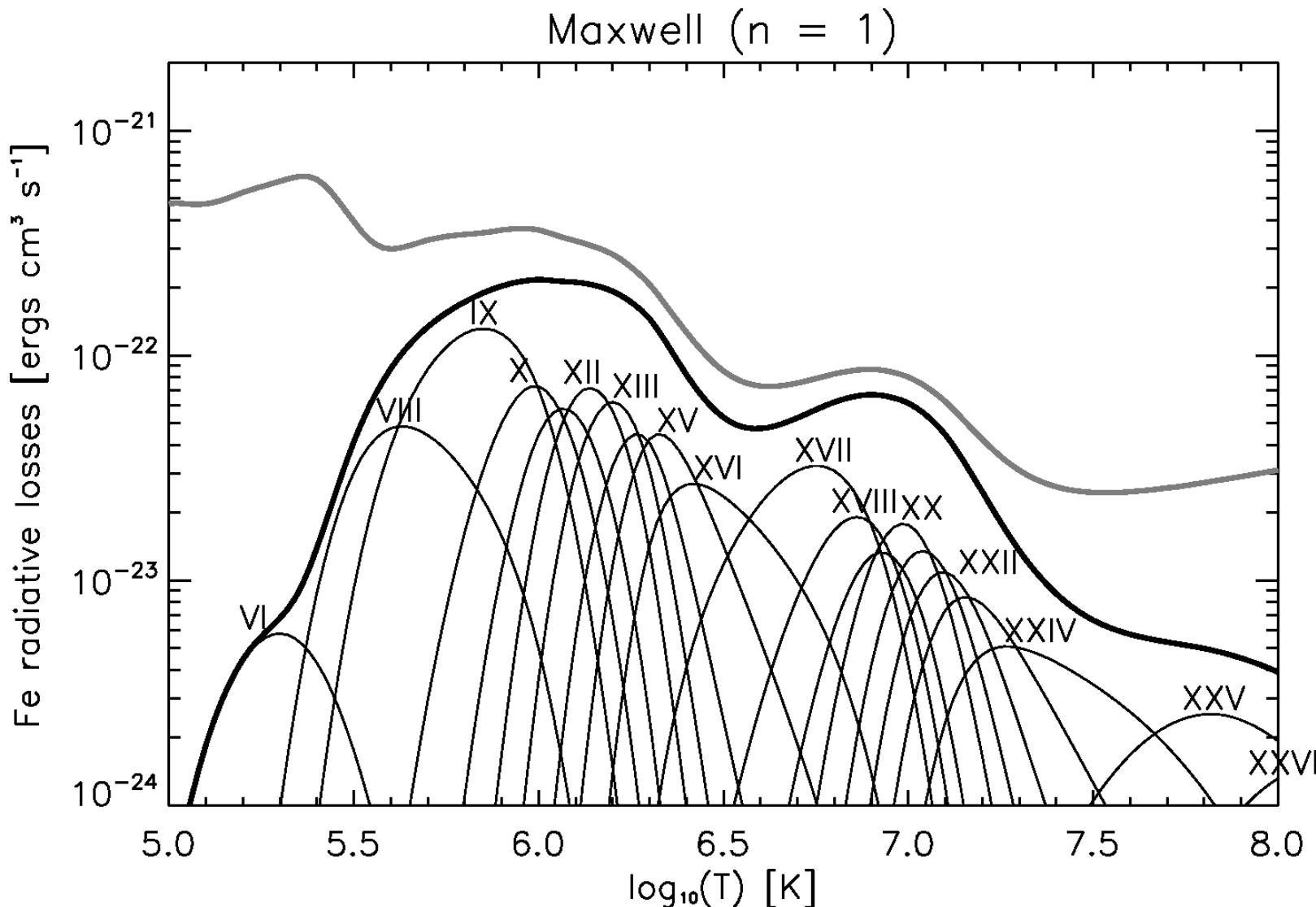


Collisional ionization equilibrium





Coronal Radiative Losses



Emission Measure and DEM(T)

- If the plasma is **isothermal** along the LOS, the intensity is simply

$$I_{ij} = \int G(T, n_e) n_H n_e dV = G(T, n_e) \int n_H n_e dV = G(T, n_e) EM(T)$$

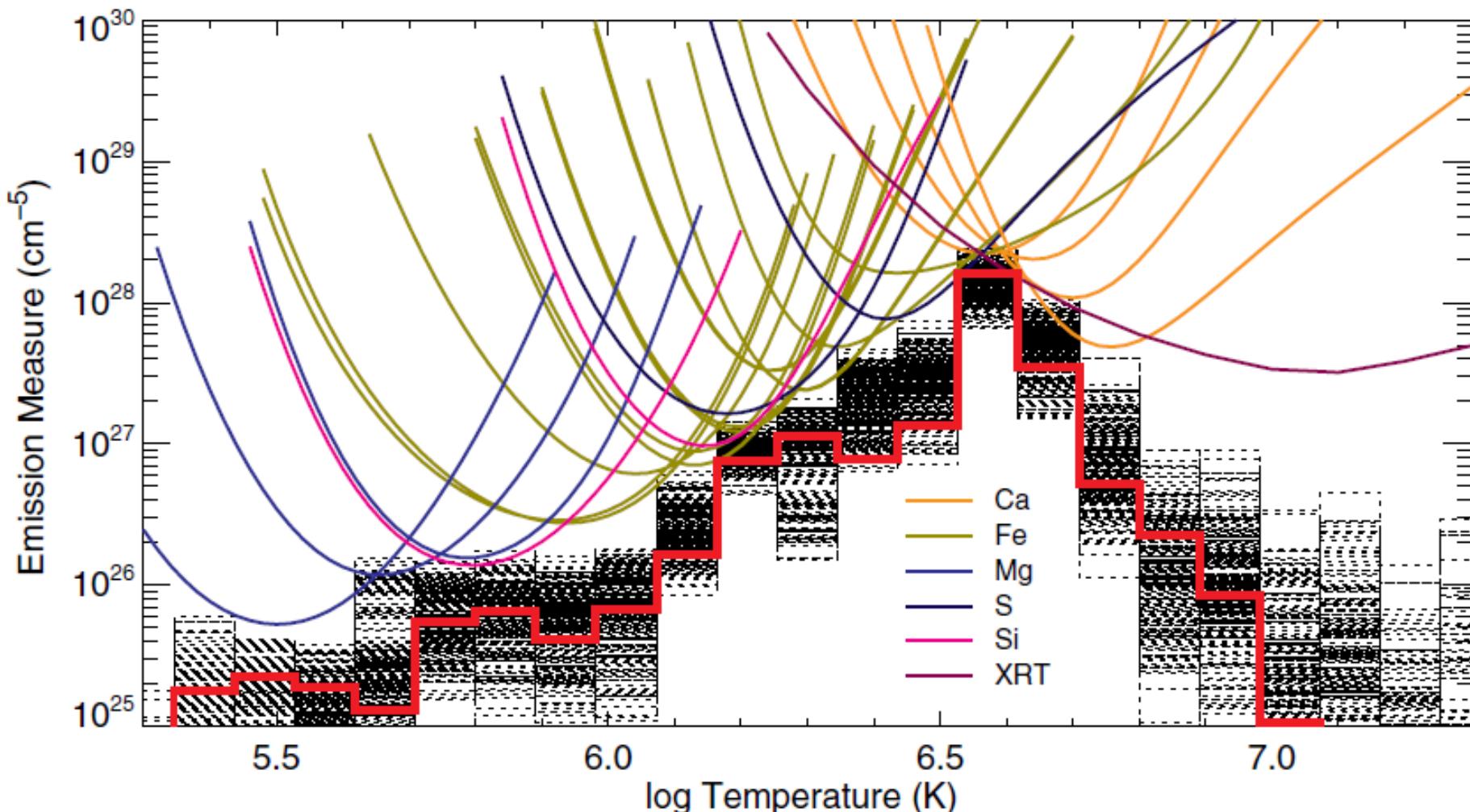
- However, if the plasma is **multithermal**, i.e., many different structures along the LOS, the intensity is given by

$$I_{ij} = \int G(T, n_e) n_H n_e \frac{dV}{dT} dT = \int G(T, n_e) DEM(T) dT$$

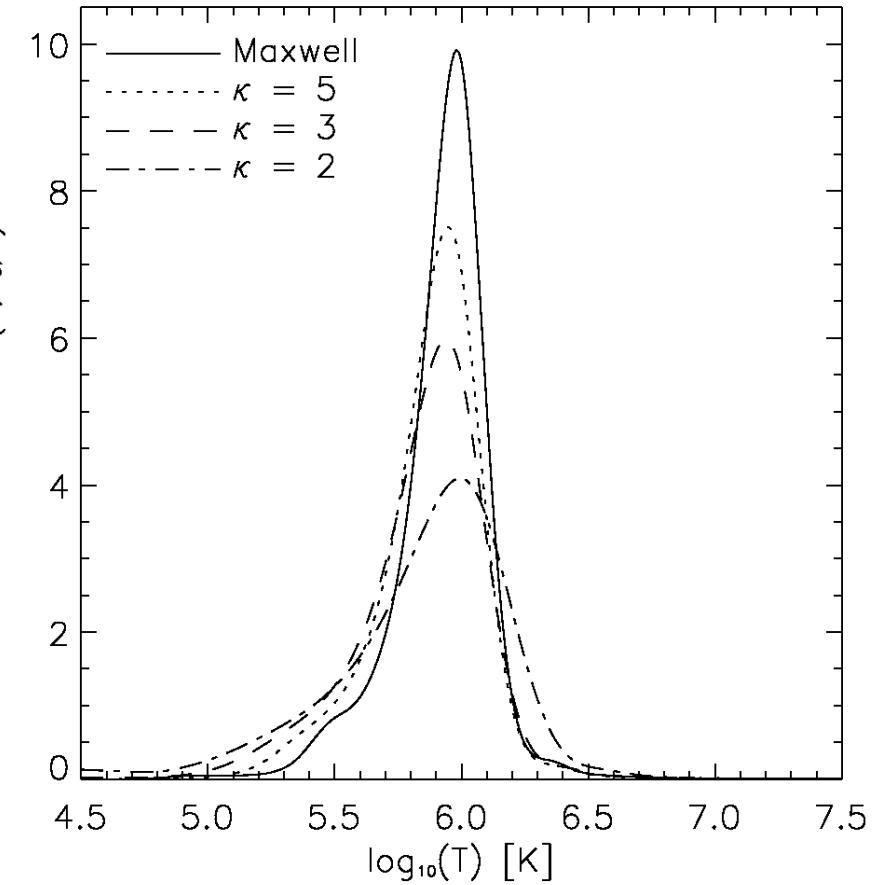
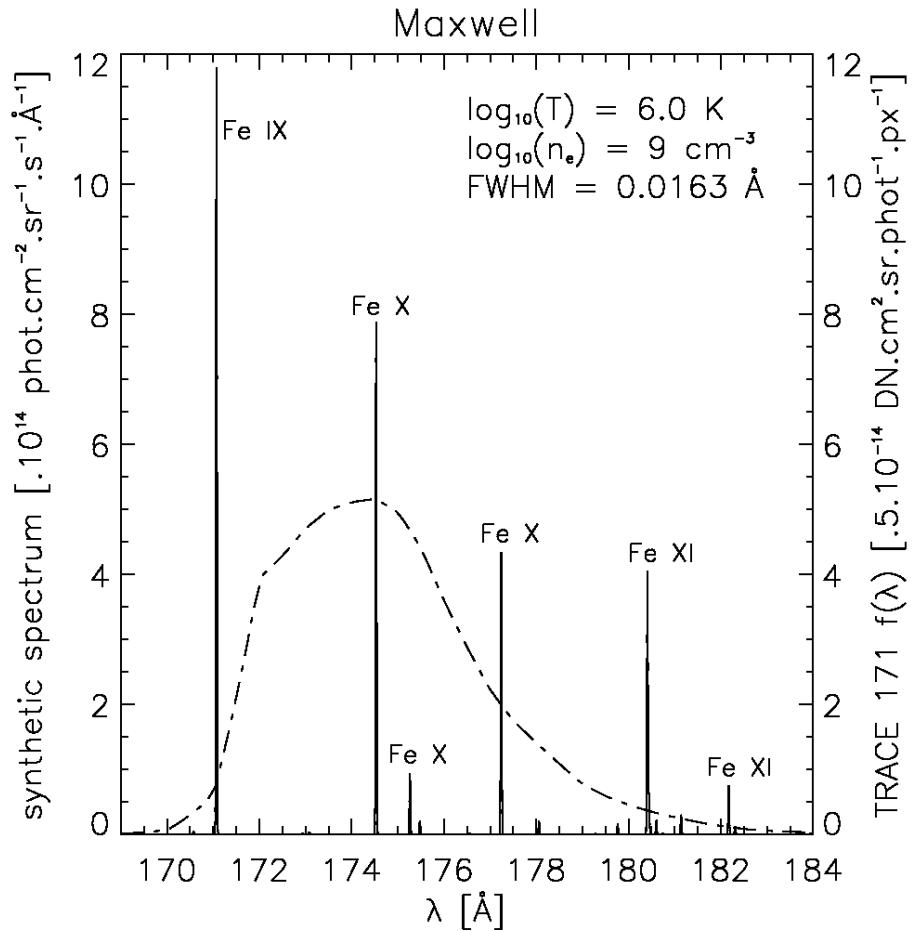
- where **DEM(T)** is the **differential emission measure**
- **DEM(T)** has to be determined from observations.
- Inverse, ill-posed problem, but corona sometimes *is* multithermal!

EM-loci Method: Multithermality

$$EM_{\text{loci}} = \frac{I_{ij}}{G_{ij}(T, n_e)} \Rightarrow DEM(T) \leq \left\{ \frac{I_{ij}}{G_{ij}(T, n_e)} \right\} \quad \forall i, j$$

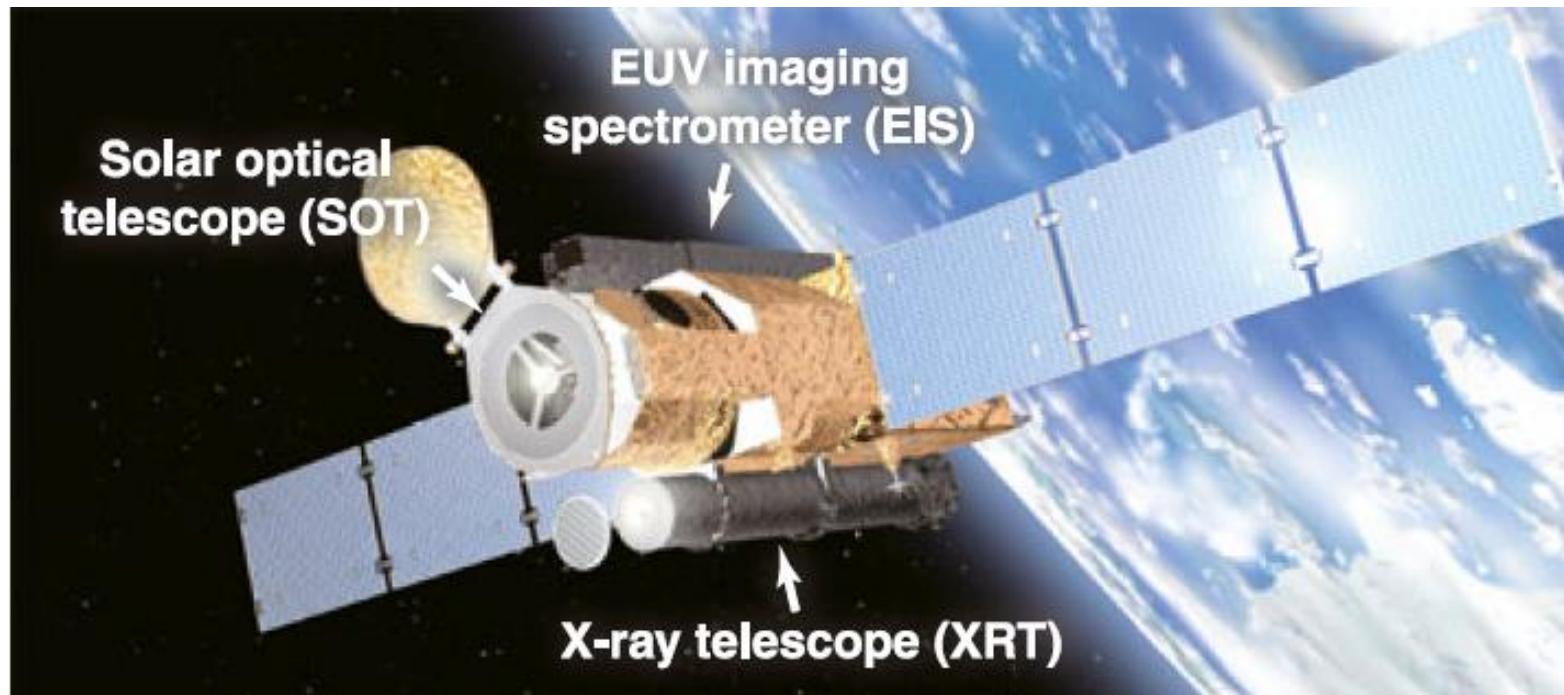


EUV and X-ray Filters



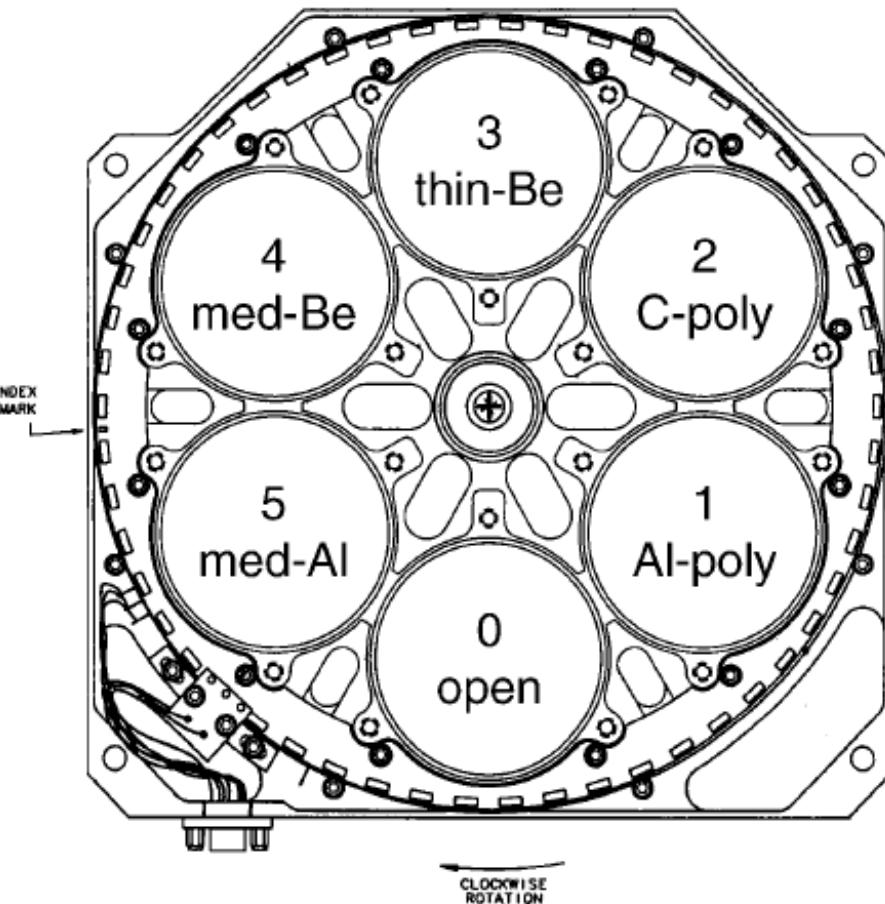
Hinode

- Hinode (“Sunrise”) – Japanese mission, launched 2006
- European and US collaboration
- The **X-Ray Telescope (XRT)**
 - multi-filter telescope
- **EUV Imaging Spectrometer (EIS)**
 - 170-210 Å and 250-290 Å
 - slit-slot mech. 1”, 2”, 40”, 266”
- **Solar Optical Telescope (SOT)**
 - 0.5 m mirror, filter packages

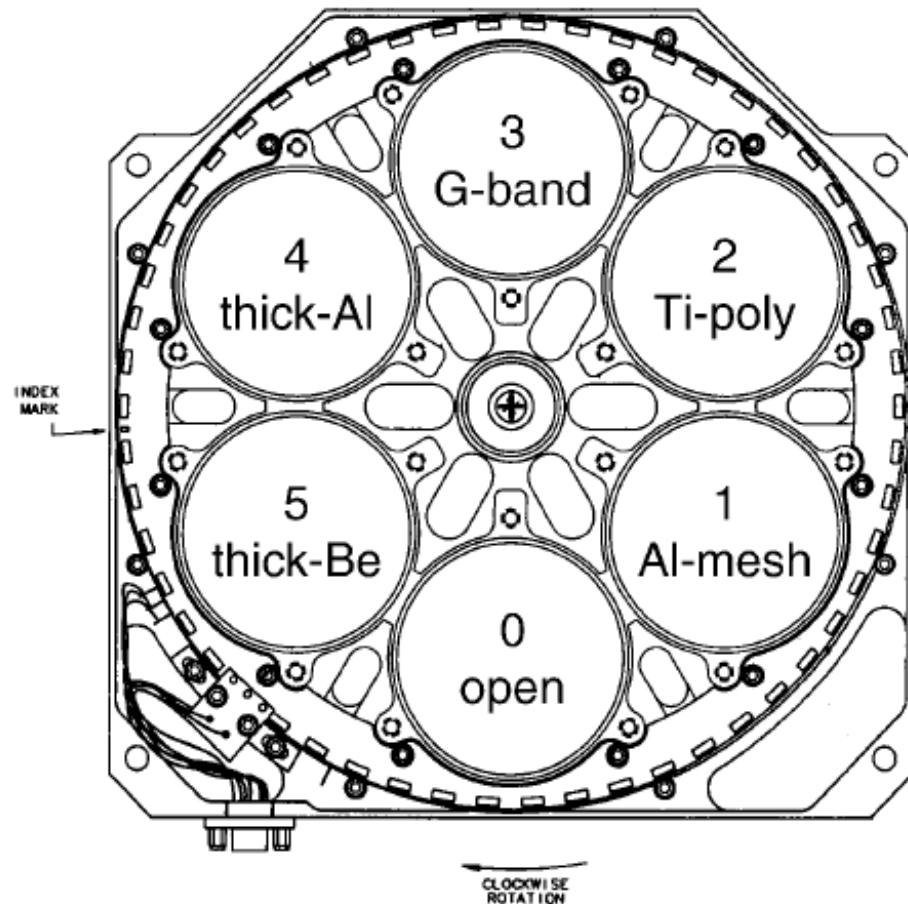


Hinode/XRT

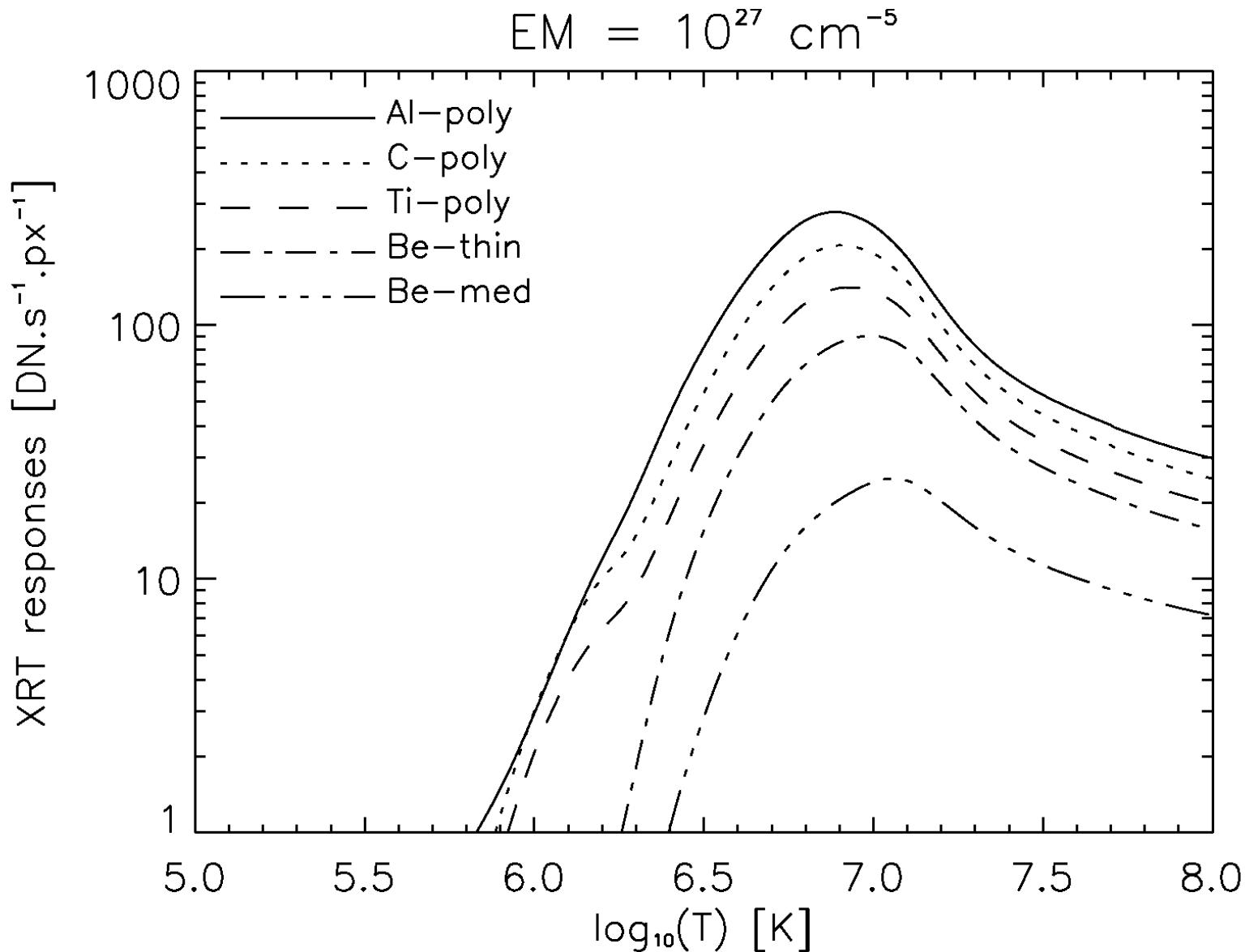
filter wheel 1



filter wheel 2

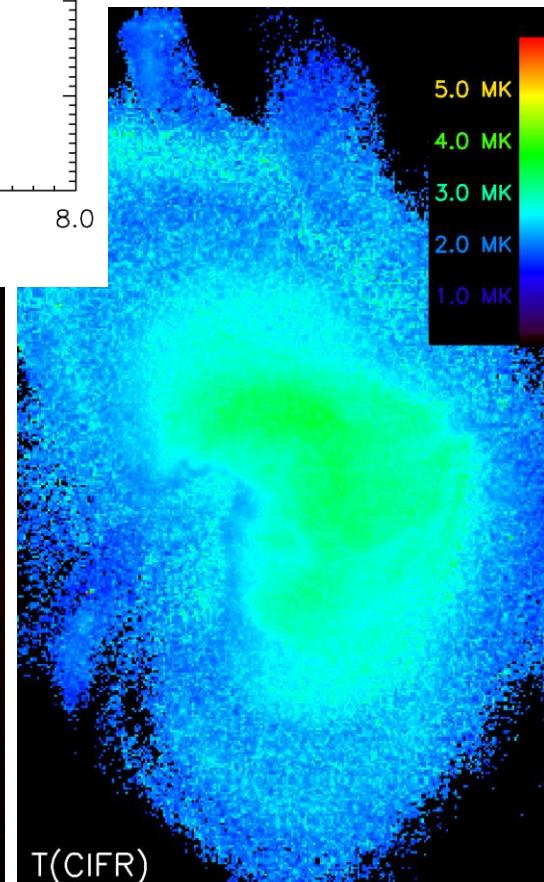
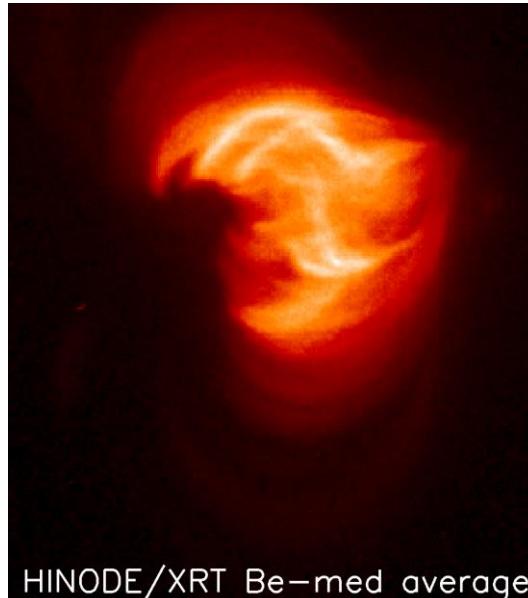
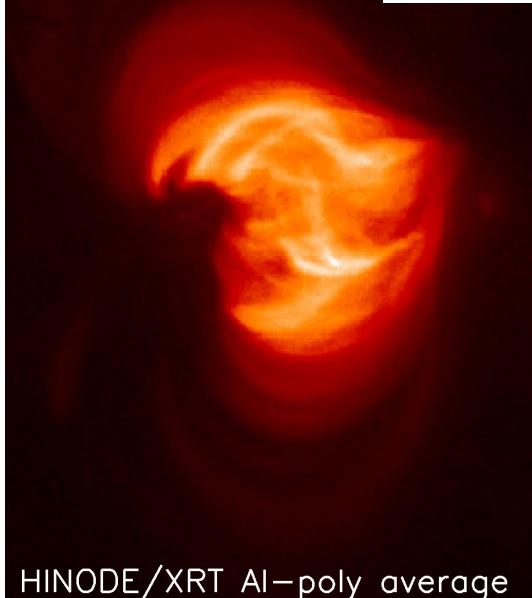
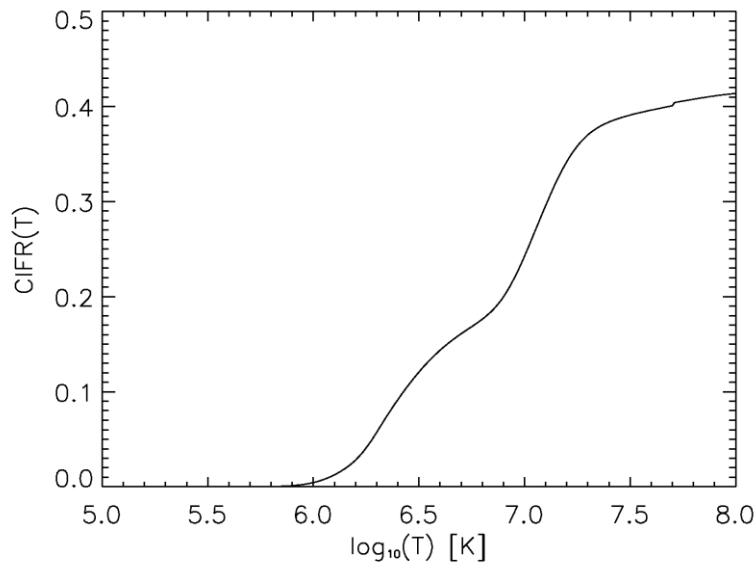
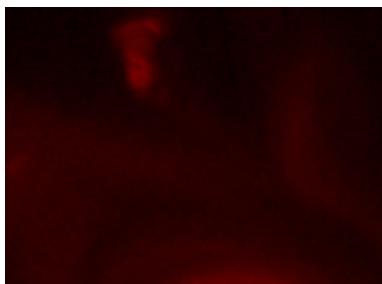


Hinode/XRT Temperature Response



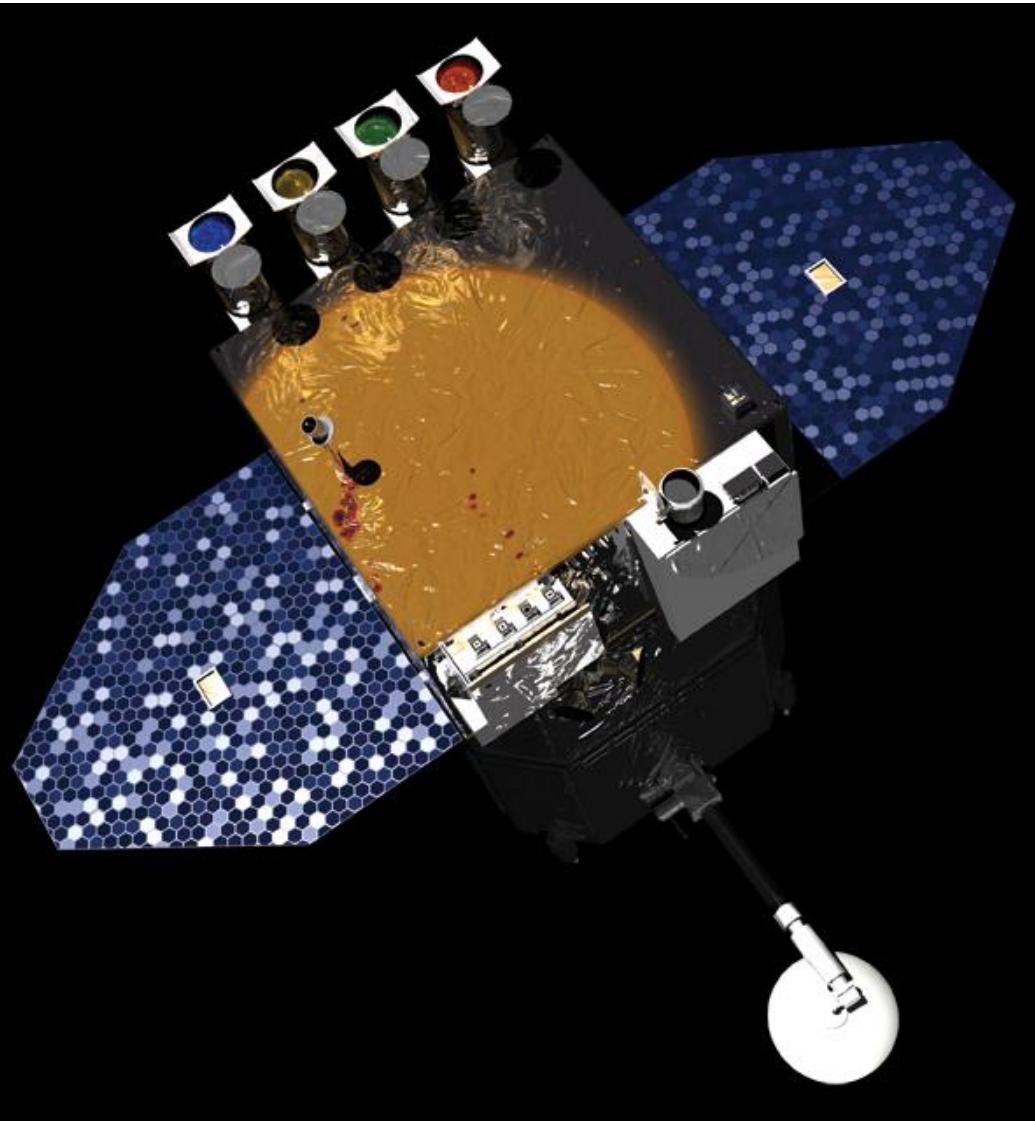
XRT Temperature Diagnostics

$$CIFR(T) = \frac{\left(\prod_{i=1}^5 F_i(T) \right)^{2/5}}{F_1(T)F_2(T)}$$



*Reale et al. (2007)
Science 317, 1582*

Atmospheric Imaging Assembly



Solar Dynamics Observatory:

- NASA, launched 2010
- current workhorse for Solar Physics

Atmospheric Imaging Assembly (AIA):

- four identical EUV full-disc telescopes, state-of-the-art
- cadence of 12 seconds
- 0.6" px size, 1.5" resolution
- broad temperature coverage to study coronal and flare physics

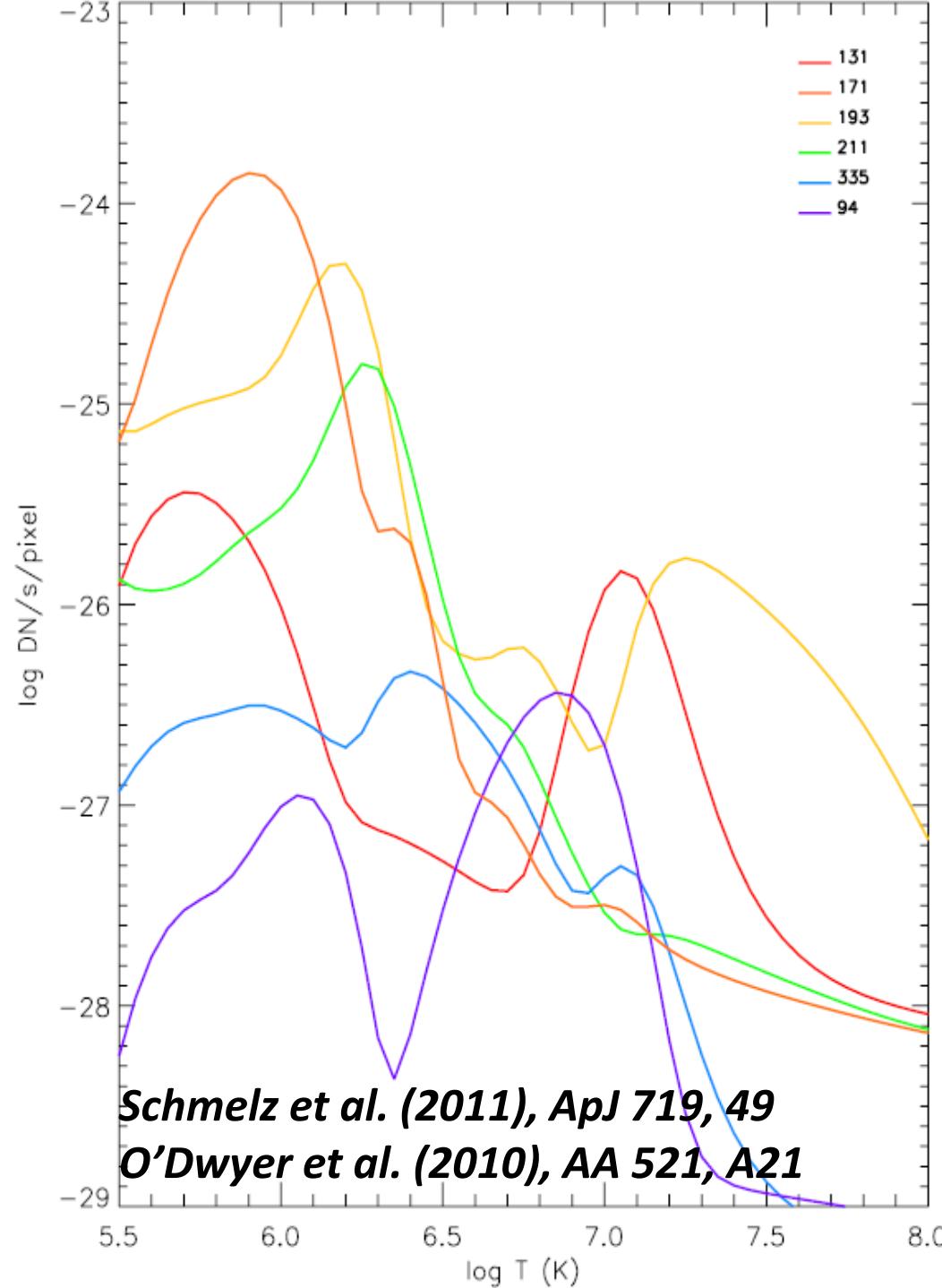
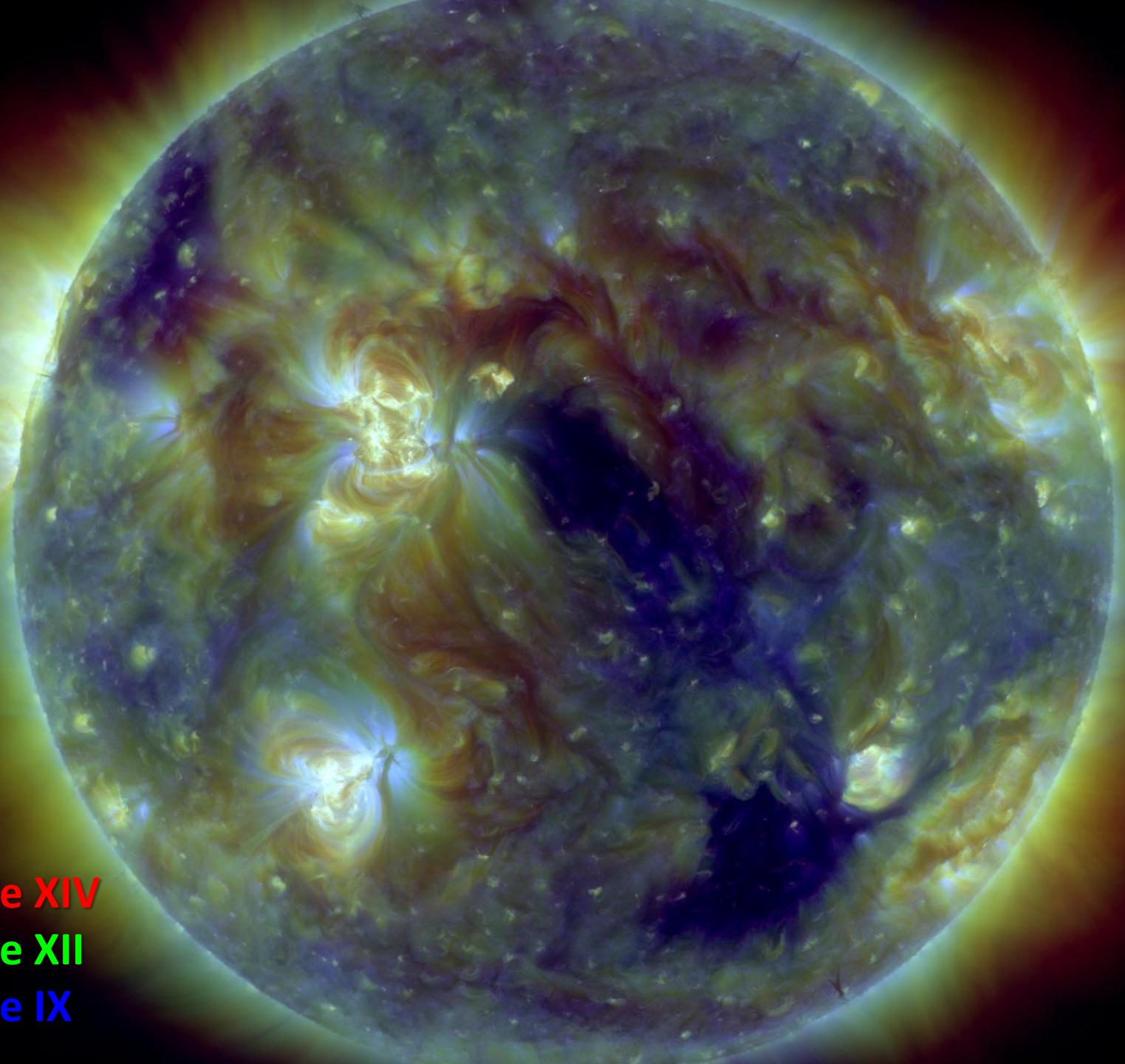


Table 1. Predicted AIA count rates.

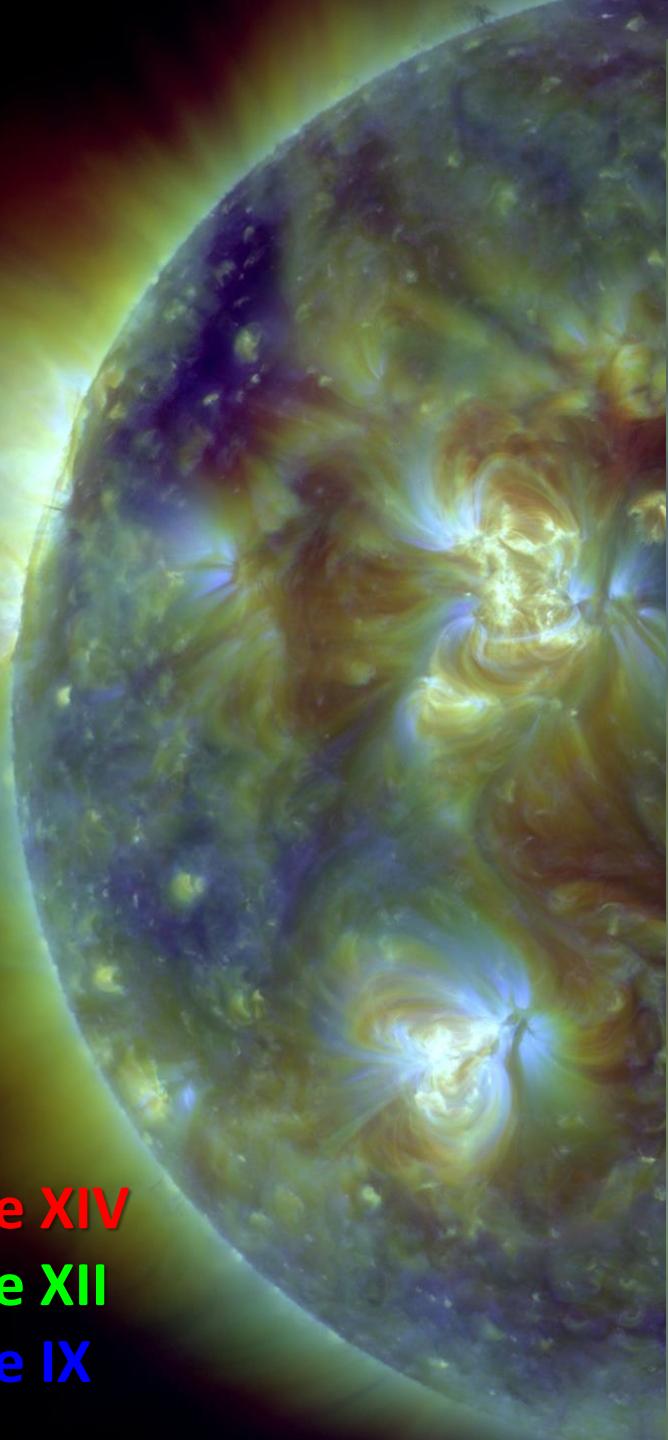
	Ion	λ Å	T_p^a K	Fraction of total emission			
				CH	QS	AR	FL
94 Å	Mg VIII	94.07	5.9	0.03	–	–	–
	Fe XX	93.78	7.0	–	–	–	0.10
	Fe XVIII	93.93	6.85	–	–	0.74	0.85
	Fe X	94.01	6.05	0.63	0.72	0.05	–
	Fe VIII	93.47	5.6	0.04	–	–	–
	Fe VII	93.62	5.6	0.05	–	–	–
	Cont.		0.11	0.12	0.17	–	–
131 Å	O VI	129.87	5.45	0.04	0.05	–	–
	Fe XXIII	132.91	7.15	–	–	–	0.07
	Fe XXI	128.75	7.05	–	–	–	0.83
	Fe VIII	130.94	5.6	0.30	0.25	0.09	–
	Fe VII	131.24	5.6	0.39	0.33	0.13	–
	Cont.		0.11	0.20	0.54	0.04	–
171 Å	Ni XIV	171.37	6.35	–	–	0.04	–
	Fe X	174.53	6.05	–	0.03	–	–
	Fe IX	171.07	5.85	0.95	0.92	0.80	0.54
	Cont.		–	–	–	–	0.23
193 Å	O V	192.90	5.35	0.03	–	–	–
	Ca XVII	192.85	6.75	–	–	–	0.08
	Ca XIV	193.87	6.55	–	–	0.04	–
	Fe XXIV	192.03	7.25	–	–	–	0.81
	Fe XII	195.12	6.2	0.08	0.18	0.17	–
	Fe XII	193.51	6.2	0.09	0.19	0.17	–
	Fe XII	192.39	6.2	0.04	0.09	0.08	–
	Fe XI	188.23	6.15	0.09	0.10	0.04	–
	Fe XI	192.83	6.15	0.05	0.06	–	–
	Fe XI	188.30	6.15	0.04	0.04	–	–
	Fe X	190.04	6.05	0.06	0.04	–	–
	Fe IX	189.94	5.85	0.06	–	–	–
	Fe IX	188.50	5.85	0.07	–	–	–
	Cont.		–	–	0.05	0.04	–
211 Å	Cr IX	210.61	5.95	0.07	–	–	–
	Ca XVI	208.60	6.7	–	–	–	0.09
	Fe XVII	204.67	6.6	–	–	–	0.07
	Fe XIV	211.32	6.3	–	0.13	0.39	0.12
	Fe XIII	202.04	6.25	–	0.05	–	–
	Fe XIII	203.83	6.25	–	–	0.07	–



211 Fe XIV

193 Fe XII

171 Fe IX

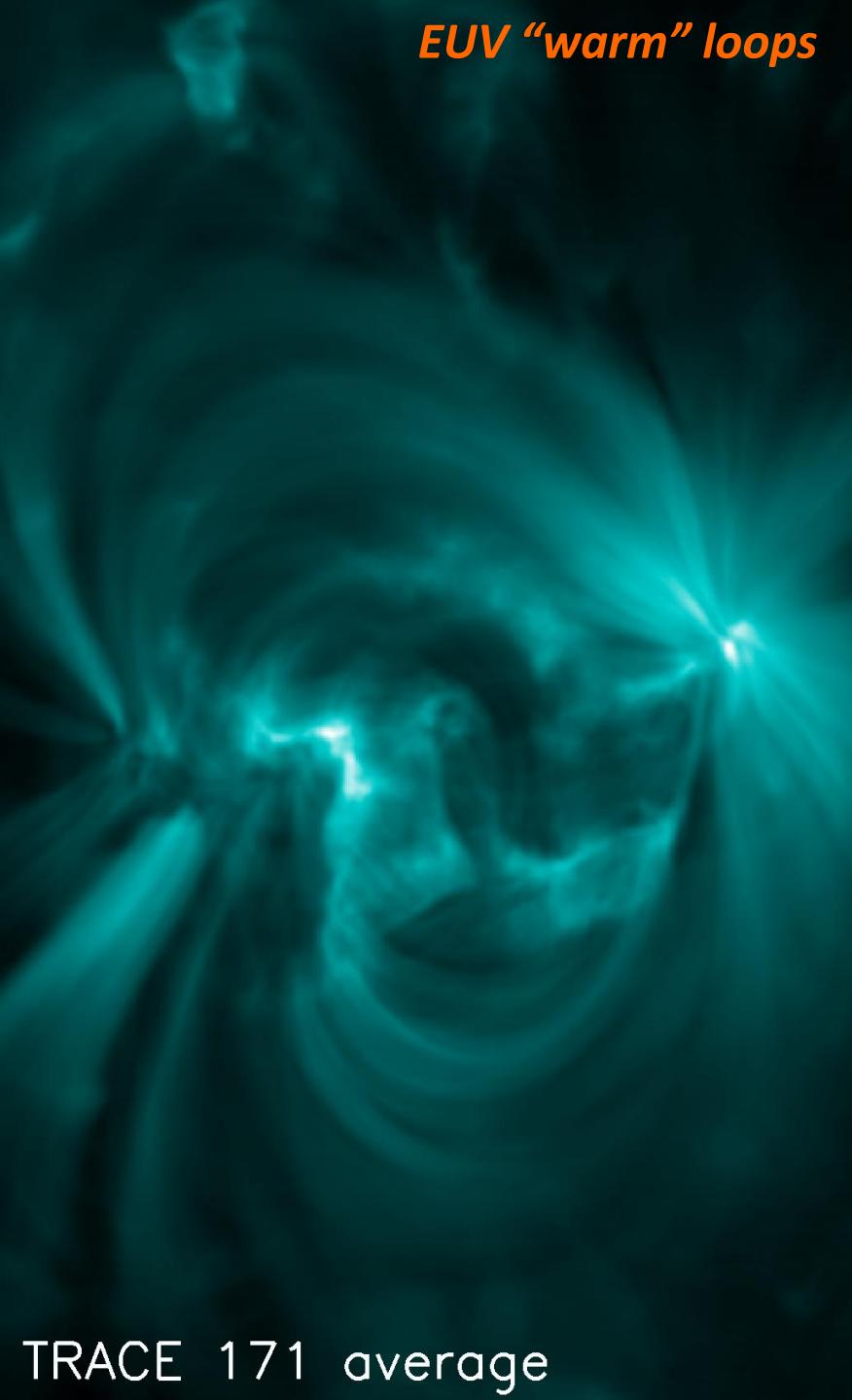


211 Fe XIV

193 Fe XII

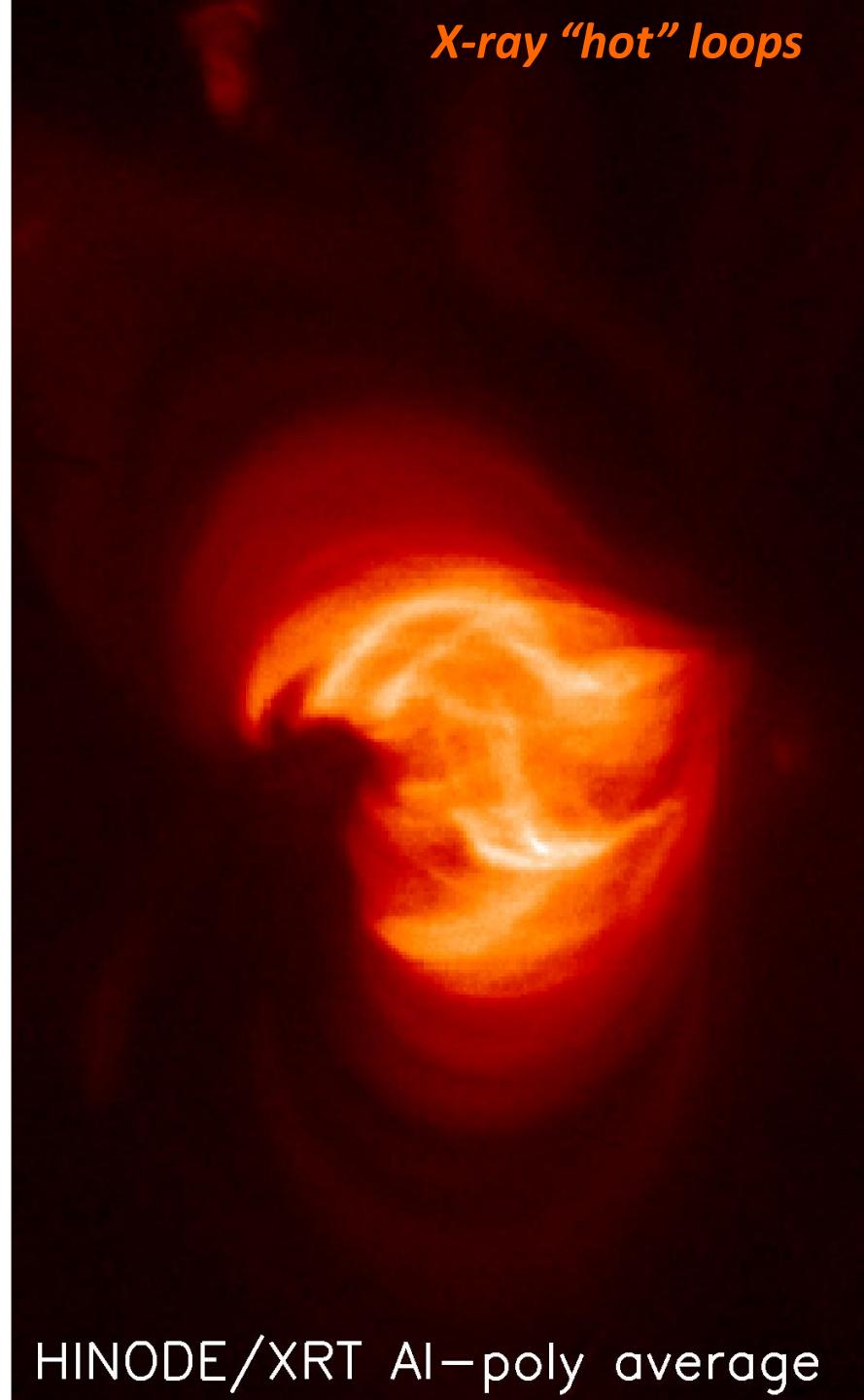
171 Fe IX

EUV “warm” loops

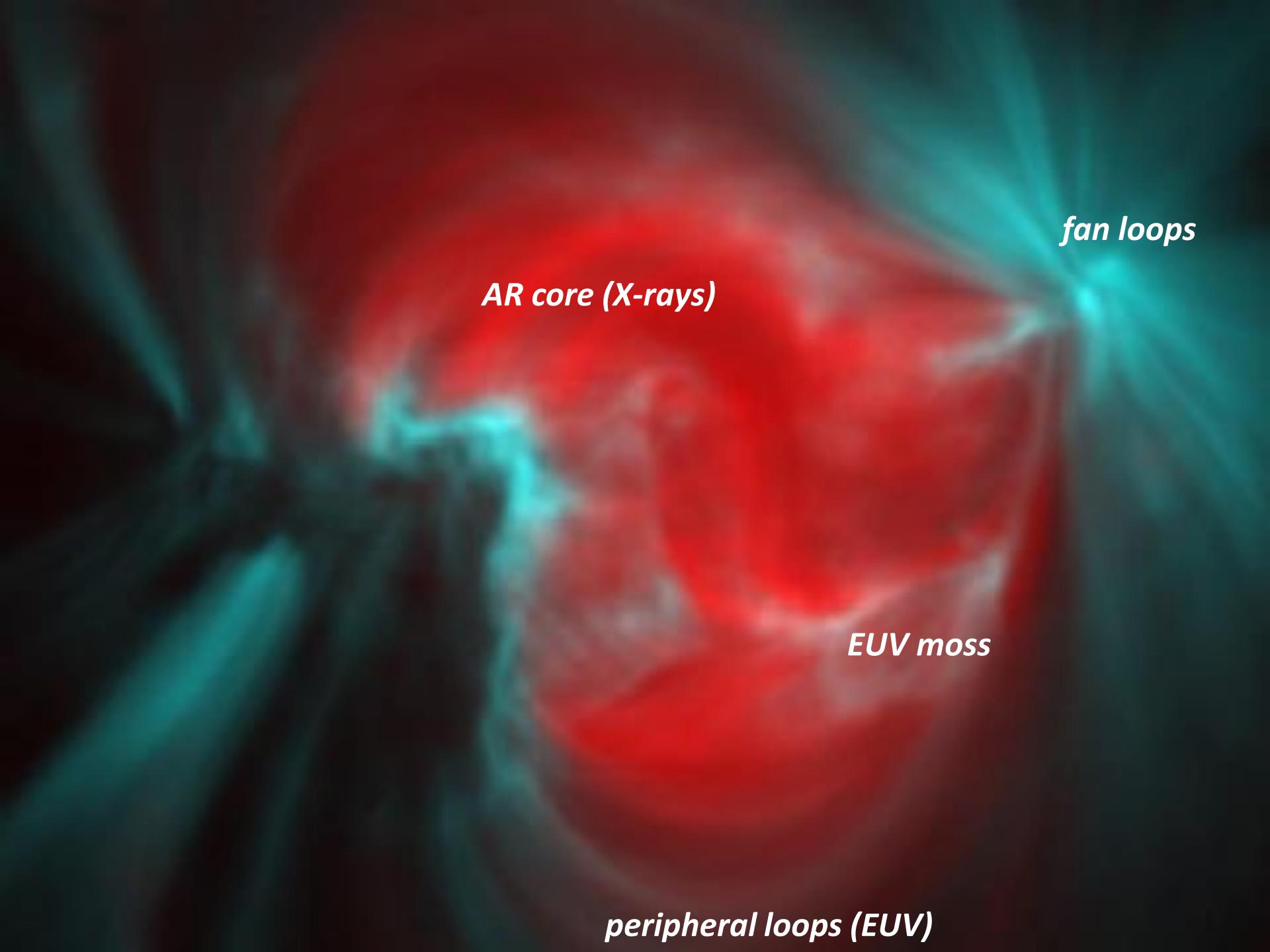


TRACE 171 average

X-ray “hot” loops



Hinode/XRT AI-poly average

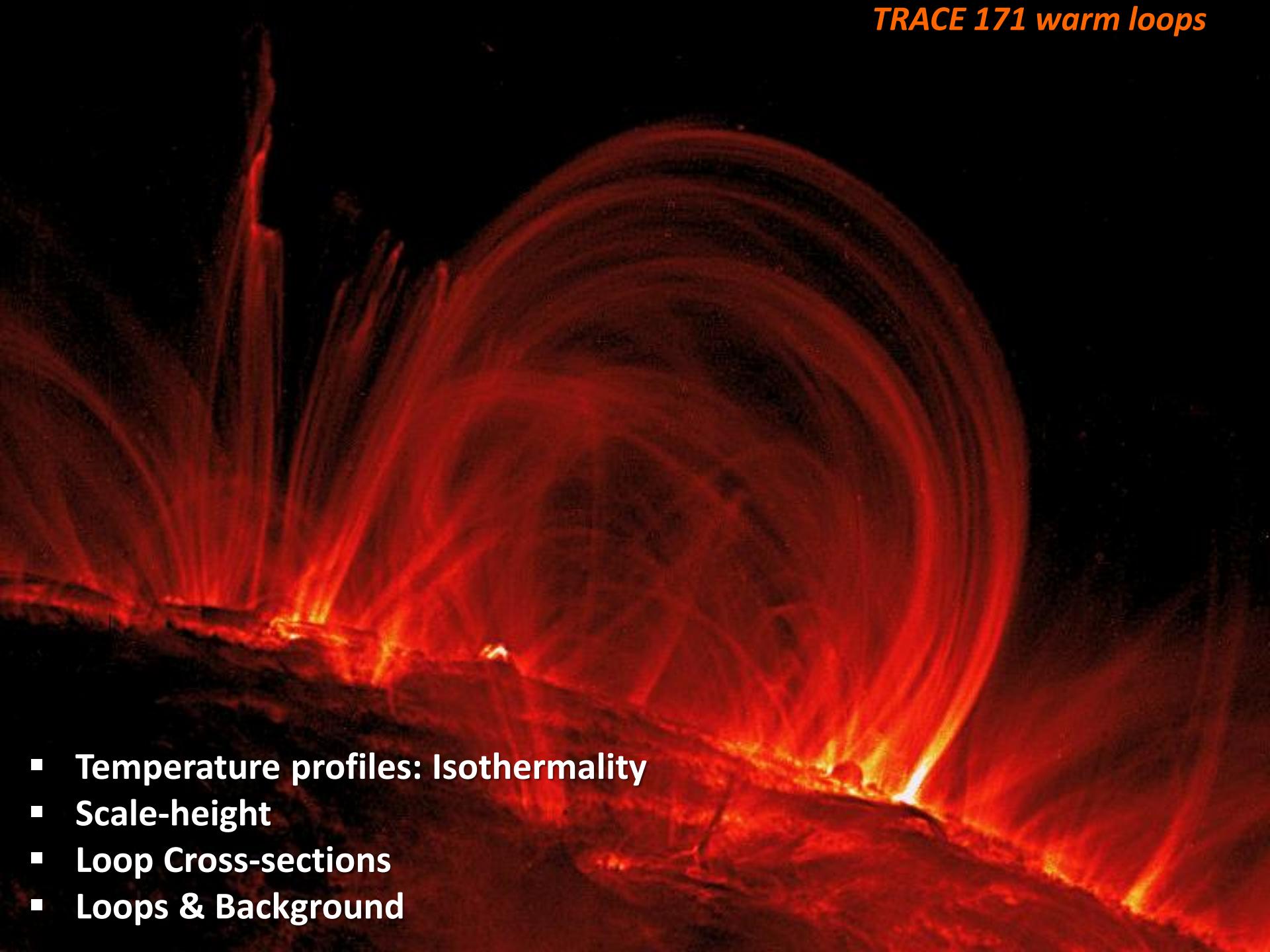


fan loops

AR core (X-rays)

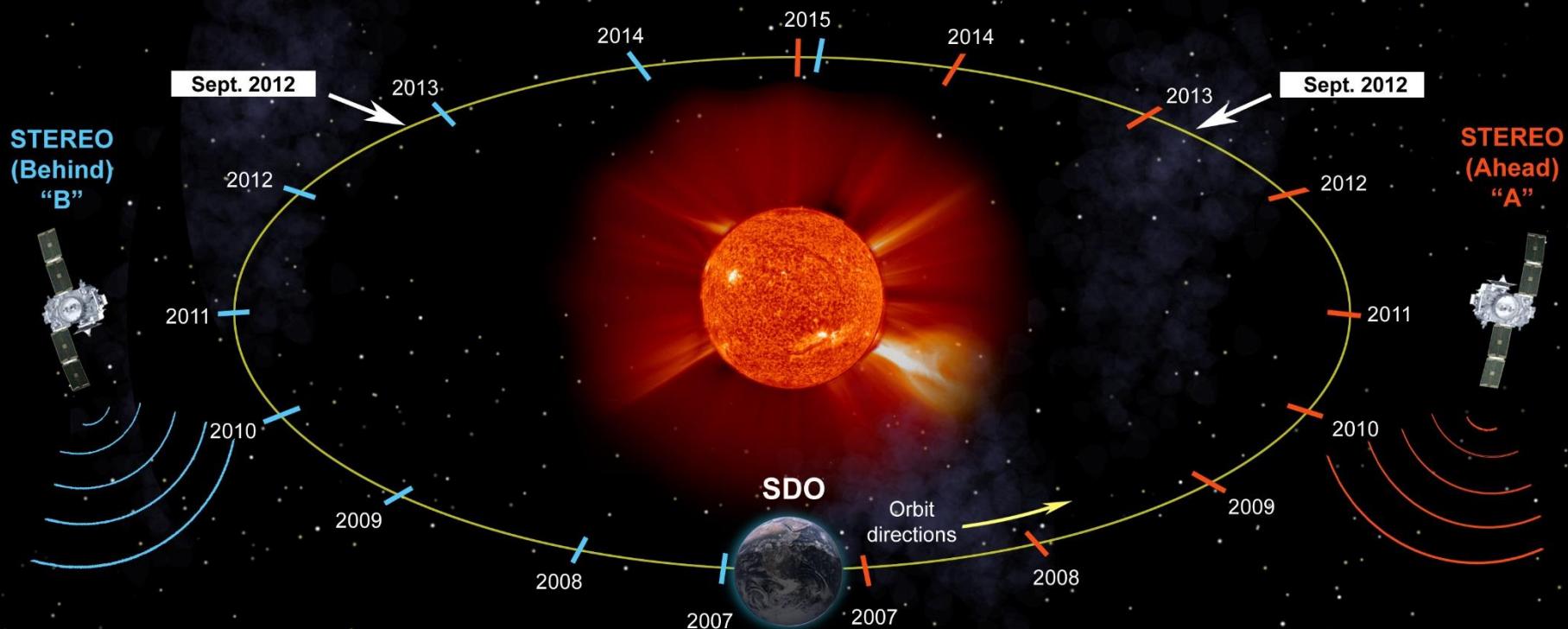
EUV moss

peripheral loops (EUV)



- Temperature profiles: Isothermality
- Scale-height
- Loop Cross-sections
- Loops & Background

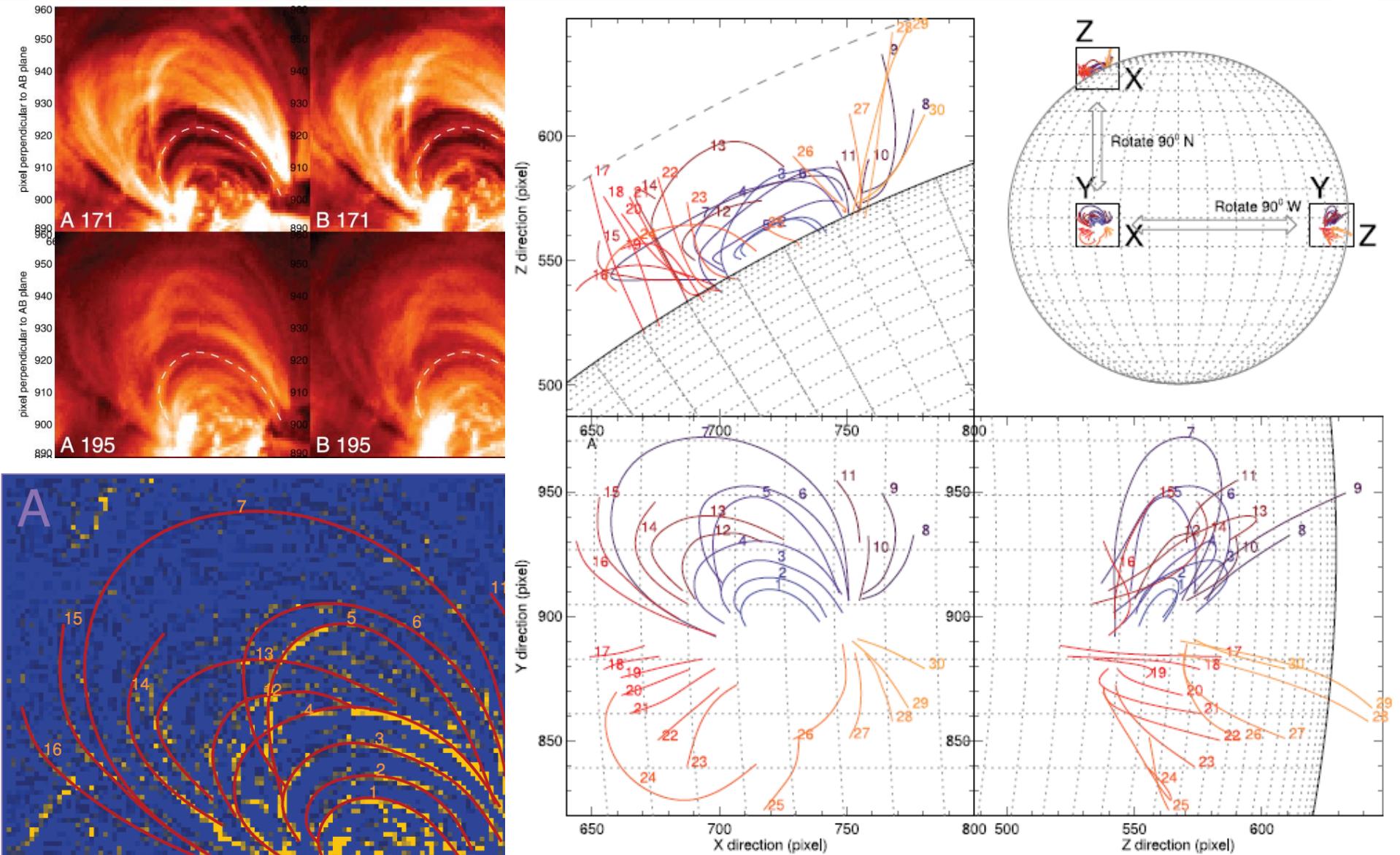
NASA's STEREO (with SDO) Sees the Entire Sun

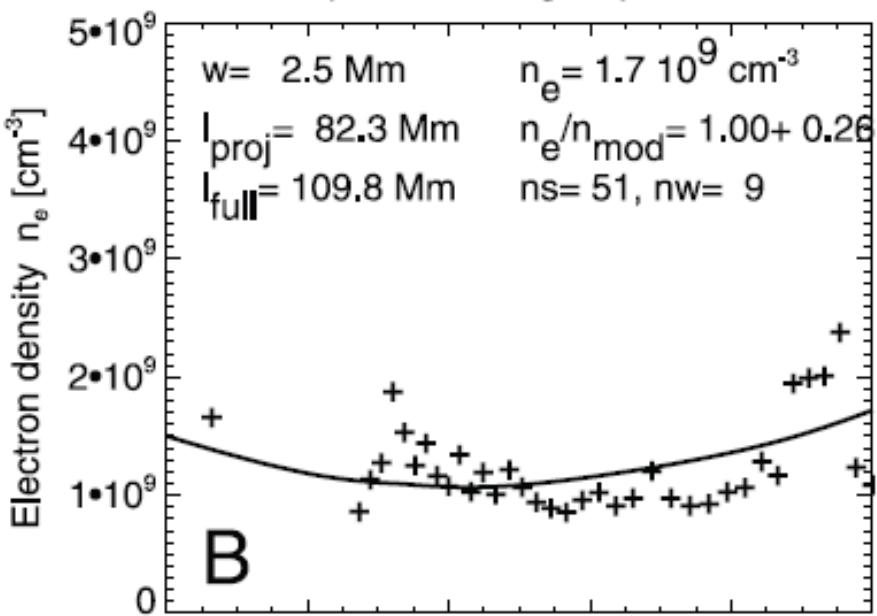
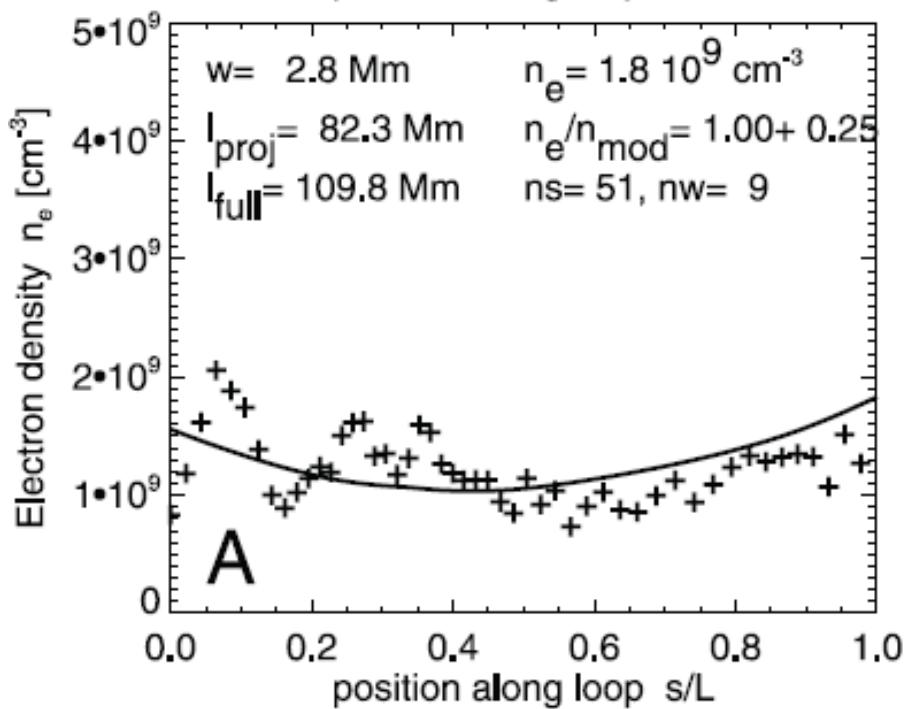
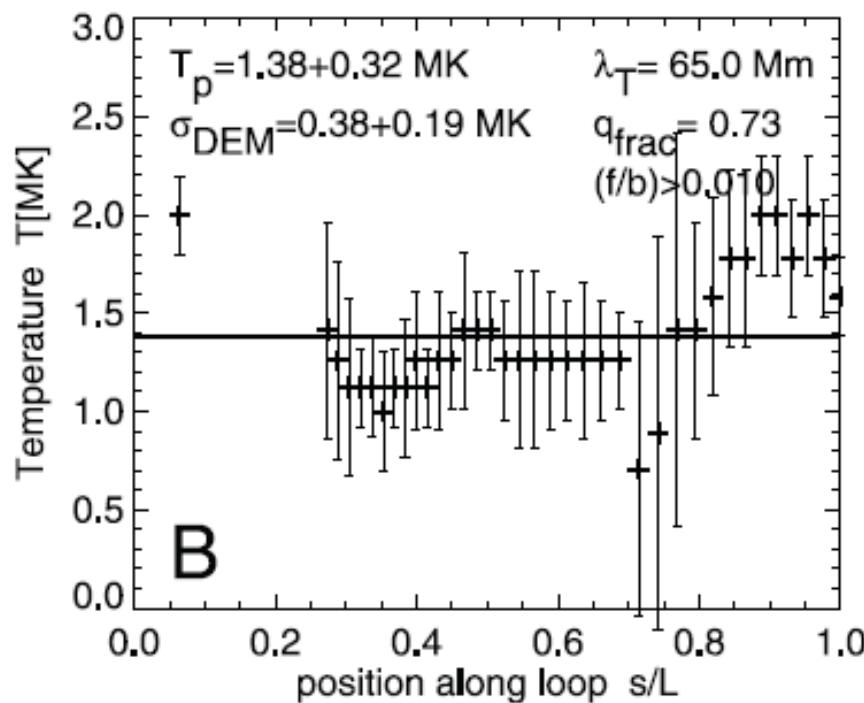
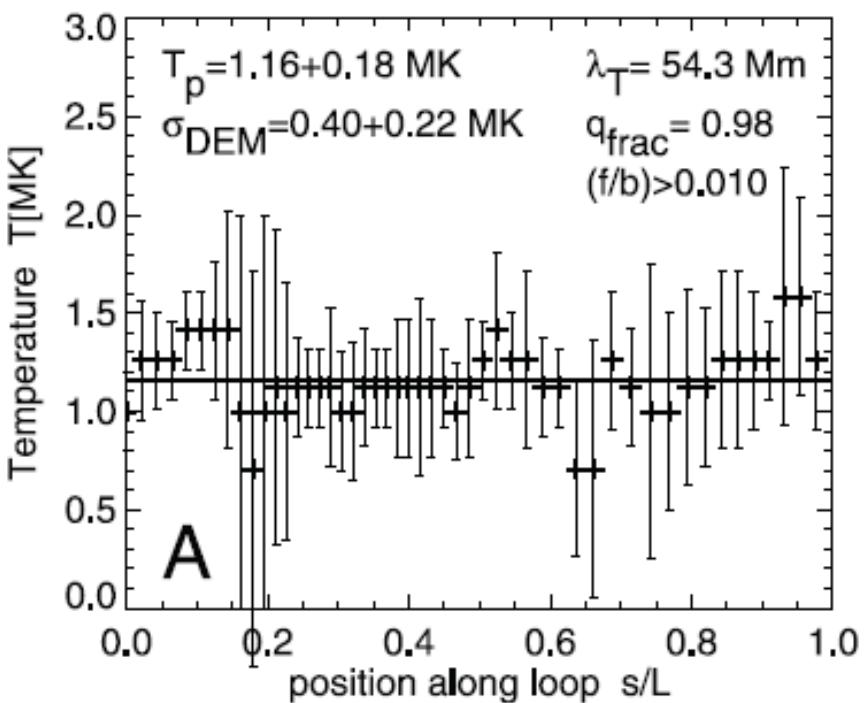


- The two **STEREO** spacecraft reach equidistant positions between themselves and Earth on Sept. 1, 2012.

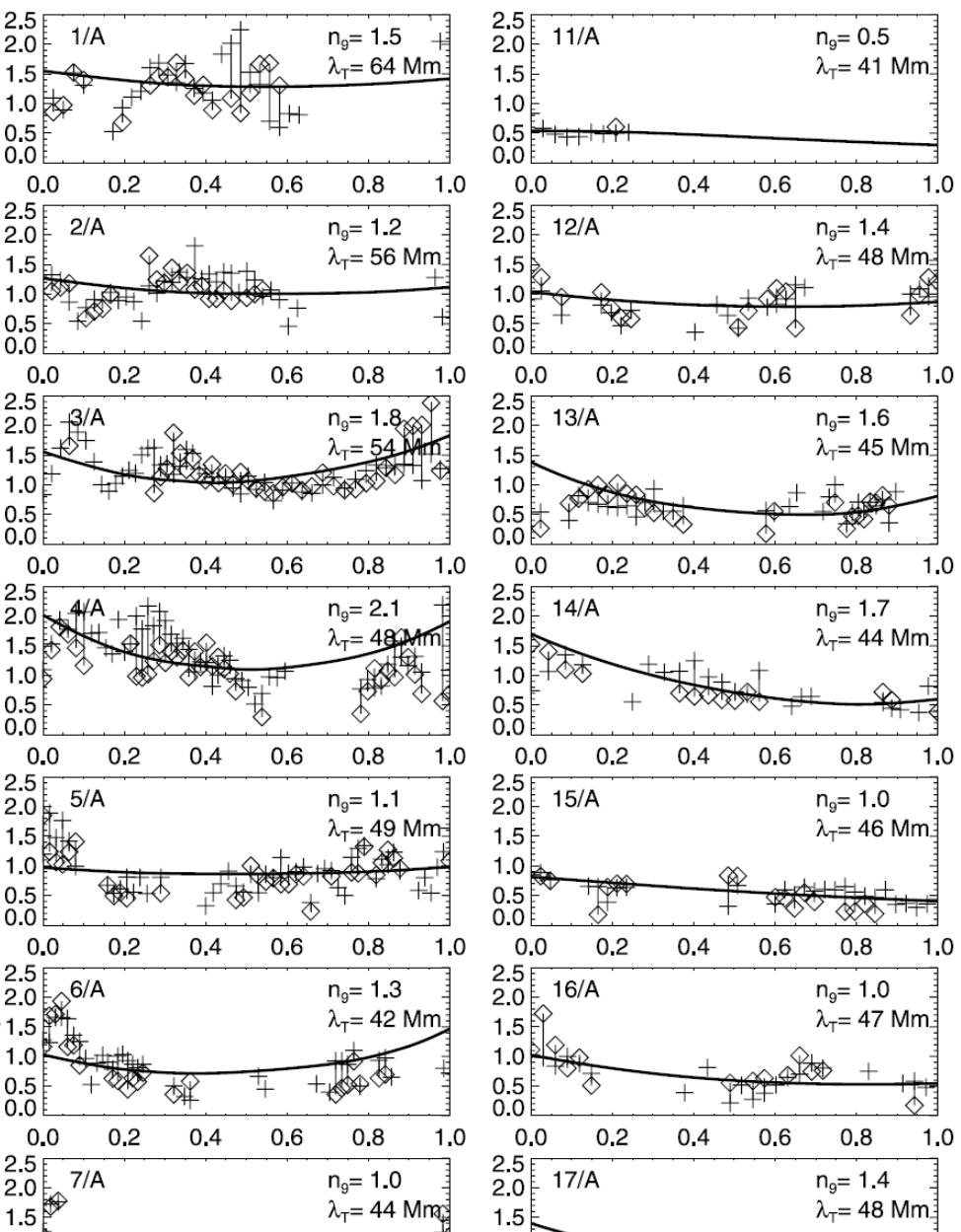
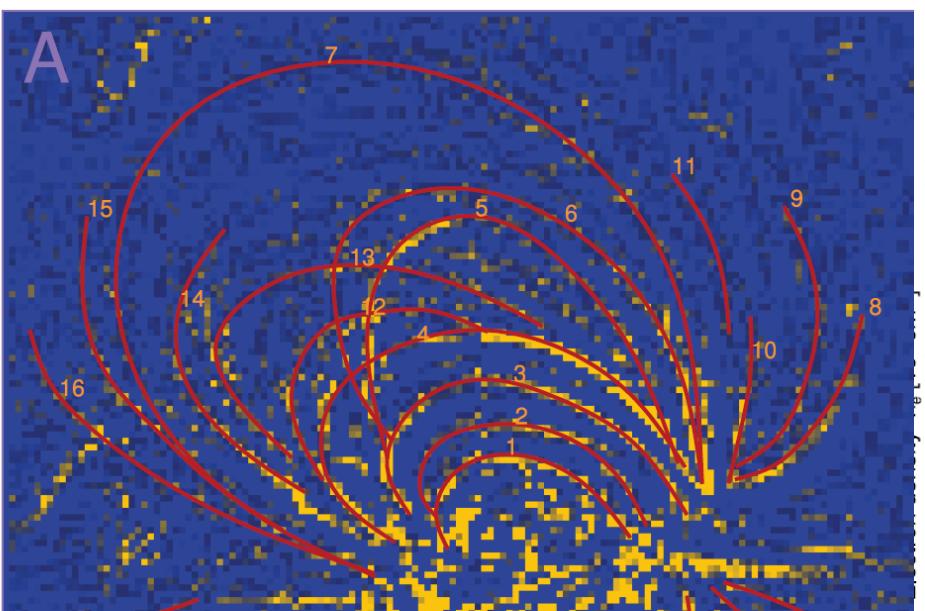
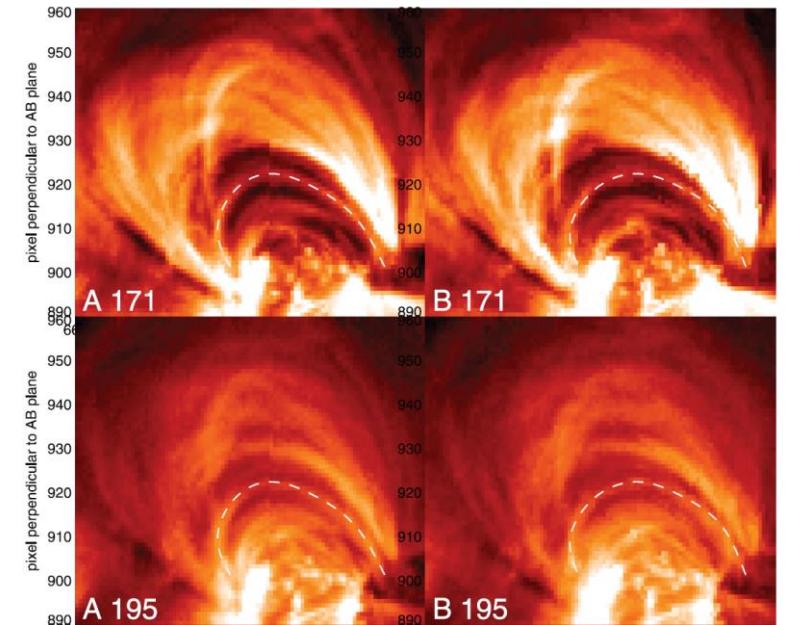
Drawing gives the relative orbital positions of both STEREO spacecraft for each year from June 2007 to June 2015.
(Not to scale)

Geometry of Coronal Loops



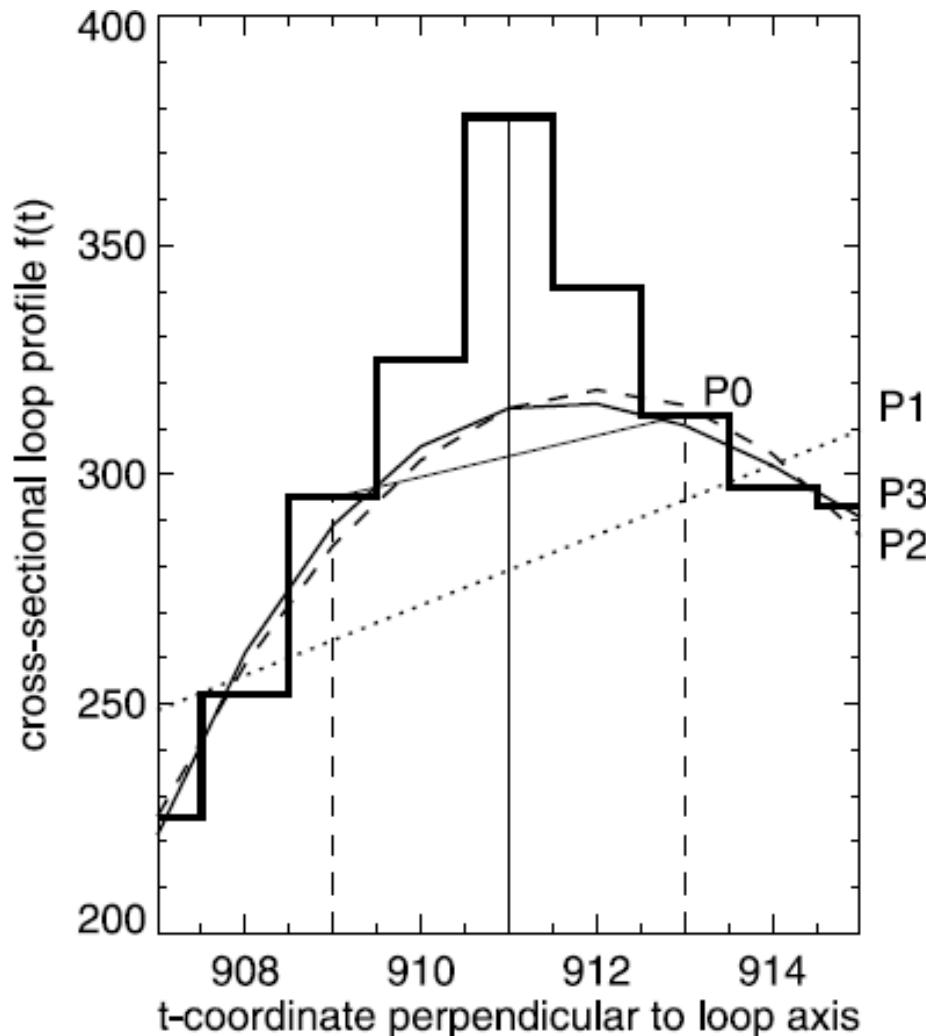
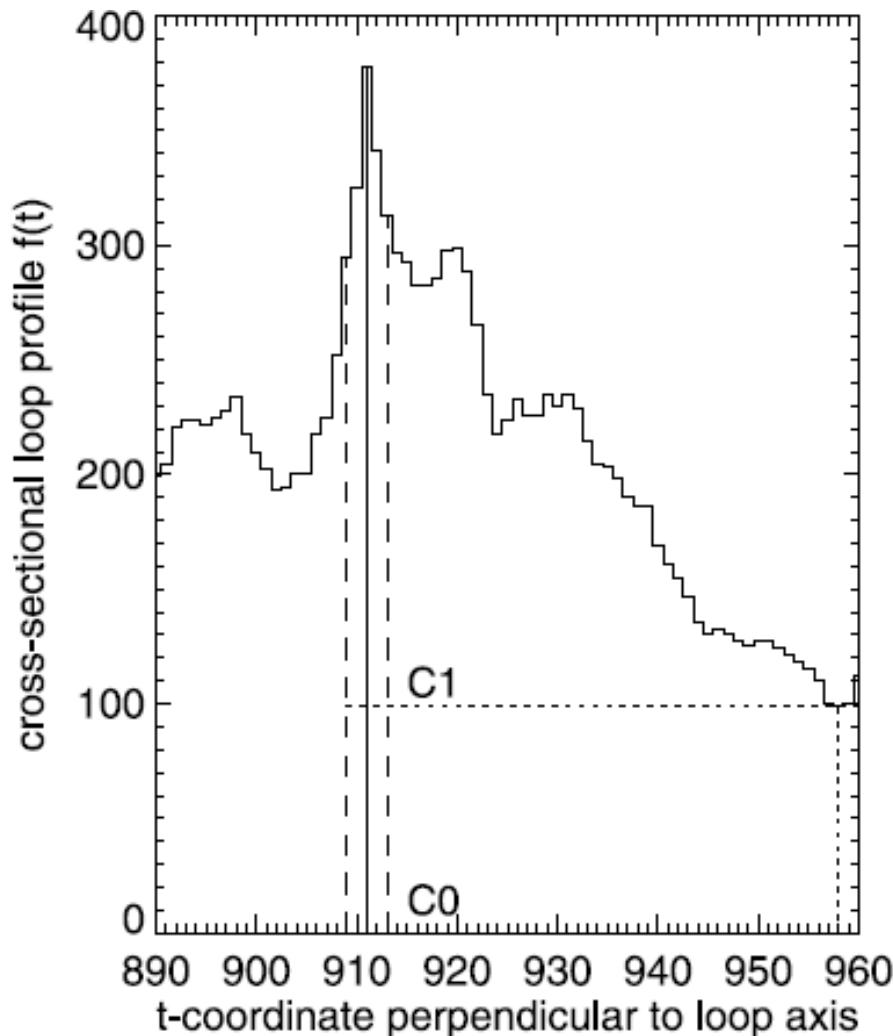


Loops can be Hydrostatic



Coronal Background

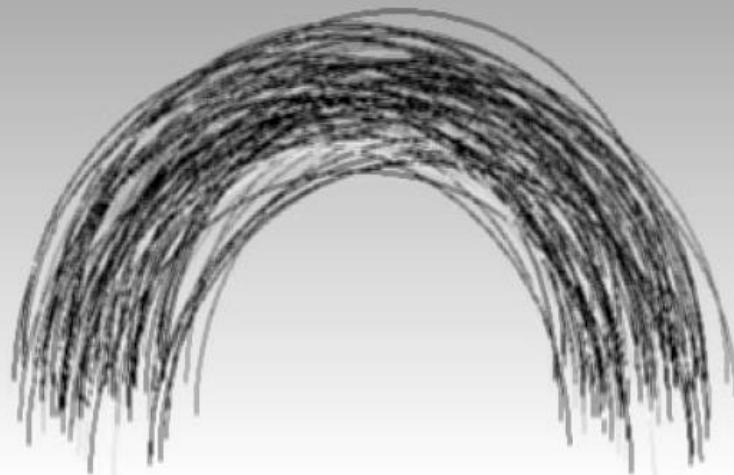
- Background can be $\sim 80\%$ of the actual observed signal:



Loops or Strands...

Aschwanden et al. (2000), ApJ 541, 1059

Multi-Thread Model



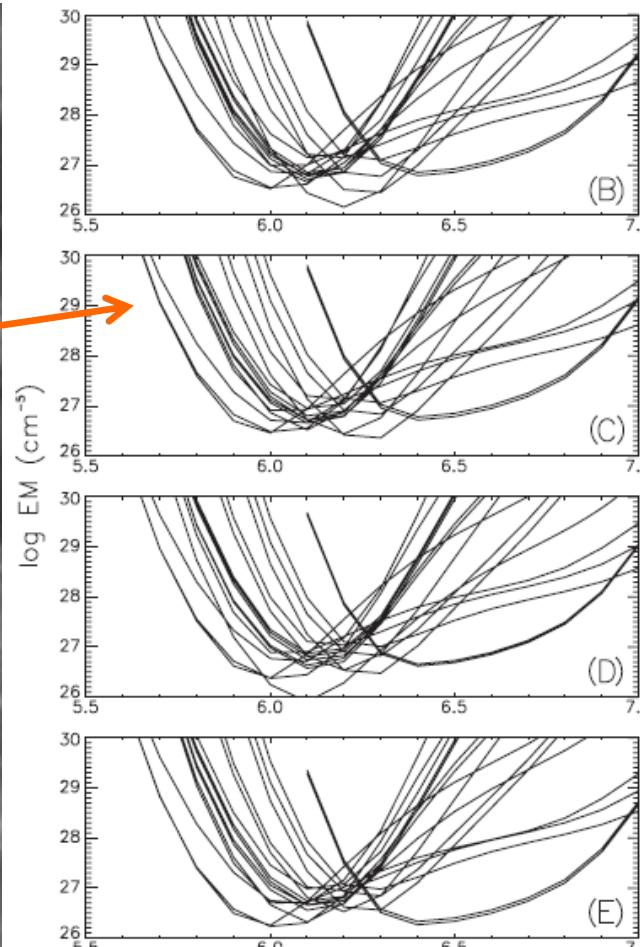
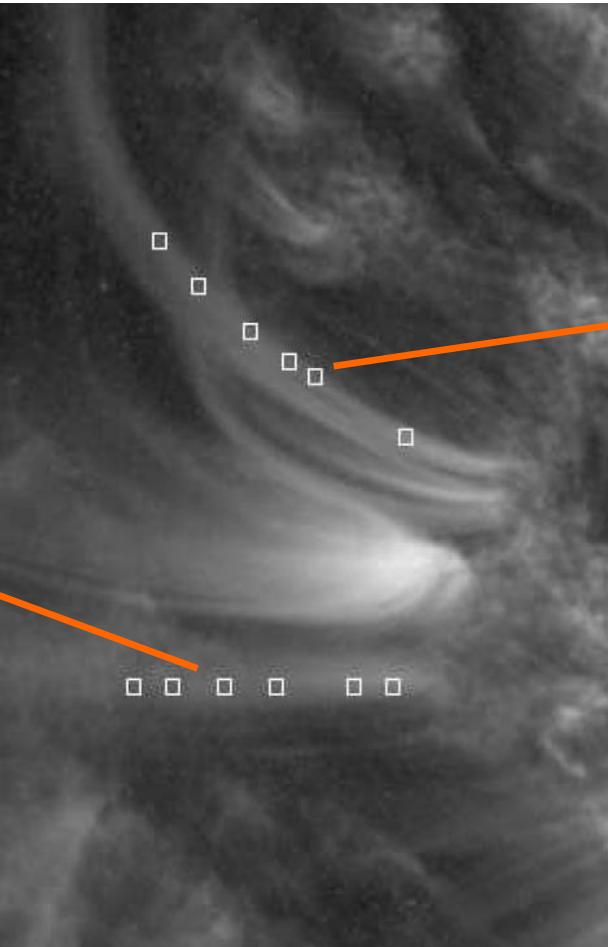
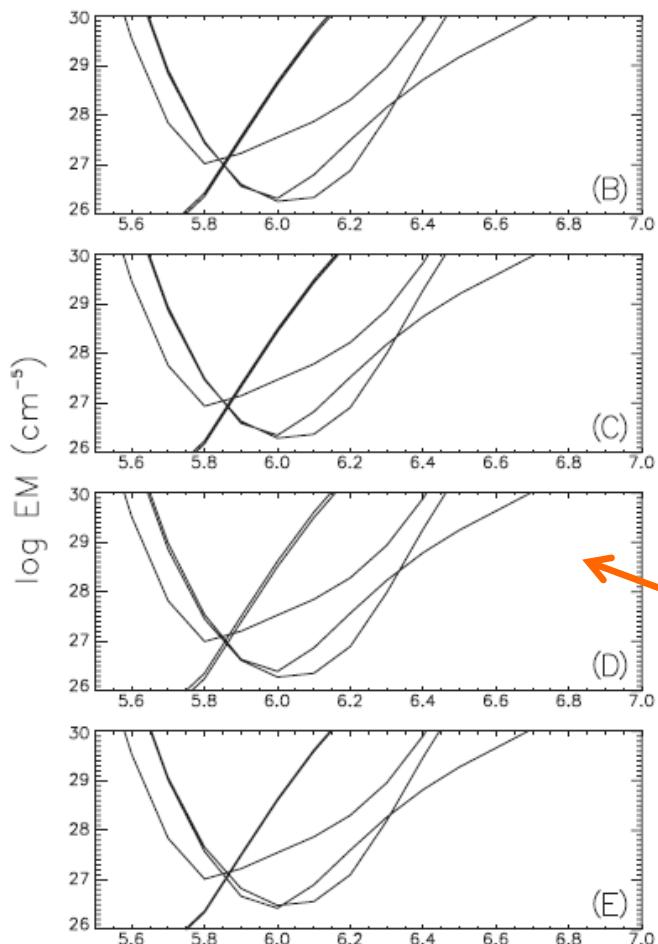
TRACE (0.5 arcsec)



- **Loop:** coherent structure in an observed image of the corona
- **Strand:** Fundamental, independent, elementary structure with an **isothermal cross-field profile**, thickness down to gyro-radius $< 1 \text{ m}$
- *Reale & Peres (2000), ApJ 521, L45: Multithermal, multi-strand loop, with different temperature structure for each strand, can produce false “isothermal” loop if unresolved*

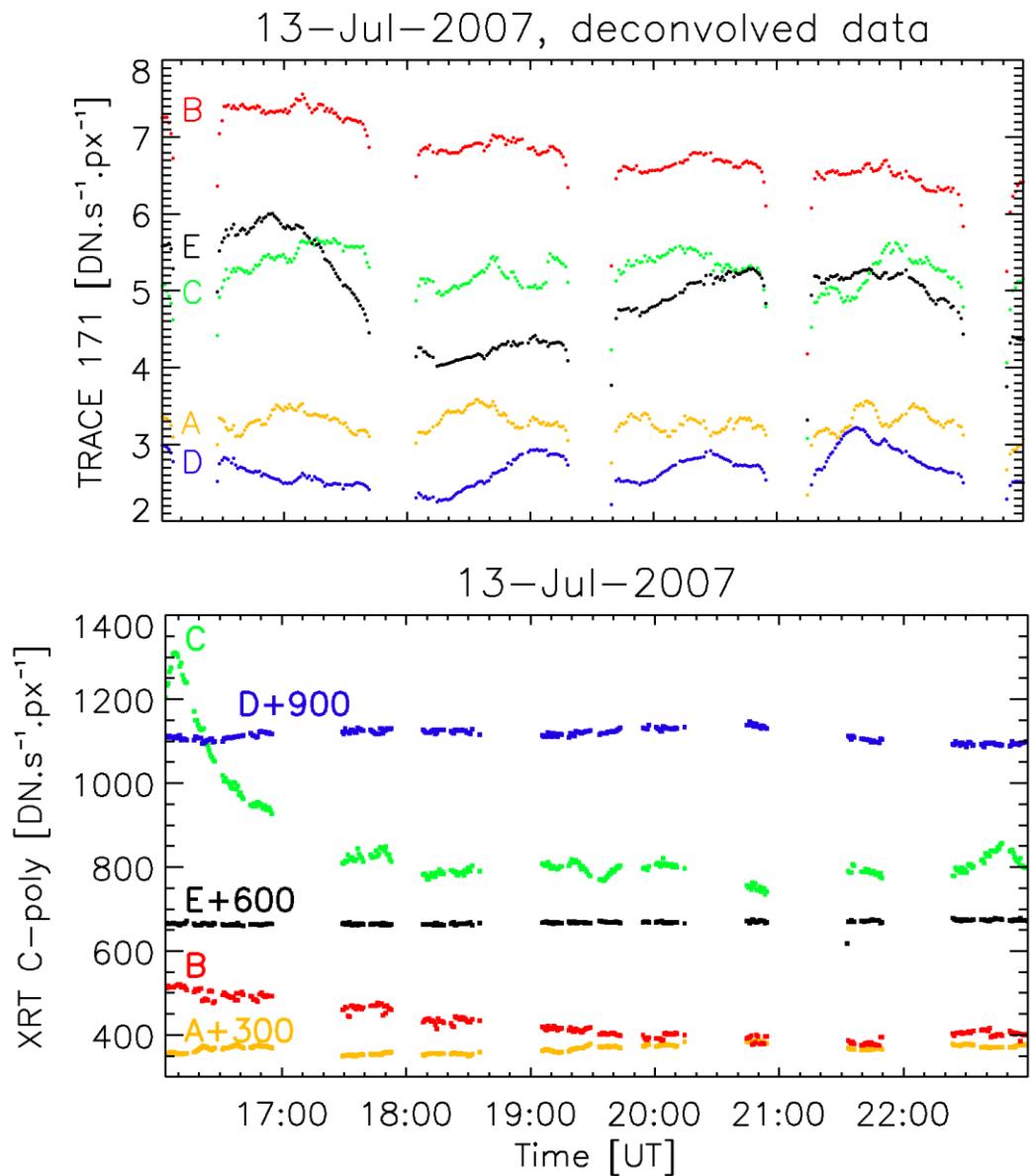
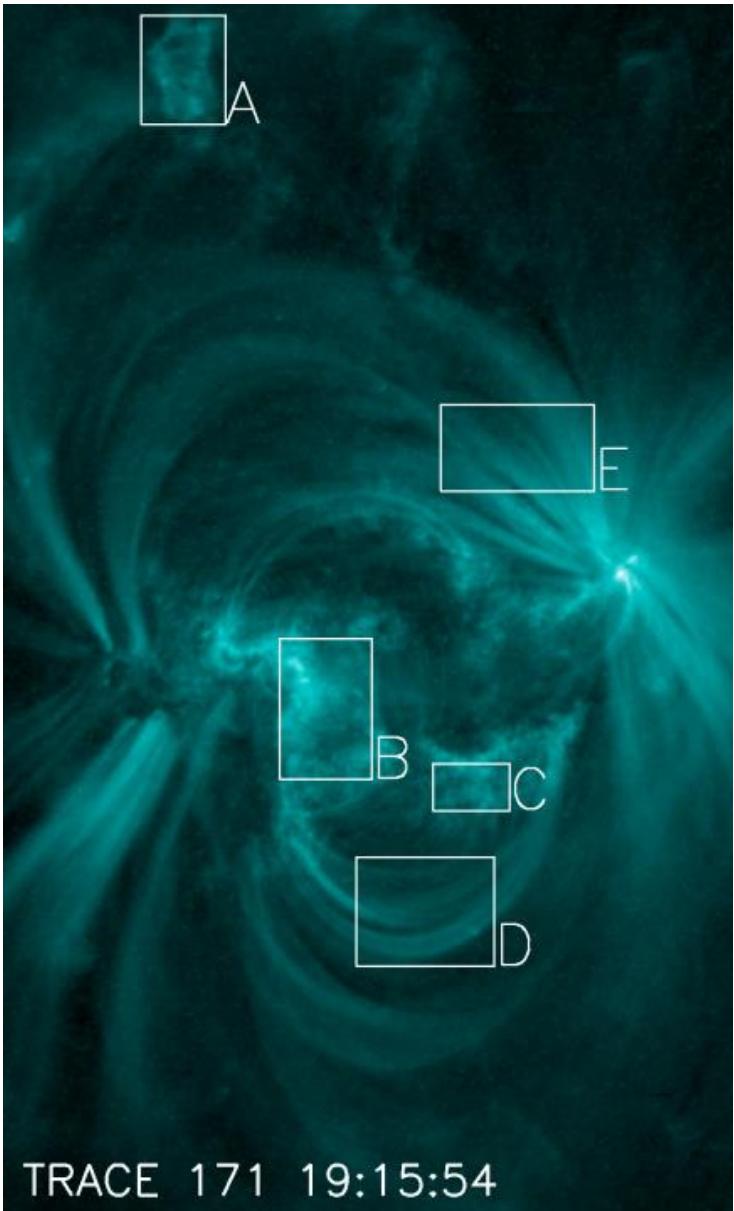
Isothermal or Multithermal?

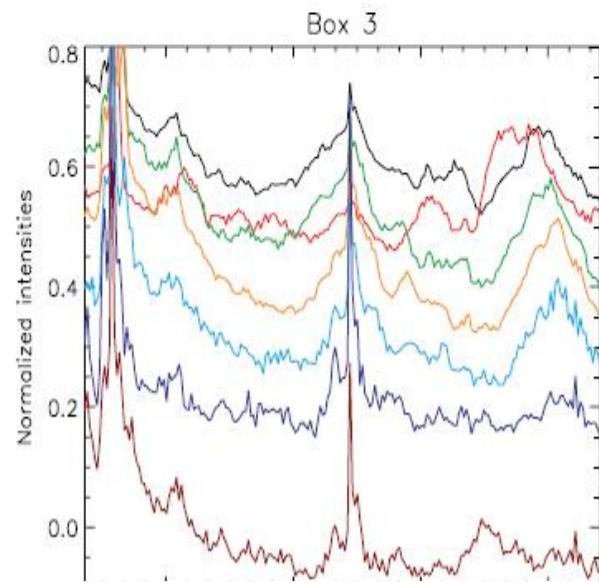
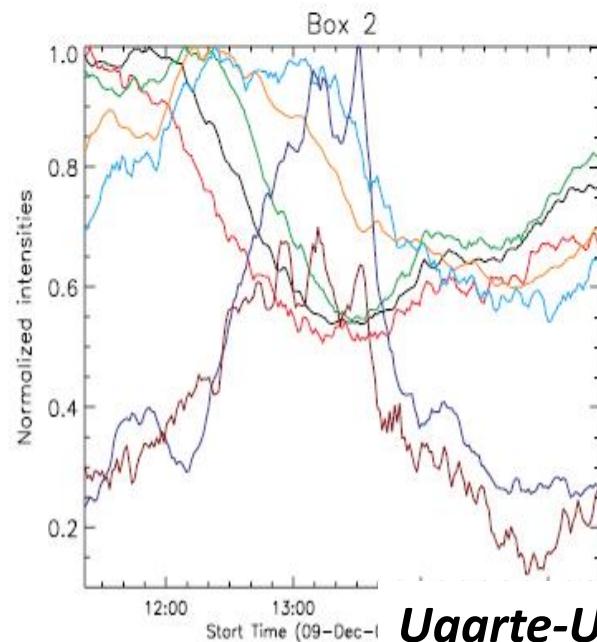
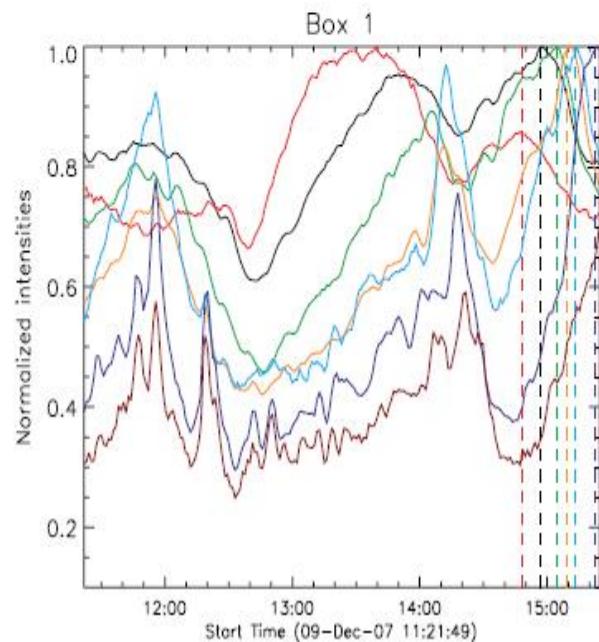
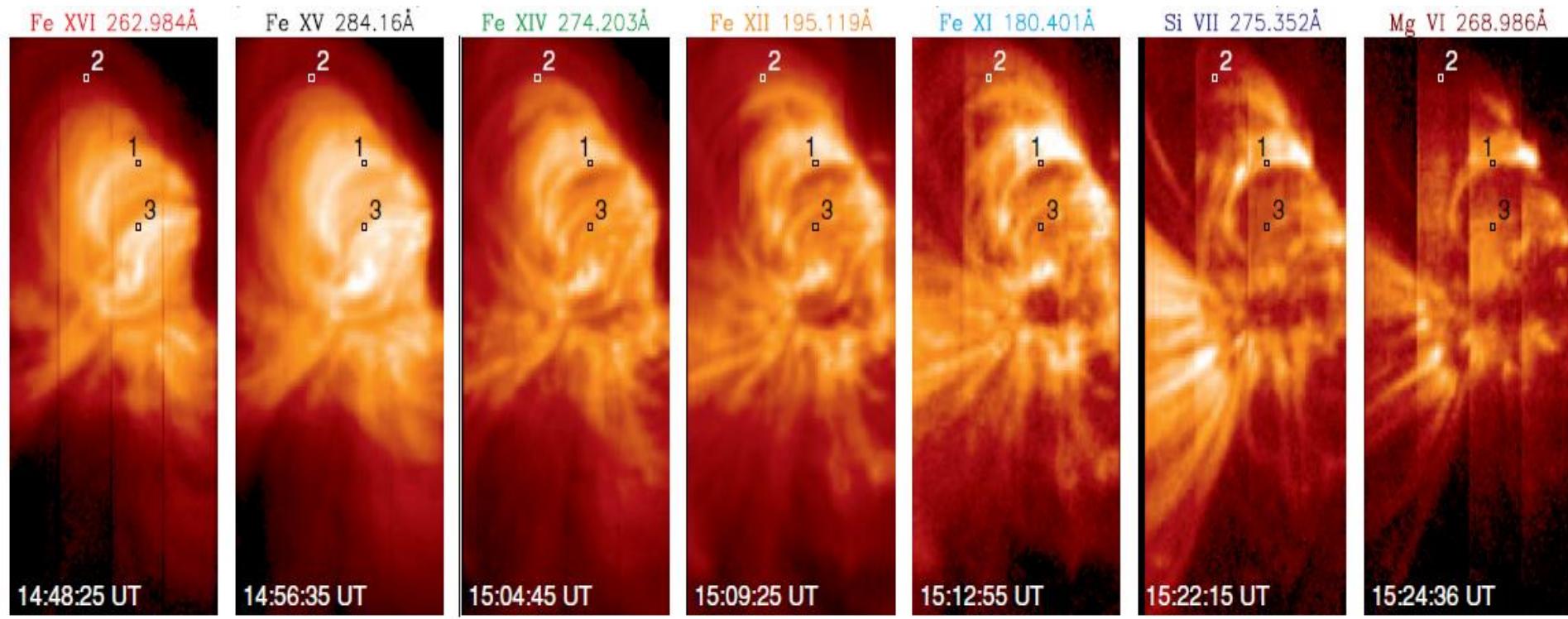
Schmelz et al. (2009): ApJ 691, 503: “Are Coronal Loops Isothermal or Multithermal?”



Conclusion: Yes

Loop Dynamics

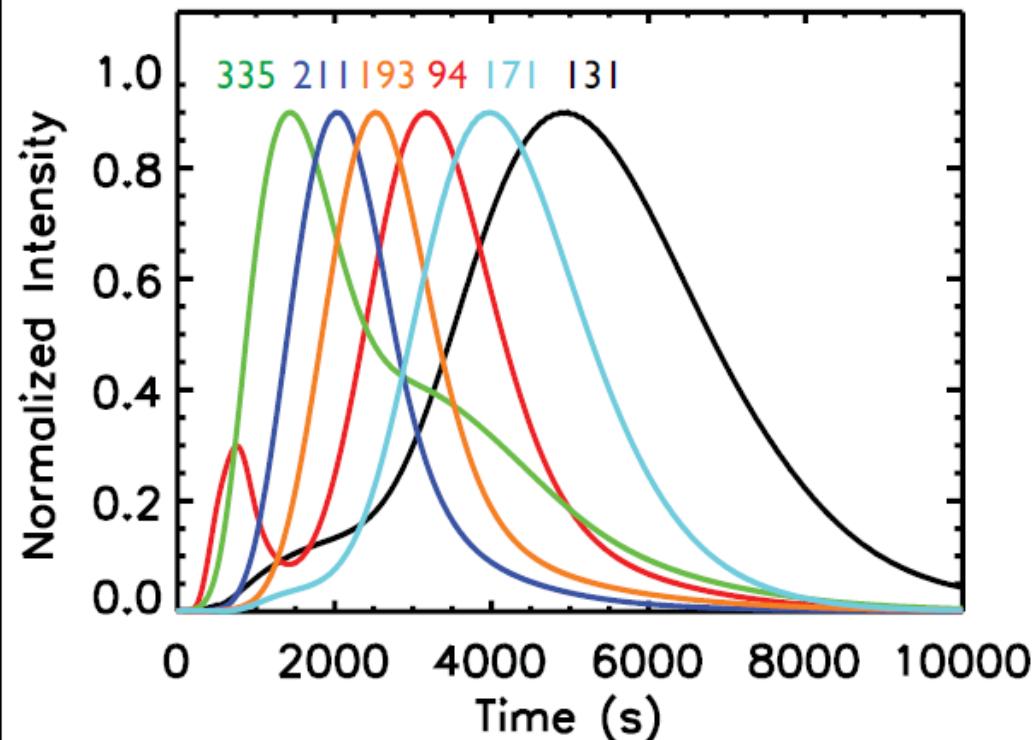




Nanoflare Storms

a)

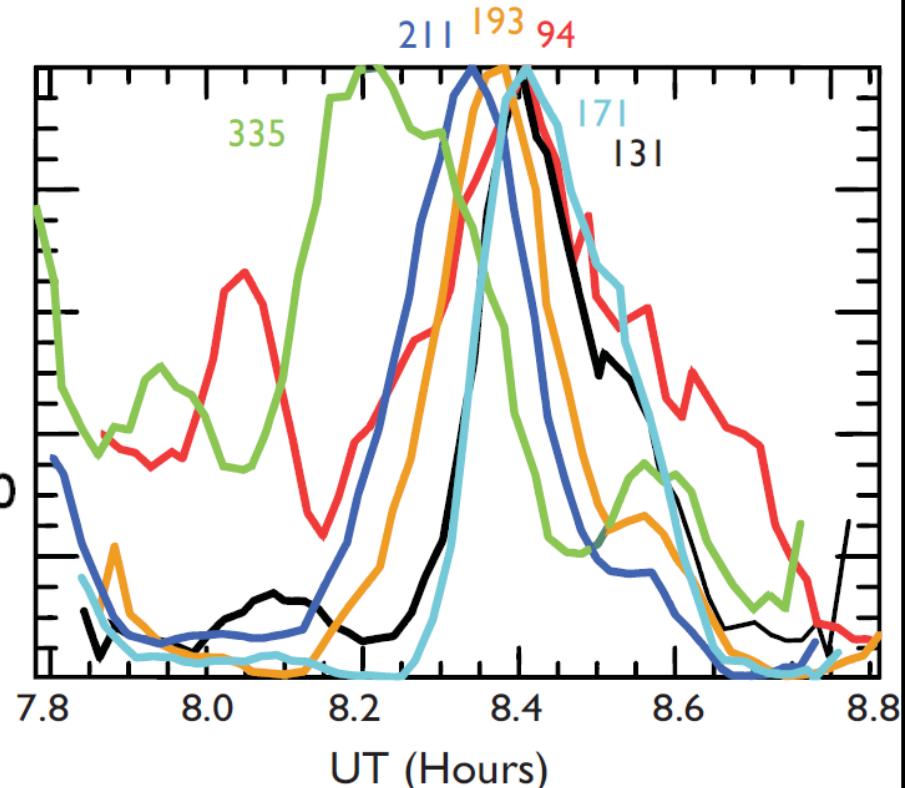
500 s Nanoflare Storm

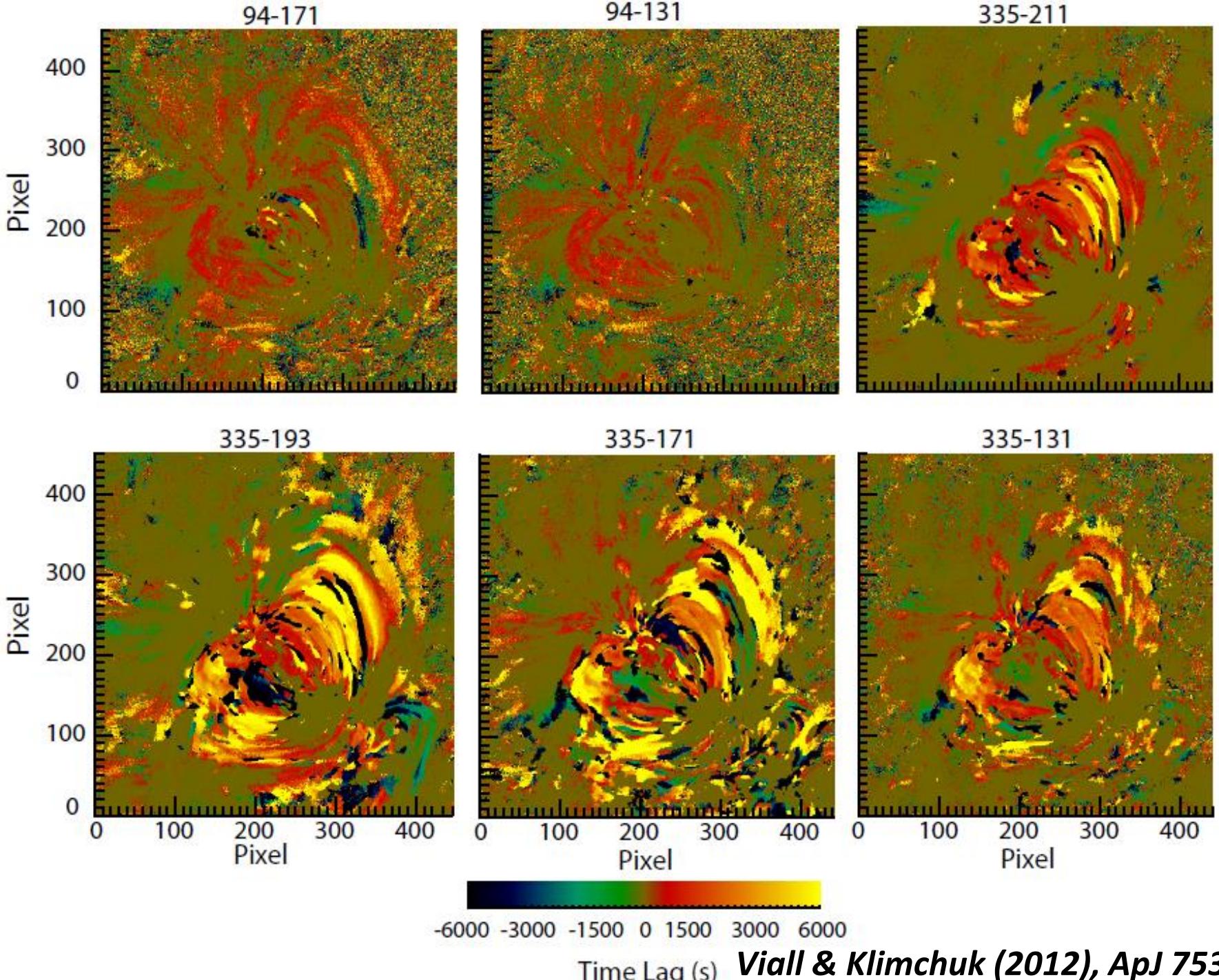


Theoretical light curves ^

Observed light curves >
for an AR core loop

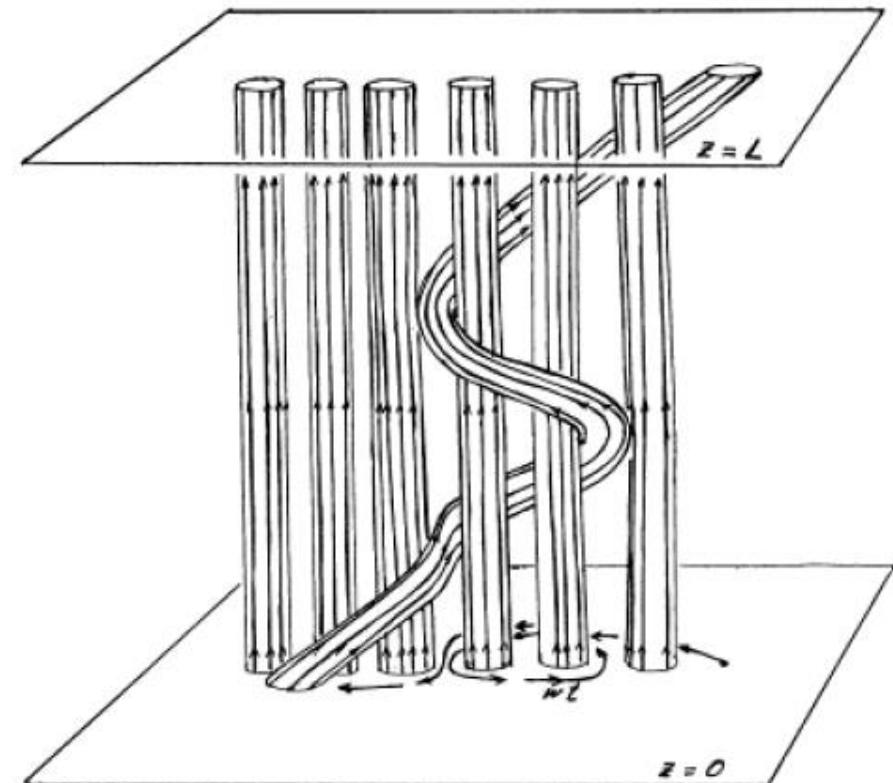
- Multi-strand loop
- One strand heated at a time, then next one is heated
- Short heating followed by cooling





Coronal Heating Problem

- The Corona is heated to temperatures of several MK. But how?
- Small-scale reconnection – Parker's nanoflares
- Wave heating – transfer of energy from waves to particles
- Note on terminology:
The current “nanoflare” models simply refer to **any impulsive energy release** (papers by the Klimchuk group),



i.e., not only reconnection, but also (any) bursty wave heating

Heat Flux Required

- Exponentially decreasing heating has heating flux of

$$F_H = E_{H0} S_H$$

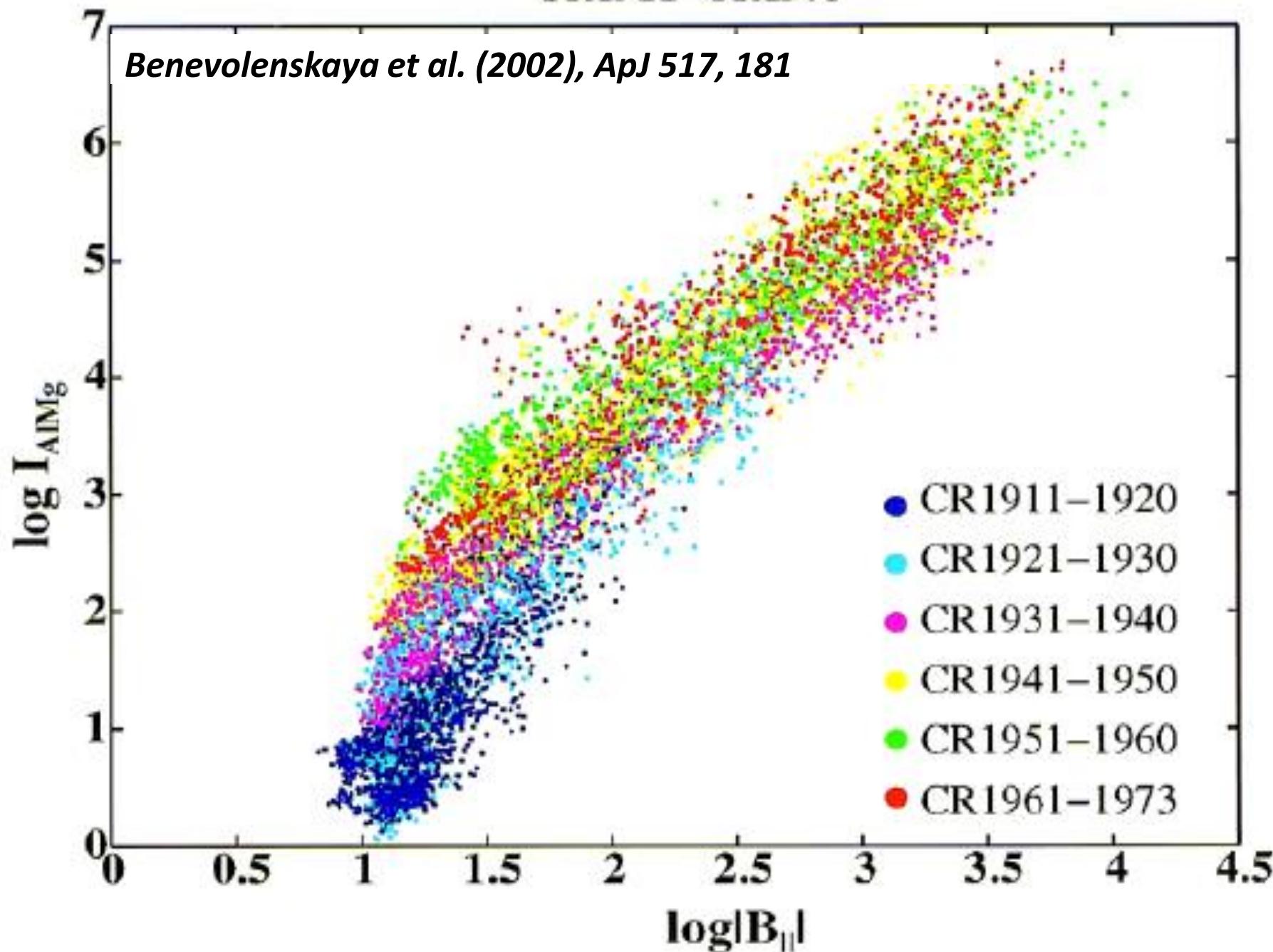
$$\approx 5 \times 10^3 \left(\frac{n_e}{10^8 \text{ cm}^{-3}} \right)^2 \left(\frac{T}{1 \text{ MK}} \right) \text{ [ergs cm}^{-2} \text{s}^{-1}\text{]}$$



$$E_{H0} \approx E_{rad} = n_e^2 Q(T)$$

- Simplest assumption: radiation losses balanced by heating flux
- **Coronal hole:** $T \approx 1 \text{ MK}$, $n_e \approx 10^8 \text{ cm}^{-3}$: $F_H \approx 5 \times 10^3 \text{ ergs cm}^{-2} \text{ s}^{-1}$
- **Active region:** $T \approx 2.5 \text{ MK}$, $n_e \approx 2 \times 10^9 \text{ cm}^{-3}$: $F_H \approx 5 \times 10^6 \text{ ergs cm}^{-2} \text{ s}^{-1}$

CR1911–CR1973



Statement of the Problem: MHD

$$\rho \left(\frac{\partial \vec{v}}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \vec{v} \right) = -\vec{\nabla} p_{\text{G}} + \vec{j} \times \vec{B} + \rho \vec{g},$$

$$\frac{1}{\gamma - 1} \left(\frac{\partial T}{\partial t} + \vec{v} \cdot \vec{\nabla} T \right) = -T \vec{\nabla} \cdot \vec{v} + \frac{1}{q k_{\text{B}} n_{\text{e}}} (E_{\text{H}} - n_{\text{e}}^2 Q(T) + \vec{\nabla} \cdot \vec{F}_{\text{C}}),$$

$$\frac{\partial \vec{B}}{\partial t} = \vec{\nabla} \times (\vec{v} \times \vec{B}),$$

$$\frac{\partial \rho}{\partial t} + \vec{\nabla} \cdot (\rho \vec{v}) = 0,$$

$$\vec{j} = \frac{1}{\mu} \vec{\nabla} \times \vec{B},$$

$$\vec{\nabla} \cdot \vec{B} = 0,$$

$$p = q n_{\text{e}} k_{\text{B}} T = \frac{\rho k_{\text{B}} T}{\bar{\mu} m_{\text{H}}},$$

$$F_{\text{C},\parallel} = \kappa_0 T^{5/2} \frac{dT}{ds}, \quad F_{\text{C},\perp} = 0.$$

Scaling Laws: Simple Solutions

Assumptions:

- No time derivatives
- No flows
- Geometrically symmetric loop with symmetric heating
- Vanishing thermal conductivity at loop apex and footpoints

$$p_0(L_0, s_H, T_1) = L_0^{-1} T_1^3 S_1^{-3},$$

$$E_{H0}(L_0, s_H, T_1) = L_0^{-2} T_1^{7/2} S_2,$$

$$S_1^{\text{RTV}} = 1,4 \times 10^2 \quad [\text{K s}^{2/3} \text{kg}^{-1/3}],$$

$$S_2^{\text{RTV}} = 9,5 \times 10^{-6} \quad [\text{kg m s}^{-3} \text{K}^{-7/2}].$$

$$S_1^{\text{Serio}} = 1.4 \times 10^2 \ e^{-\left(0,08L_0/s_H + 0,04L_0/s_p\right)},$$

$$S_2^{\text{Serio}} = 9,5 \times 10^{-6} \ e^{\left(0,78L_0/s_H - 0,36L_0/s_p\right)}.$$

Rosner, Tucker, Vaiana (1978)

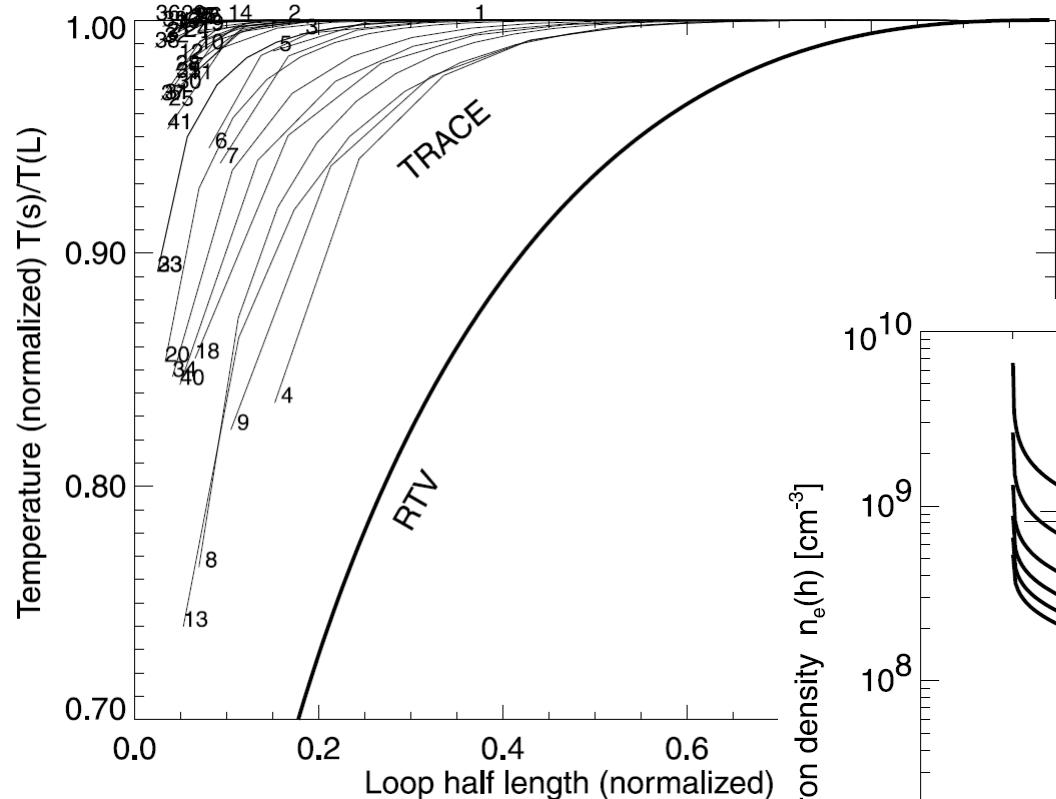
Serio et al. (1981)

Aschwanden & Schrijver (2002)

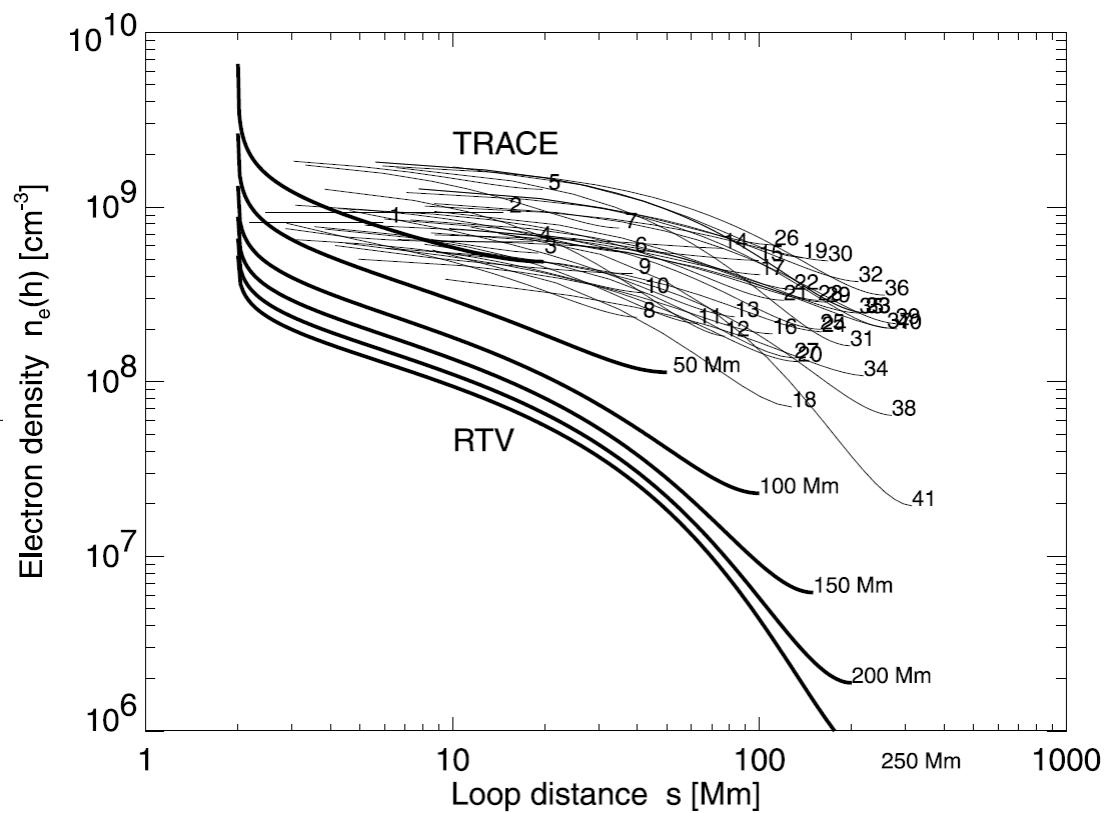
Dudík et al. (2009)

Martens (2010)

Comparison to Observations



*Aschwanden et al. (2000),
ApJ 541, 1059*



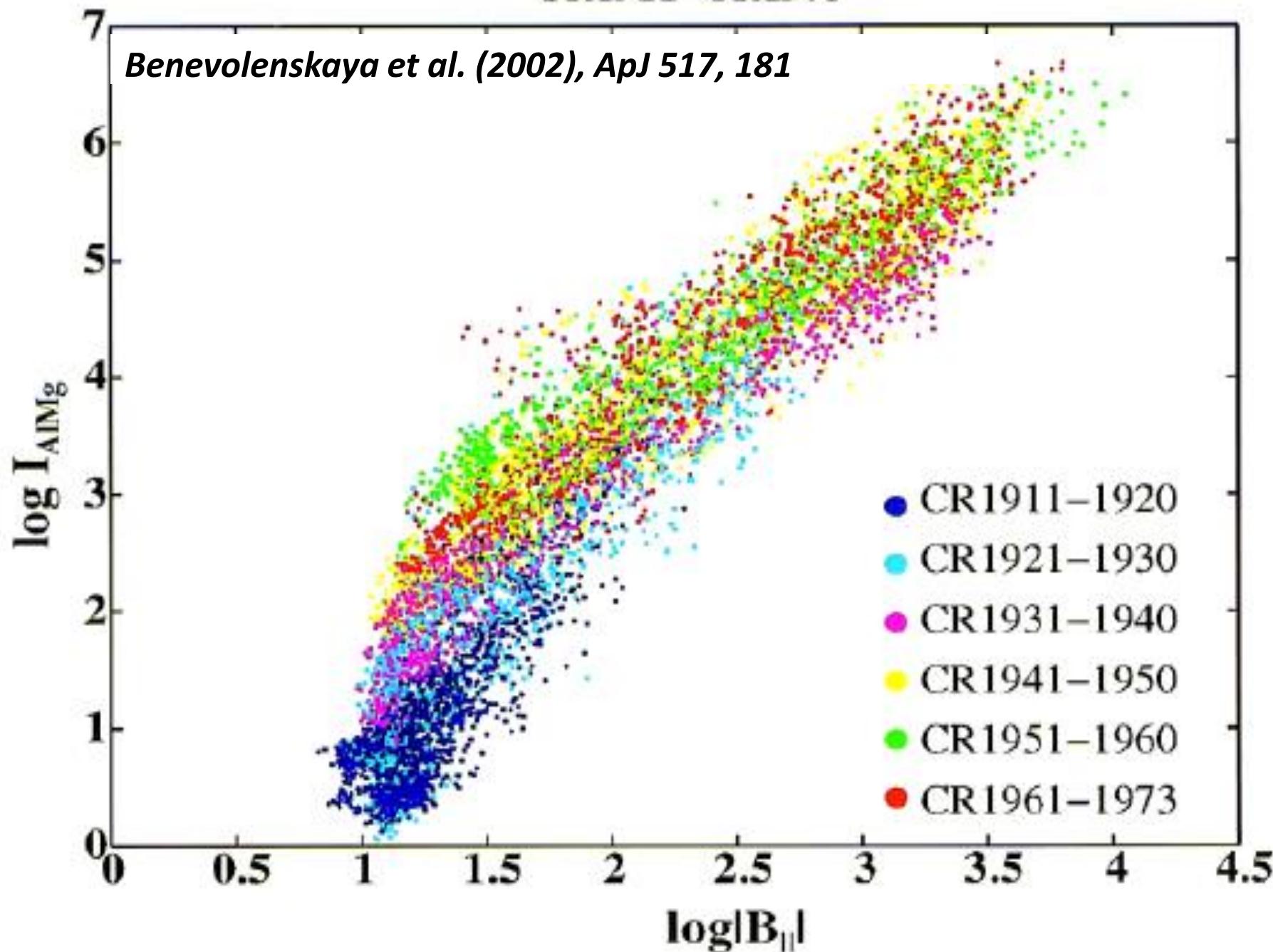
Proposed Heating Models

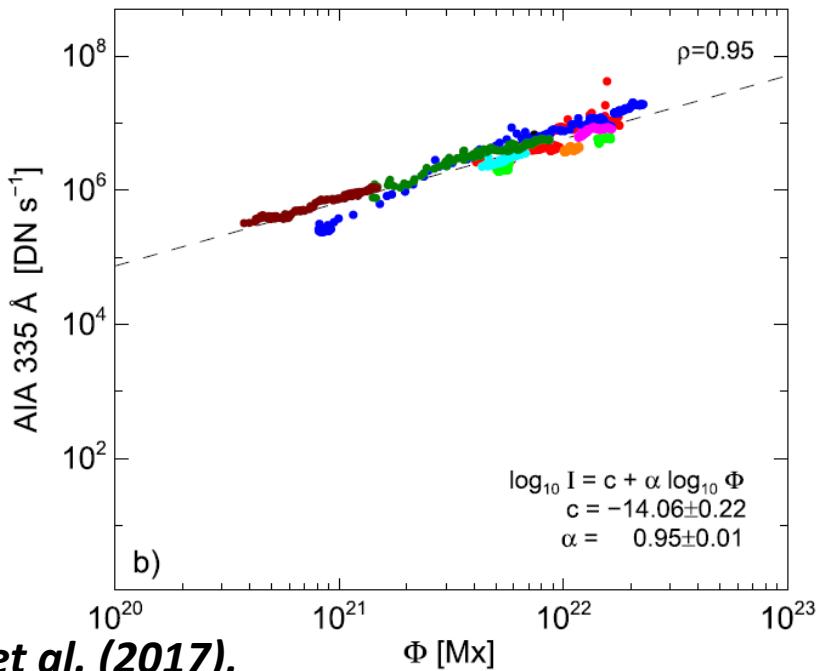
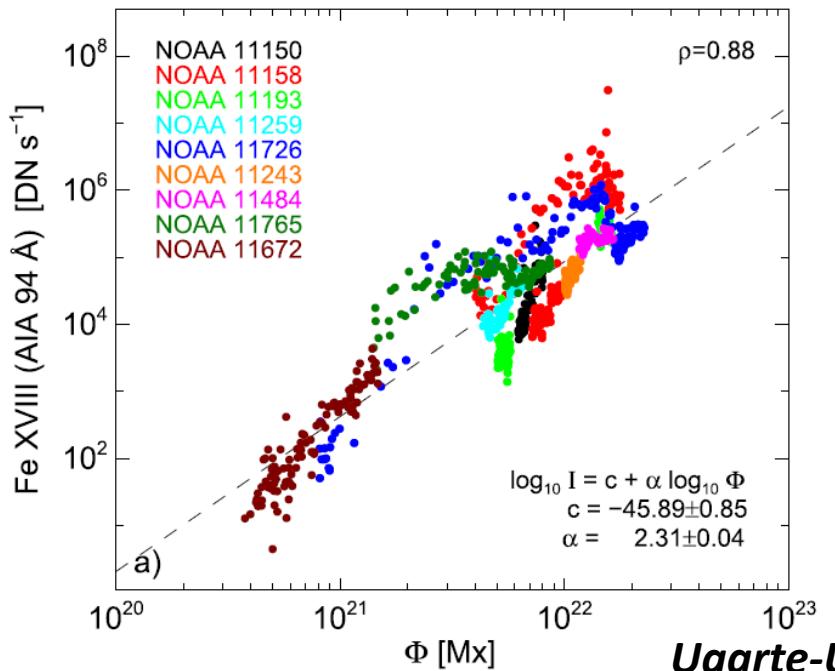
Lundquist et al. 2008, ApJ 689, 1388

TABLE 1
HEATING SCALE RELATIONSHIPS

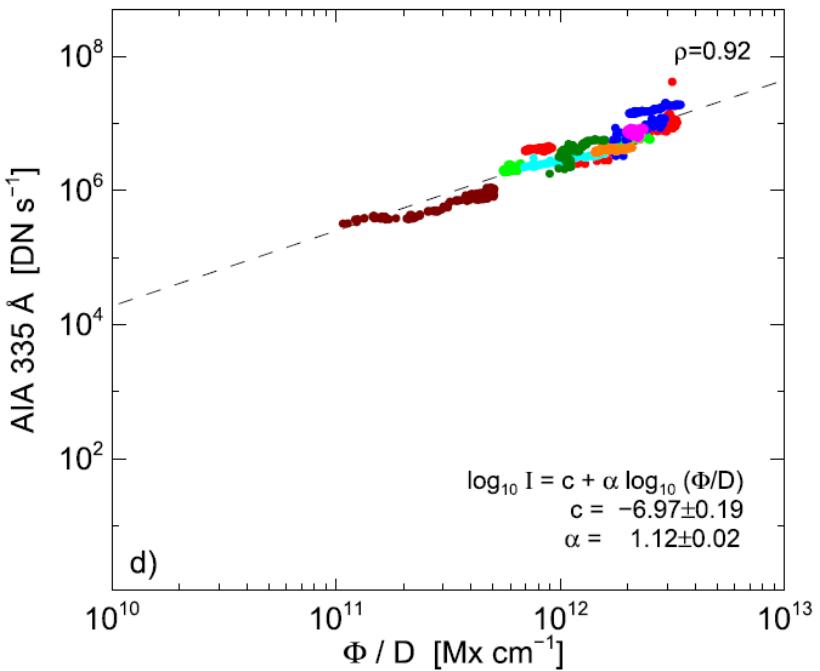
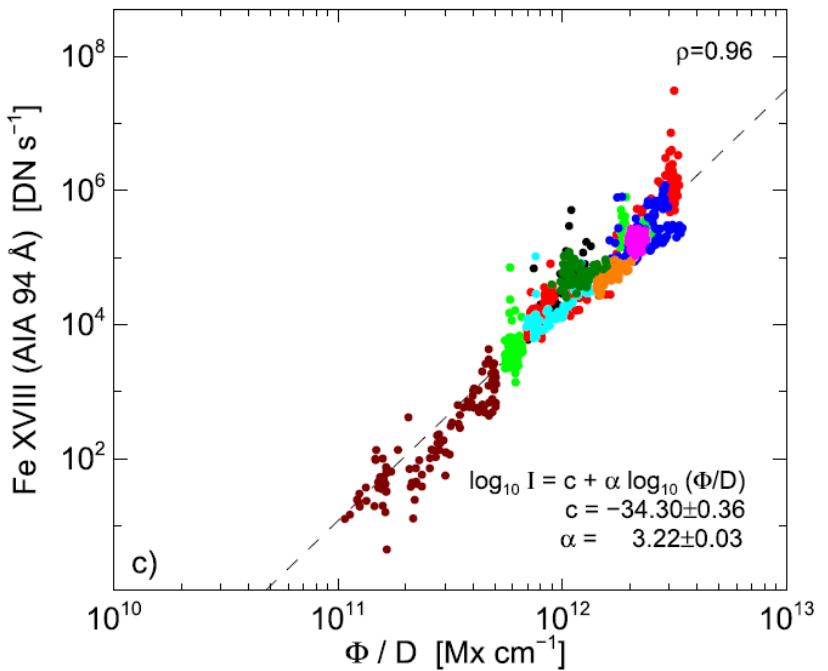
Description	Number	Reference	MDK Scaling	B Case a	B Case b	B Case c	L
Stochastic buildup.....	1	1	$B^2 L^{-2} V^2 \tau$	B^2	B^1	B^2	L^{-2}
Critical angle.....	2	2	$B^2 L^{-1} V^1 \tan \theta$	B^2	$B^{1.5}$	B^2	L^{-1}
Critical twist.....	3	3	$B^2 L^{-2} V^1 R^1 \phi$	B^2	B^1	...	L^{-2}
Reconnection $\propto v_A$	4	4	$B^1 L^{-2} \rho^{0.5} V^2 R^1$	B^1	...	$B^{0.5}$	$L^{-2.45}$
Reconnection $\propto v_{A\perp}$	5	5	$B^{1.5} L^{-1.5} \rho^{0.25} V^{1.5} R^{1.5}$	$B^{1.5}$...	$B^{0.75}$	$L^{-1.725}$
Current layers (DC).....	6	6	$B^2 L^{-2} V^2 \tau \log R_m$	B^2	L^{-2}
	7	7	$B^2 L^{-2} V^2 S^{0.1} \tau$	B^2	L^{-2}
	8	8	$B^2 L^{-2} V^2 \tau$	B^2	L^{-2}
Current sheets	9	9	$B^2 L^{-1} R^{-1} V_{ph}^2 \tau$	B^2	...	$B^{2.5}$	L^{-1}
Taylor relaxation	10	10	$B^2 L^{-2} V_{ph}^2 \tau$	B^2	L^{-2}
Turbulence (DC) with:							
Constant dissipation coefficients.....	11	11	$B^{1.5} L^{-1.5} \rho^{0.25} V^{1.5} R^{1.5}$	$B^{1.5}$...	$B^{0.75}$	$L^{-1.725}$
Closure	12	12	$B^{1.67} L^{-1.33} \rho^{0.17} V^{1.33} R^{0.33}$	$B^{1.67}$...	$B^{1.505}$	$L^{-1.483}$
Closure + spectrum ($s = 0.7$).....	13	13	$B^{1.7} L^{-1.7} \rho^{0.15} V^{1.3} R^{0.7}$	$B^{1.7}$...	$B^{1.35}$	$L^{-1.835}$
Closure + spectrum ($s = 1.1$).....	14	13	$B^{2.1} L^{-2.1} \rho^{-0.05} V^{0.9} R^{1.1}$	$B^{2.1}$...	$B^{1.55}$	$L^{-2.055}$
Resonance ($m = -1$).....	15	14	$B^0 L^{-2}$	B^0	L^{-2}
Resonance ($m = -2$).....	16	14	$B^{-1} L^{-1} \rho^{0.5}$	B^{-1}	$L^{-1.45}$
Resonant absorption I ($m = -1$).....	17	15	$B^0 L^0$	B^0	L^0
Resonant absorption I ($m = -2$).....	18	15	$B^{-1} L^1 \rho^{0.5}$	B^{-1}	$L^{0.55}$
Resonant absorption II ($m = -1$).....	19	16	$B^0 L^1 \rho^1$	B^0	$L^{0.1}$
Resonant absorption II ($m = -2$).....	20	16	$B^{-1} L^2 \rho^{1.5}$	B^{-1}	$L^{0.65}$
Current layers (AC)	21	17	$B^1 L^{-1} \rho^{0.5} V^2$	B^1	$L^{-1.45}$
Turbulence (AC)	22	18	$B^{1.67} L^{-1.33} R^{0.33}$	$B^{1.67}$...	$B^{1.505}$	$L^{-1.33}$

CR1911–CR1973



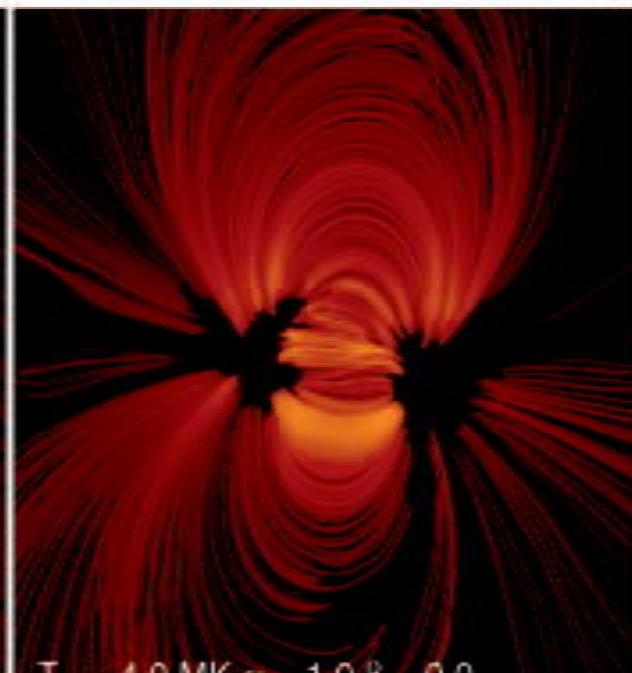


*Ugarte-Urra et al. (2017),
ApJ 846, 165*

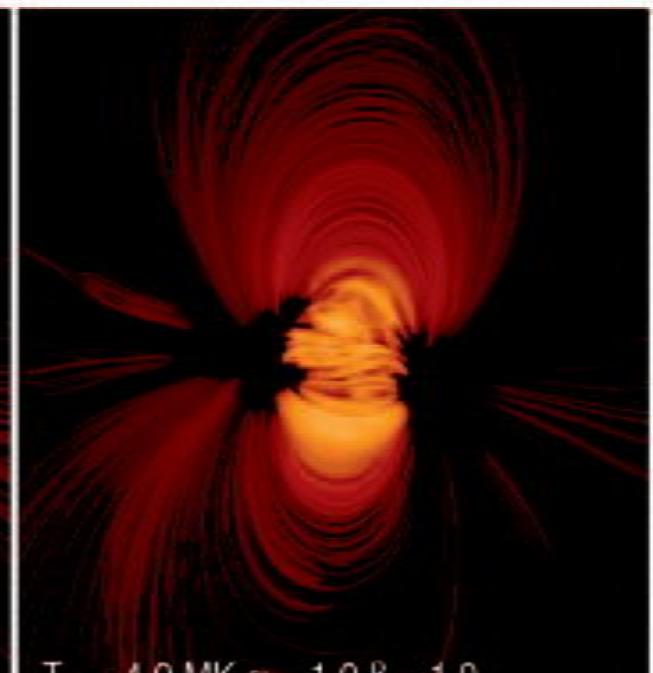




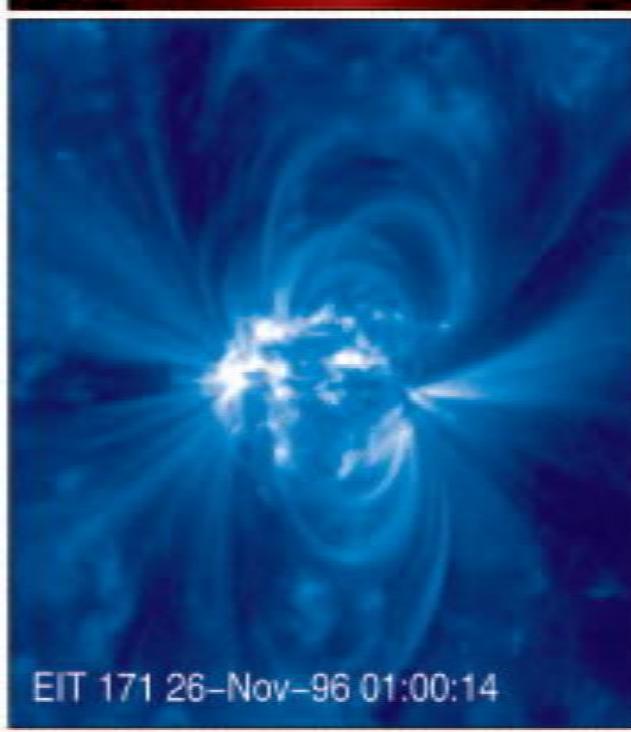
SXT Open/AlMg 26-Nov-96 05:21:52



$T_0 = 4.0 \text{ MK} \alpha = 1.0 \beta = 0.0$



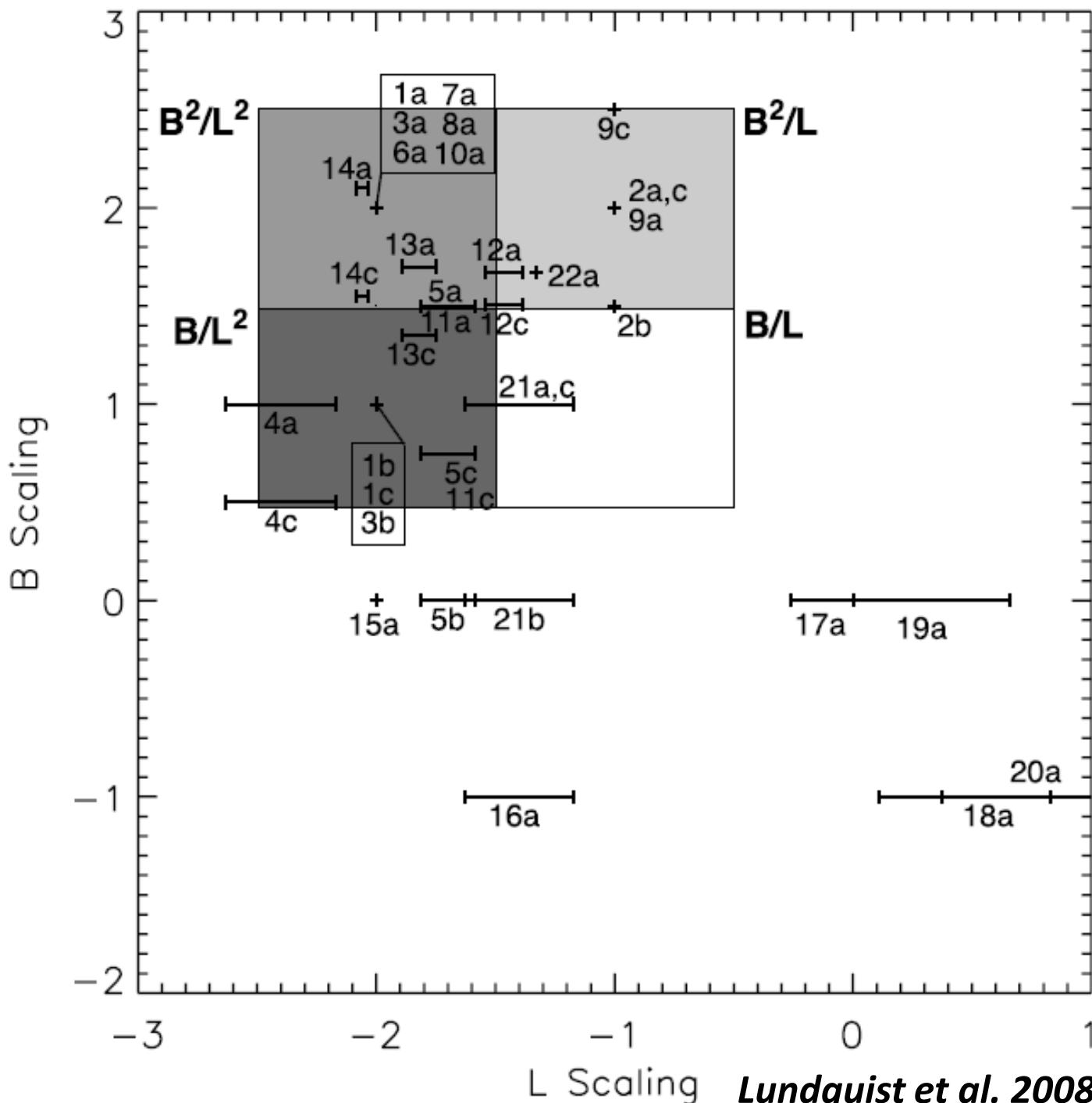
$T_0 = 4.0 \text{ MK} \alpha = 1.0 \beta = 1.0$

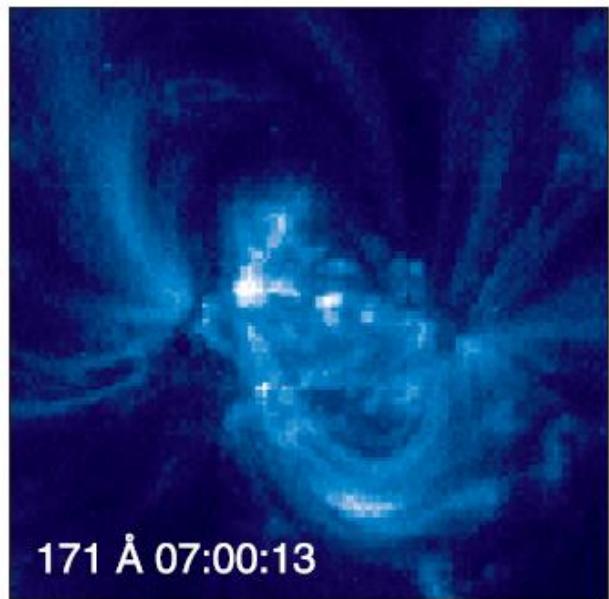


EIT 171 26-Nov-96 01:00:14

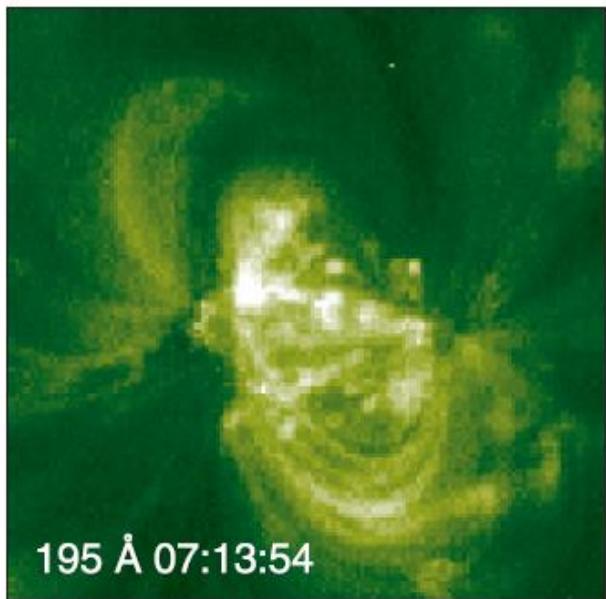
$$E_H = C_H \left(\frac{B}{B_{ref}} \right)^\alpha \left(\frac{L_{ref}}{L} \right)^\beta$$

*Warren & Winebarger (2007)
ApJ. 666, 1245*

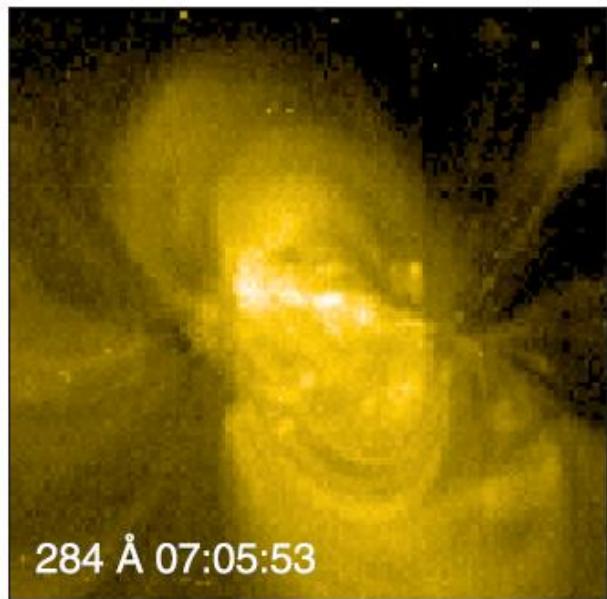




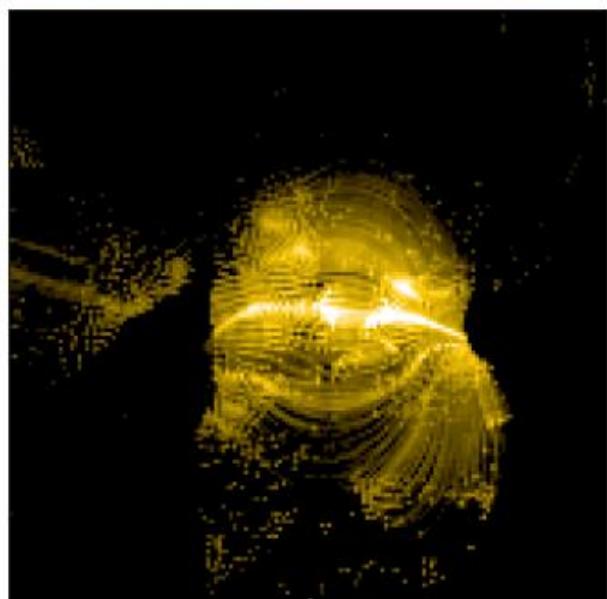
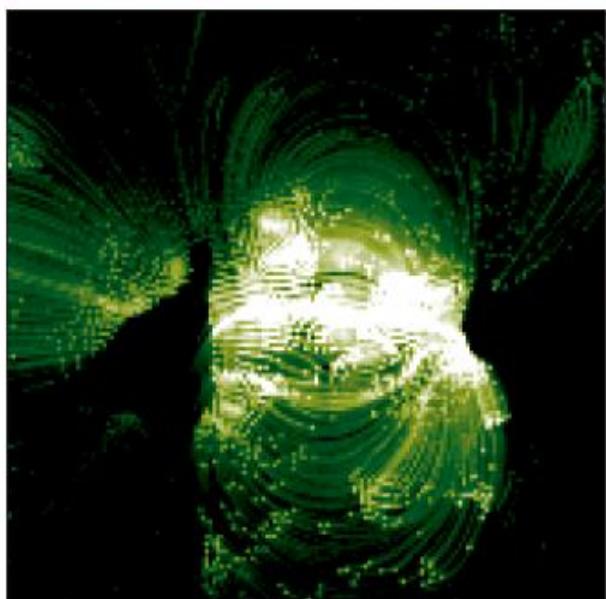
171 Å 07:00:13

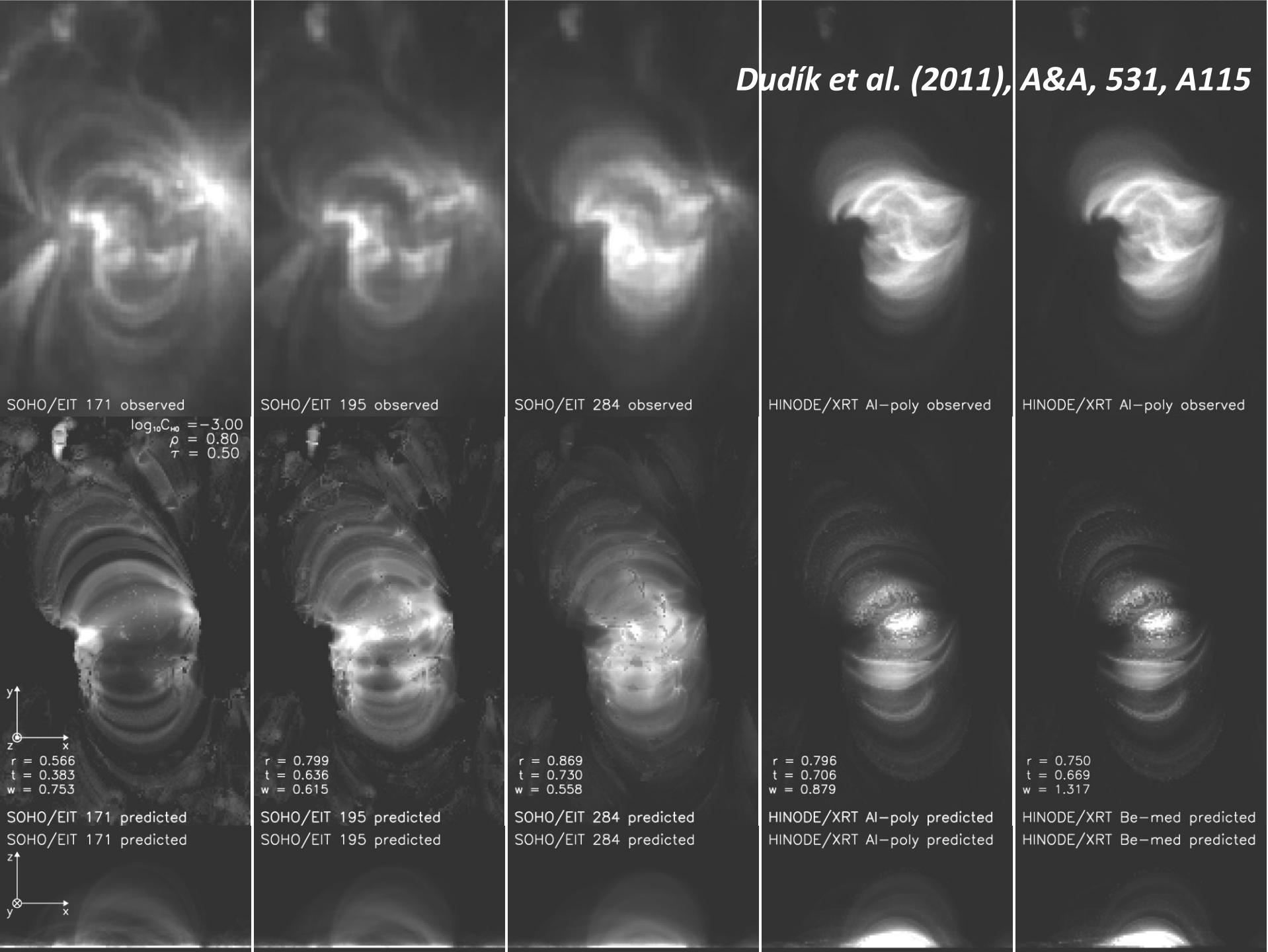


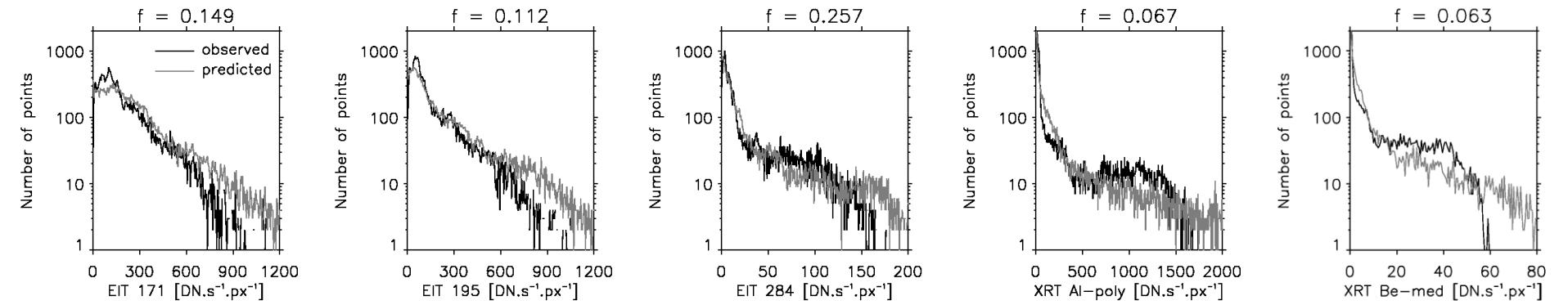
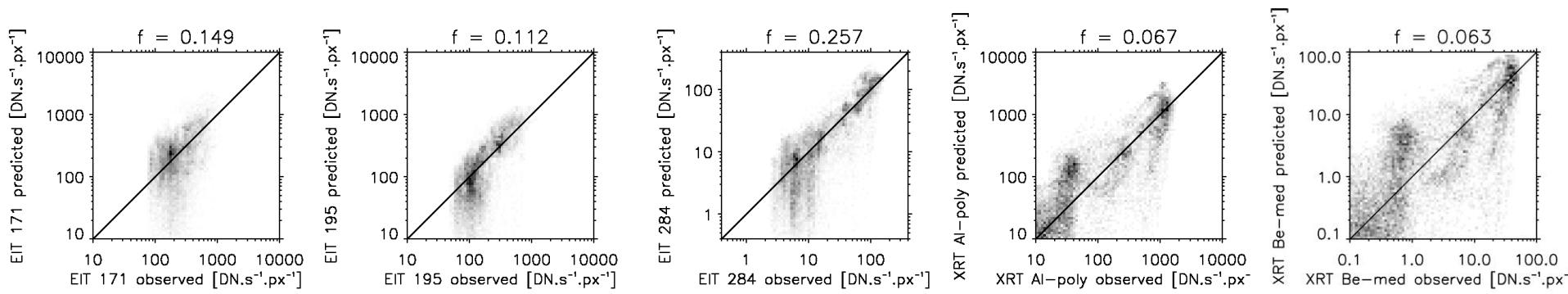
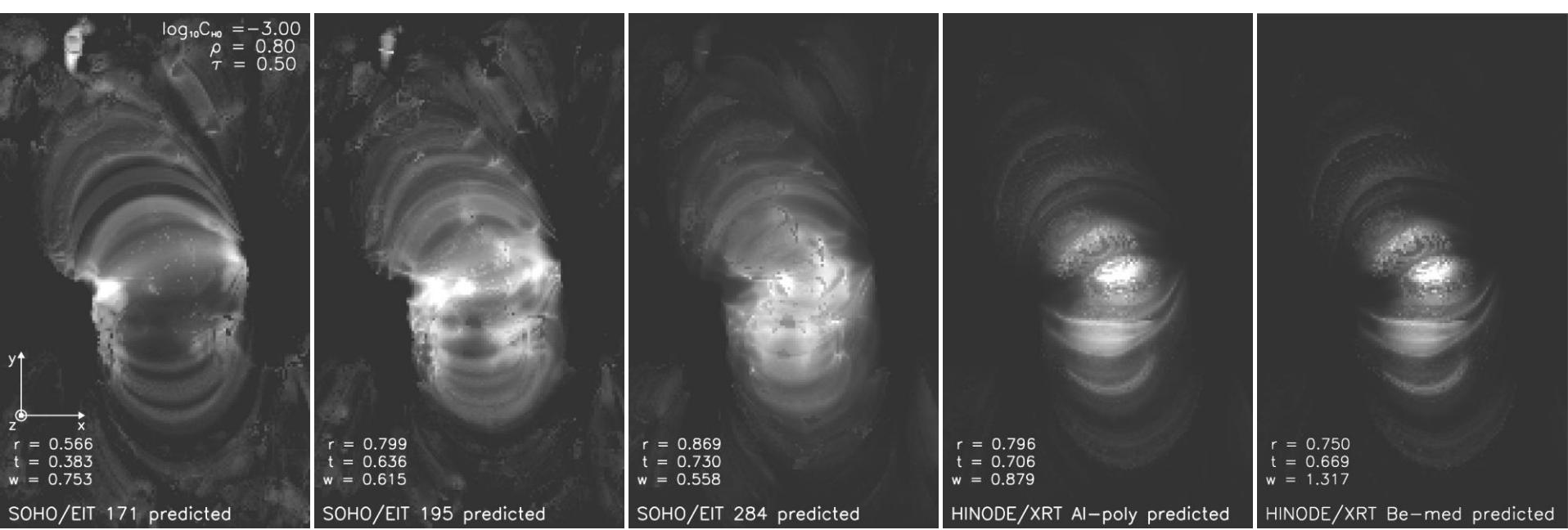
195 Å 07:13:54

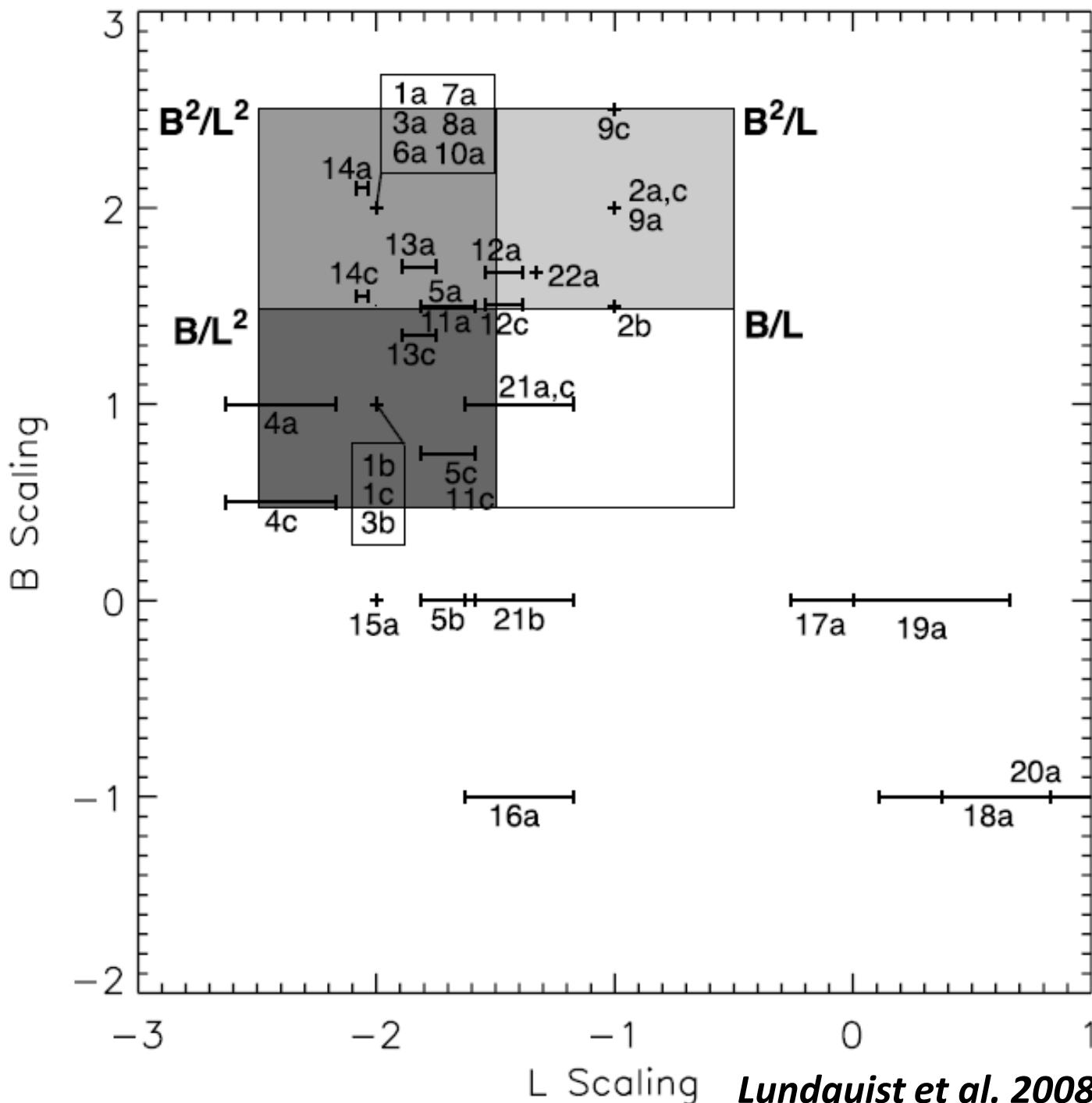


284 Å 07:05:53



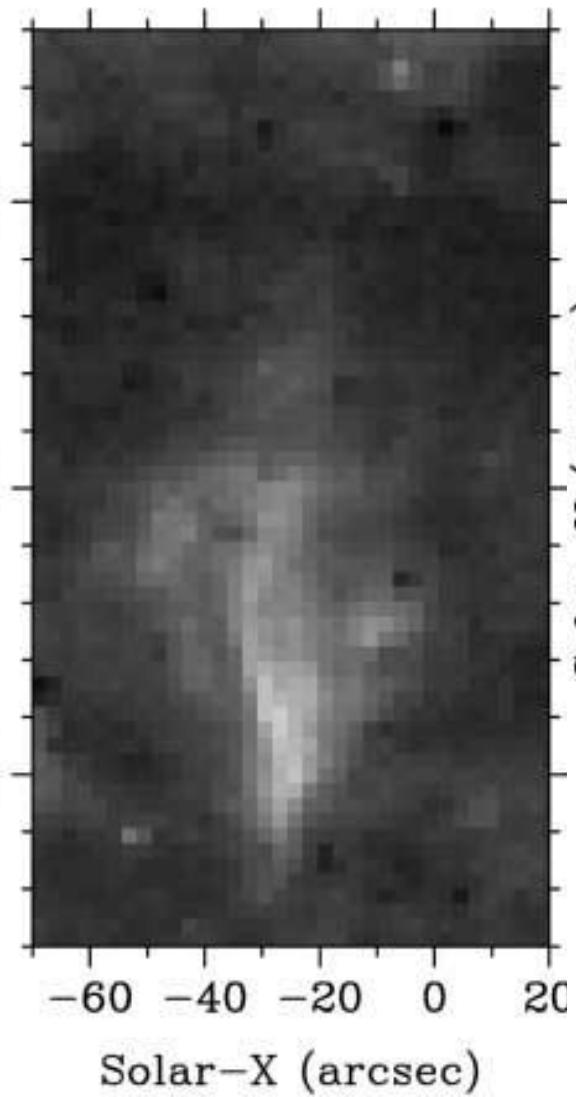




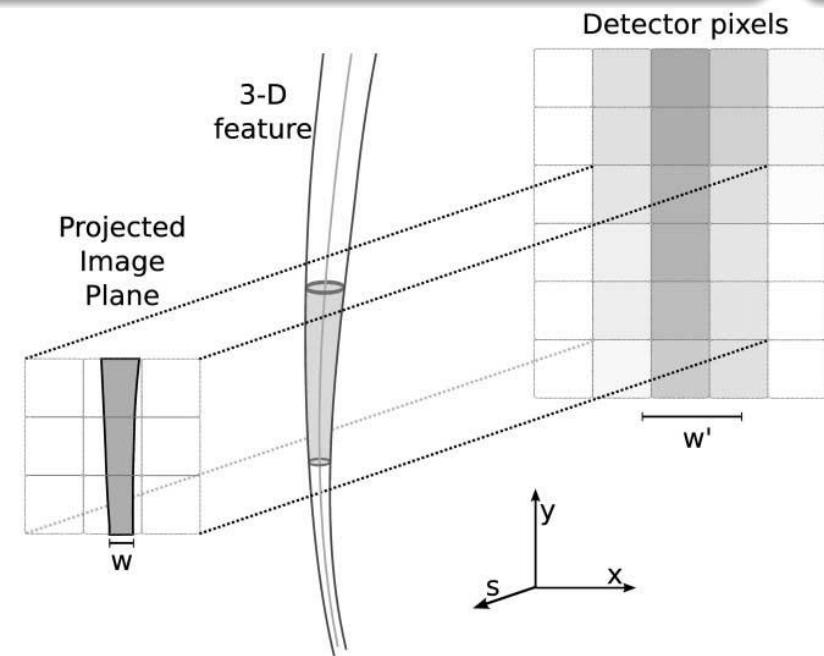
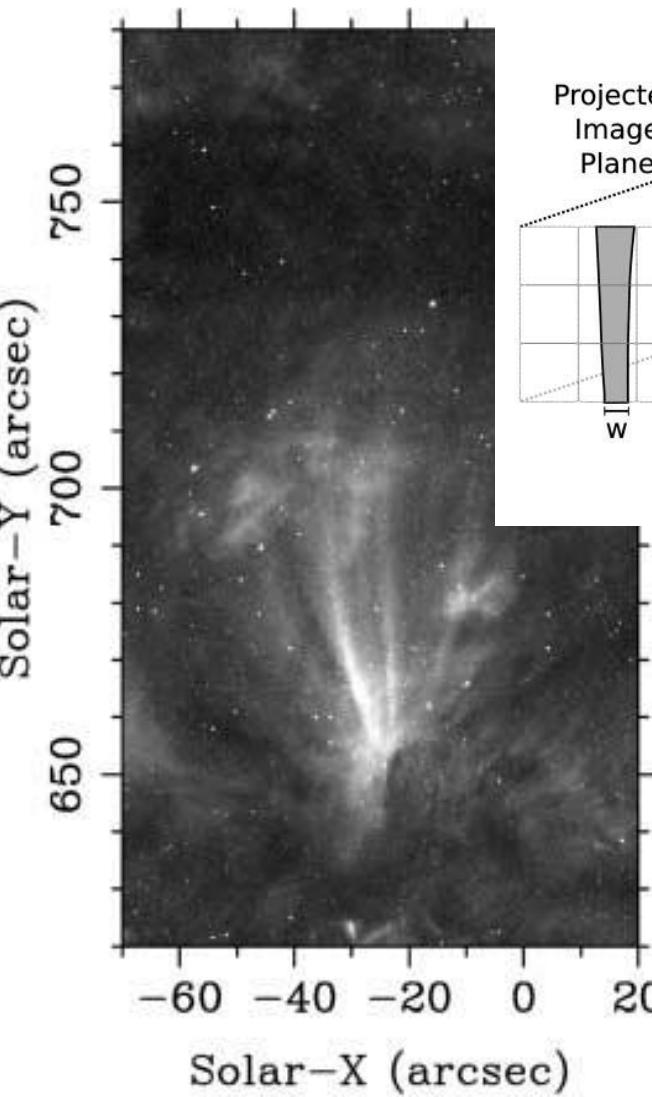


Do We Understand the Geometry?

EIT 171 A



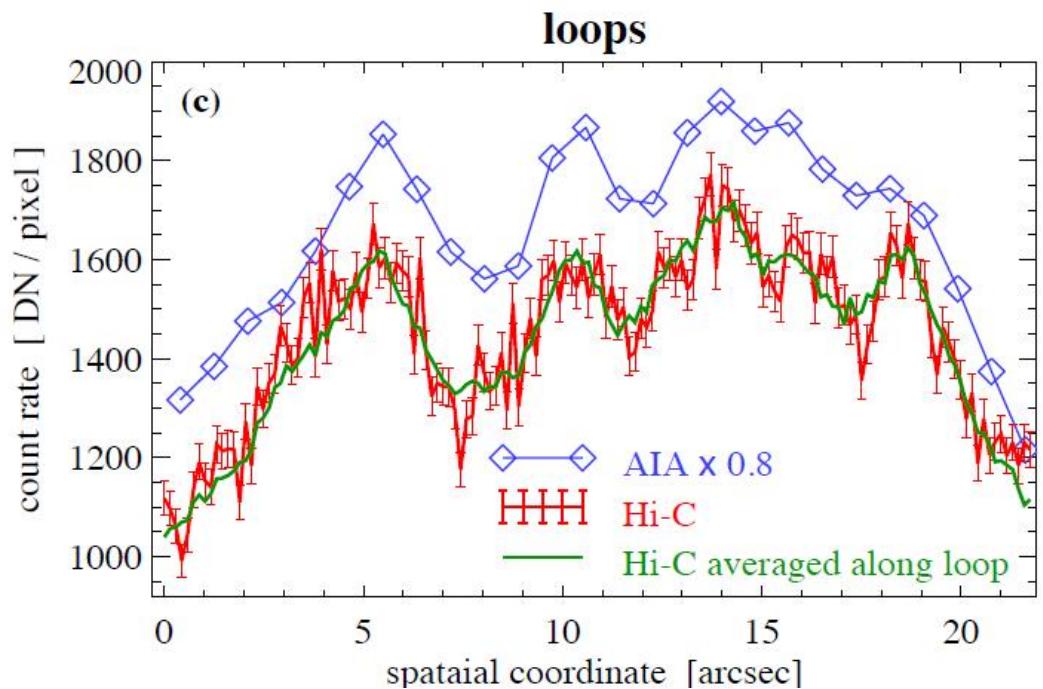
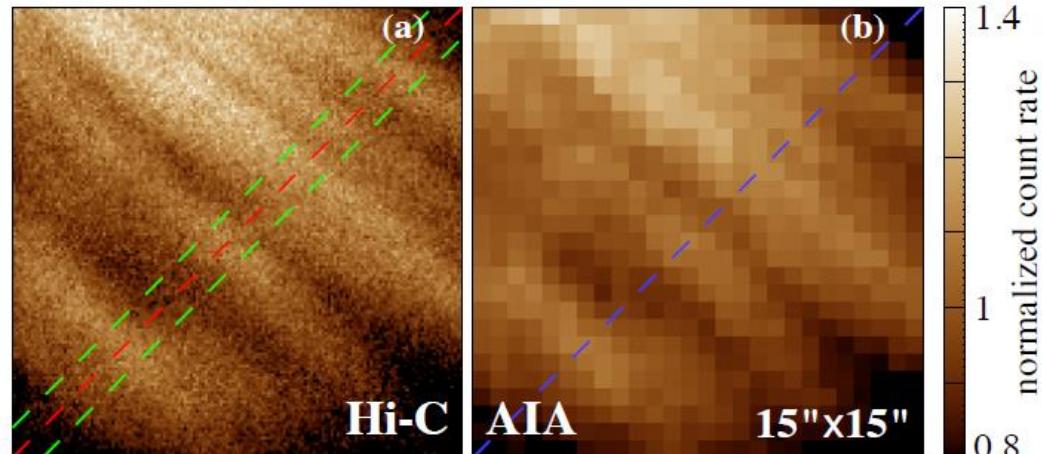
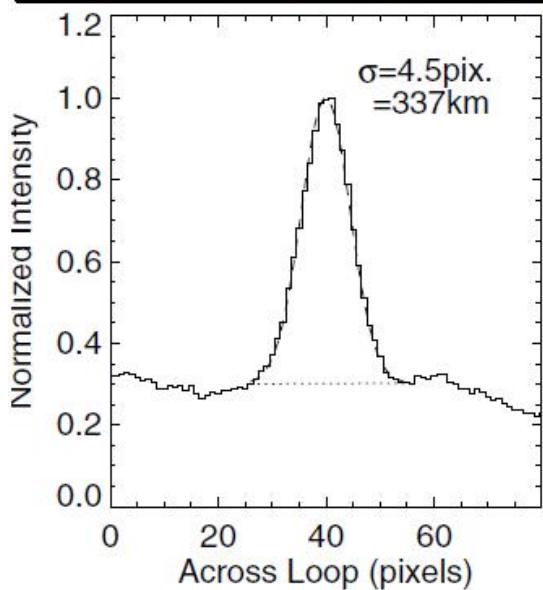
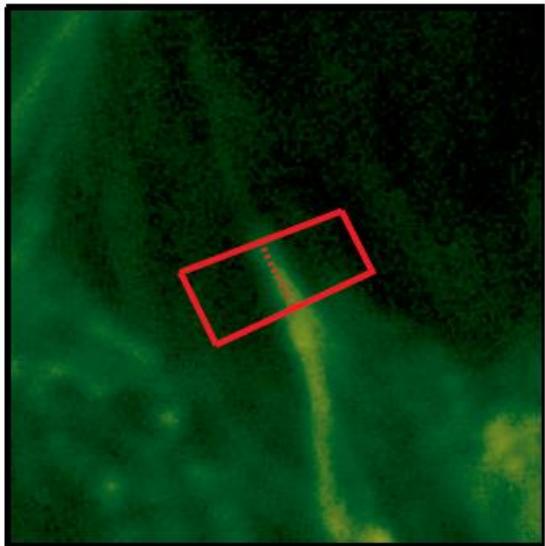
TRACE 171



*DeForest (2007),
ApJ 661, 532:*

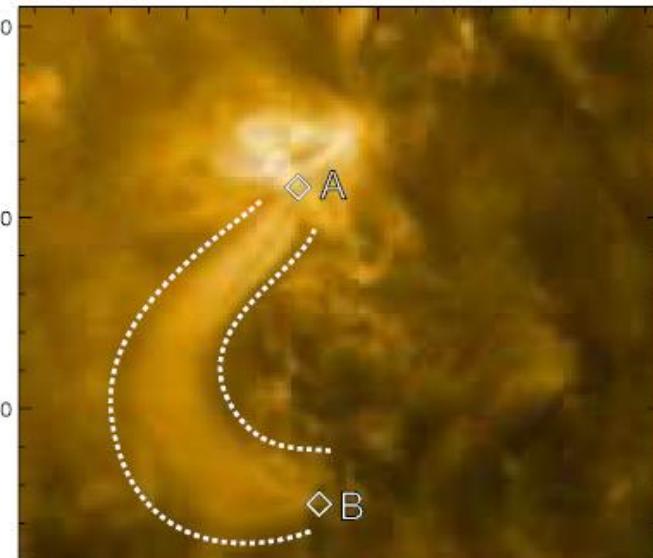
Poorly resolved
expanding structures
**may appear to be
non-expanding**

But some loops are resolved...

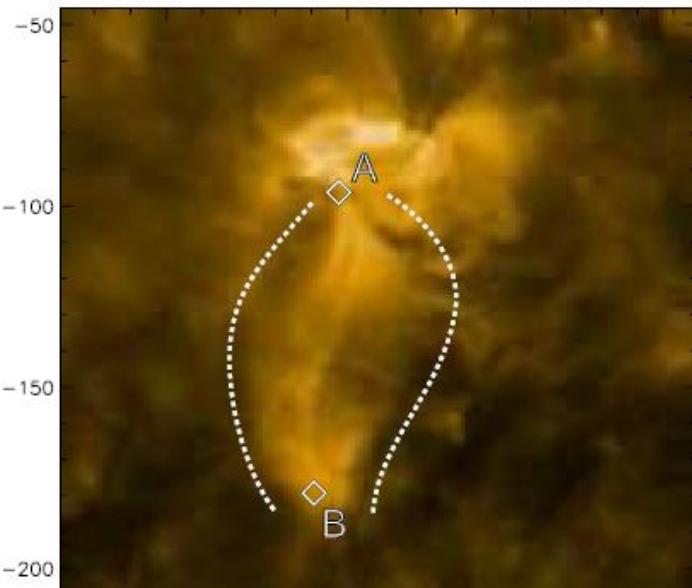


Geometry... Part 2

STEREO A 171A | 2008-01-10T05:06:00.017

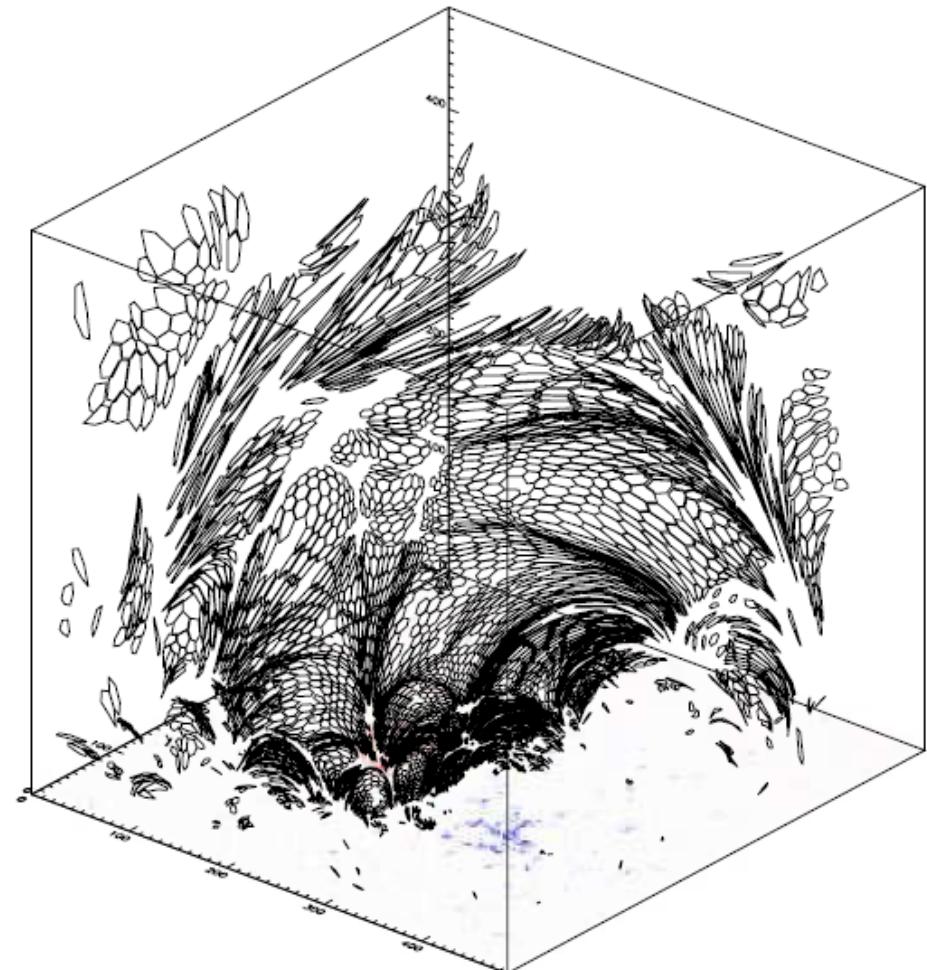


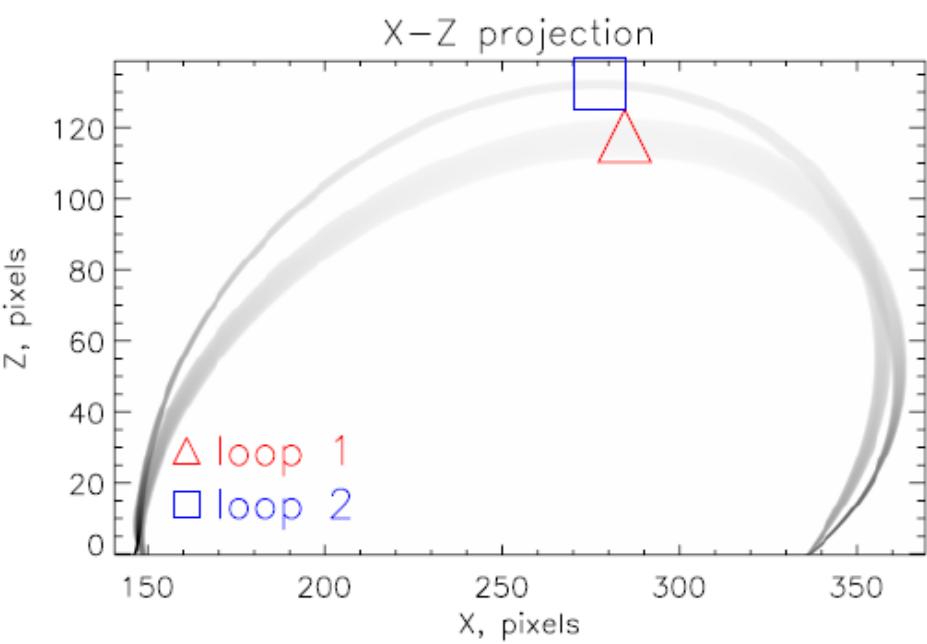
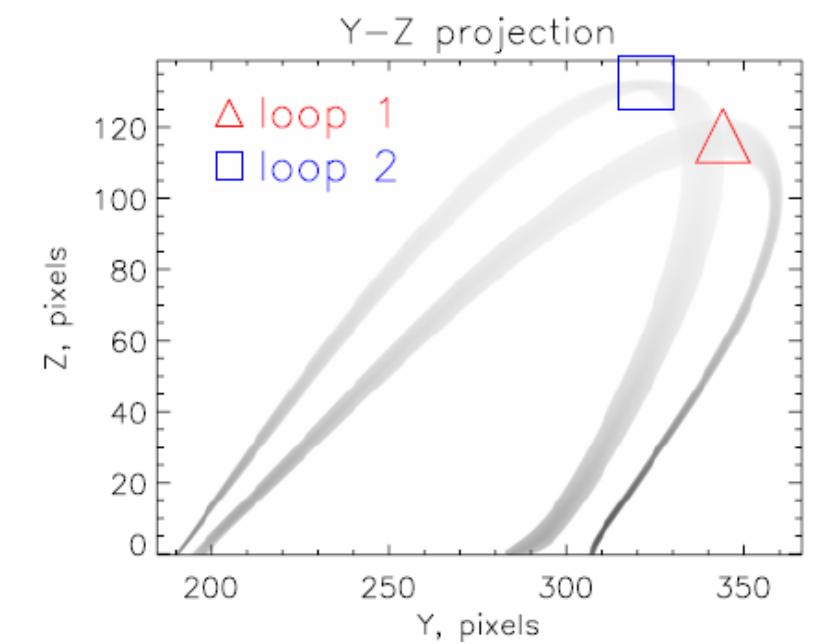
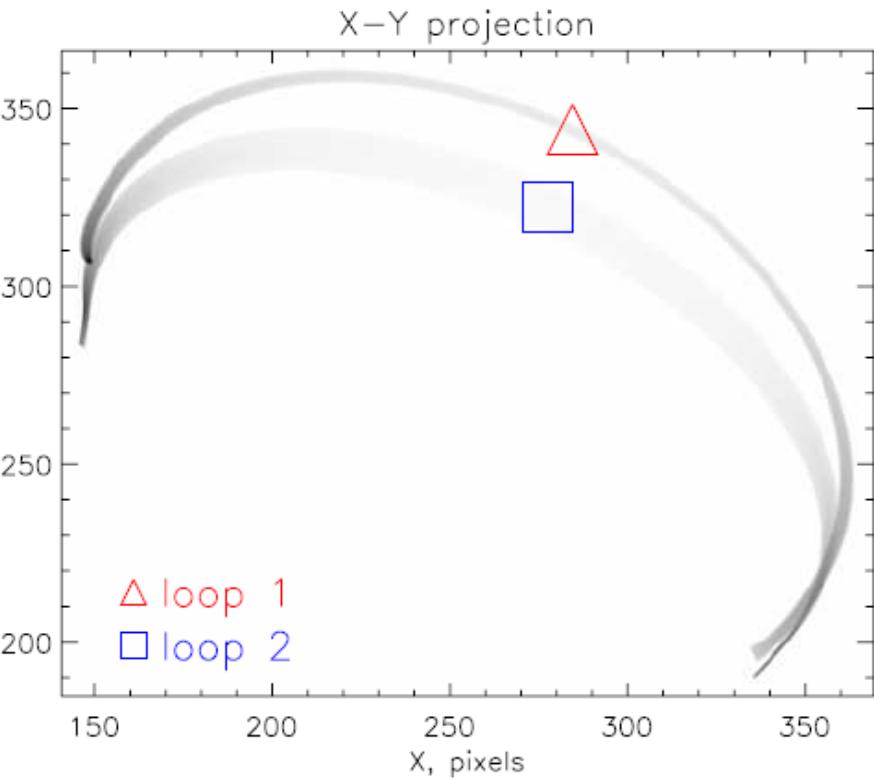
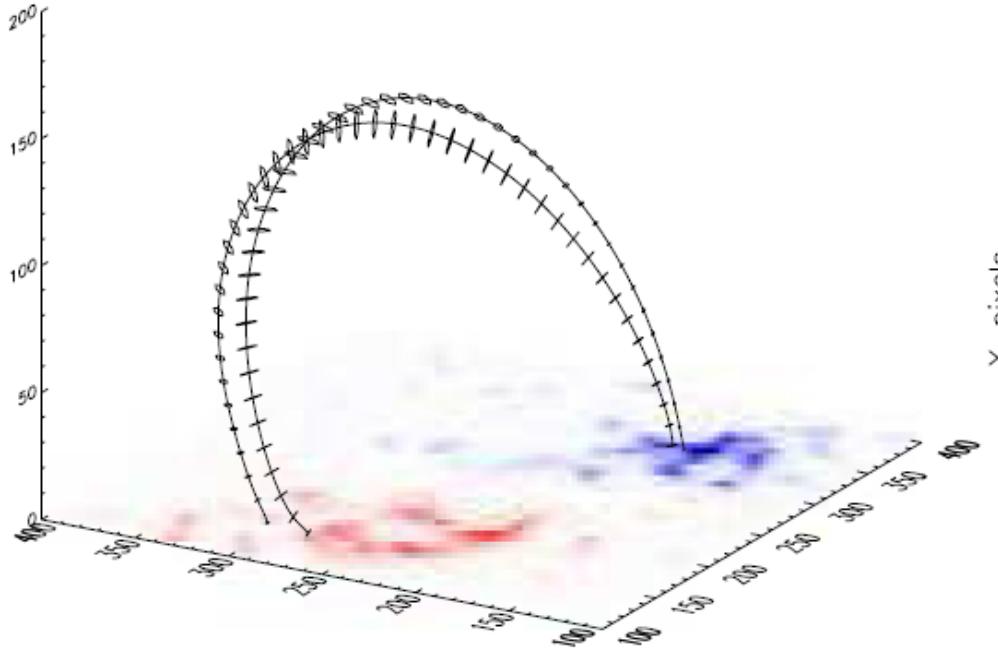
STEREO B 171A | 2008-01-10T05:06:20.158



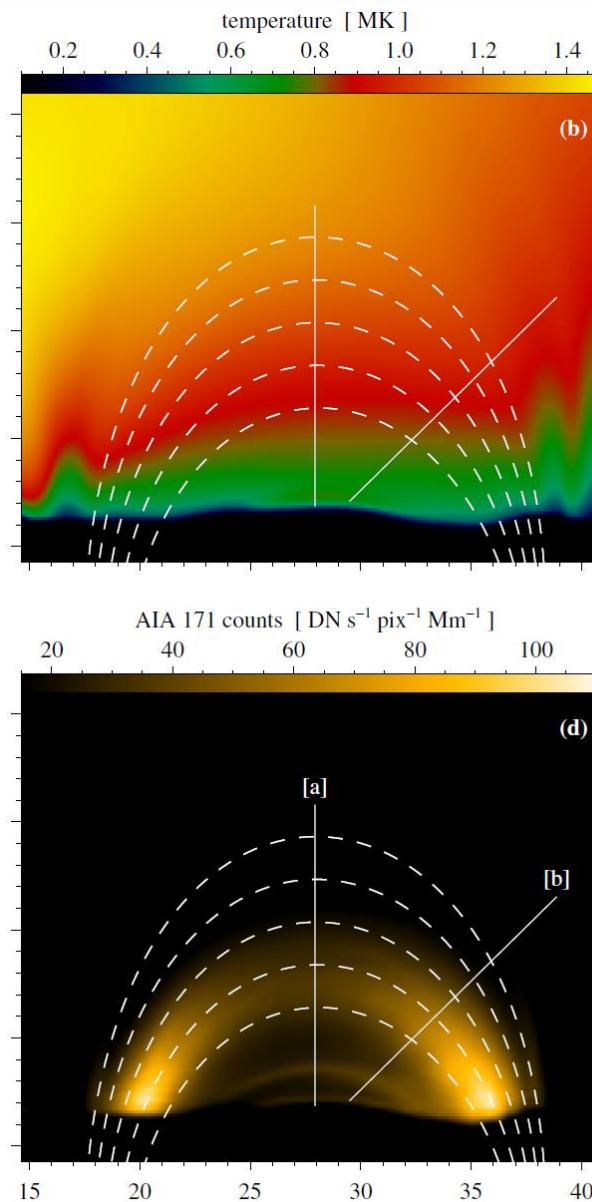
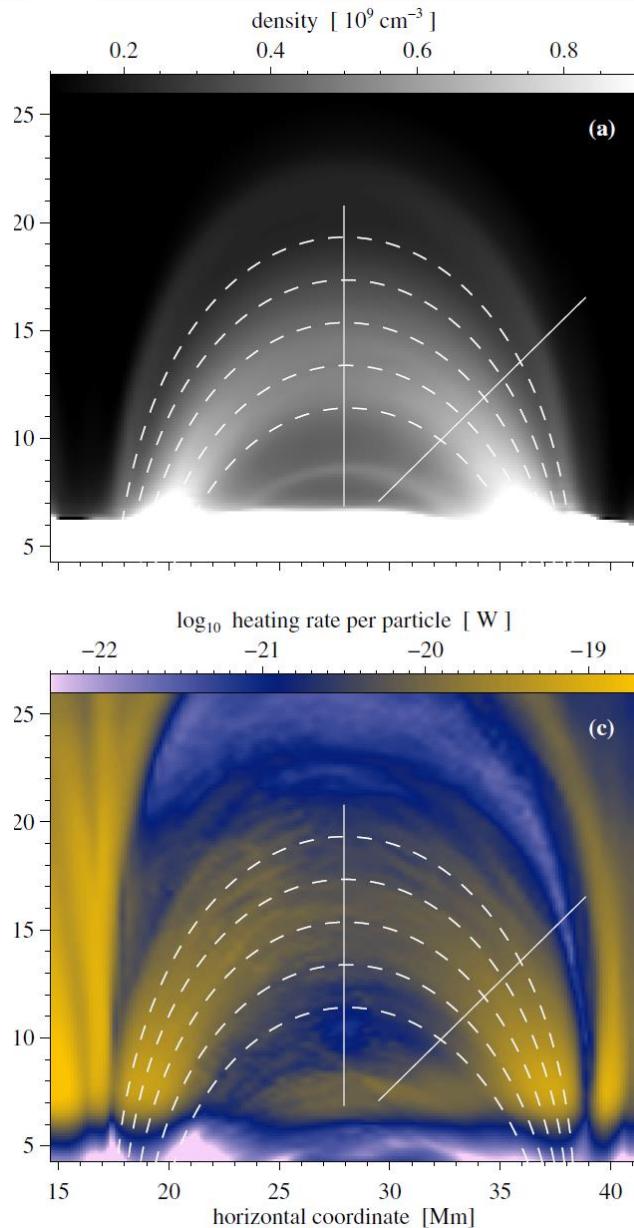
Malanushenko & Schrijver (2013), ApJ 775, 120

- No circular cross-sections
- Introduces bias in loop selection





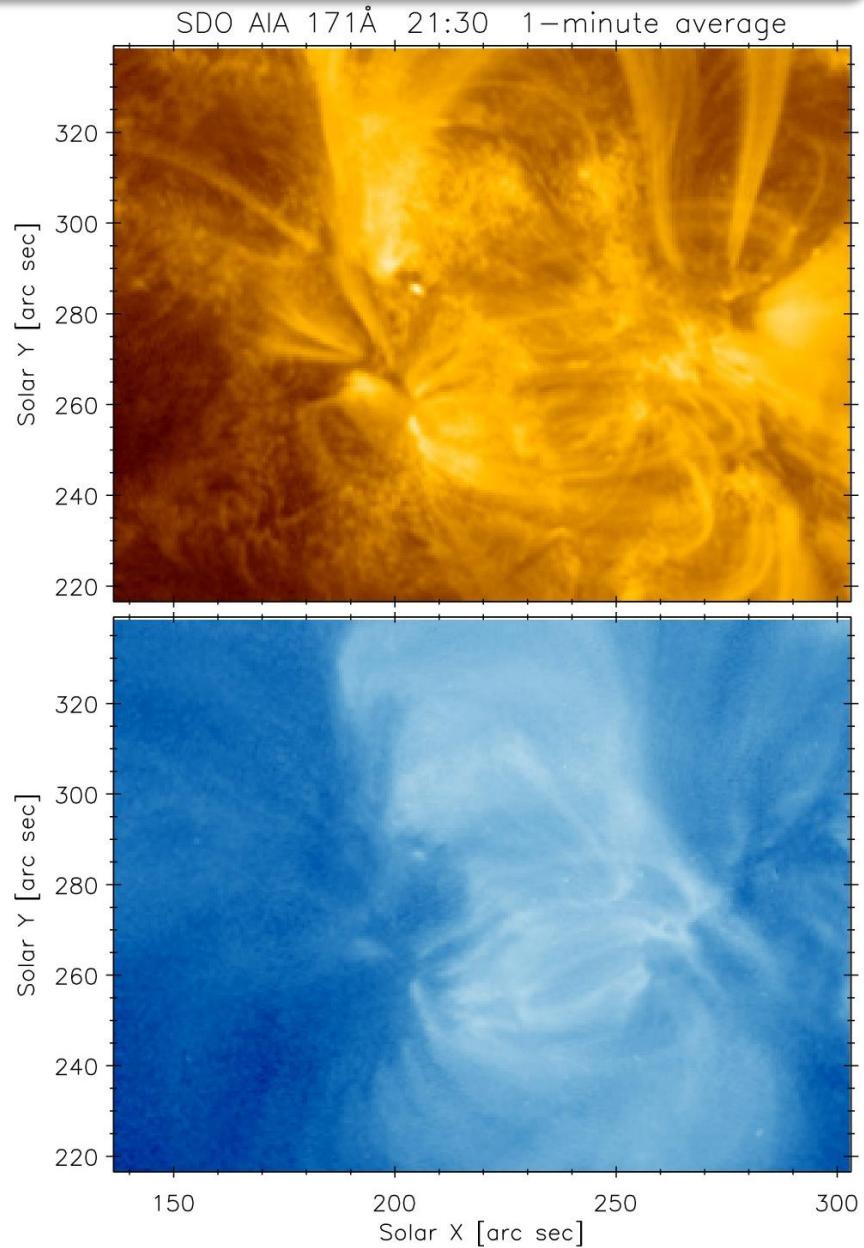
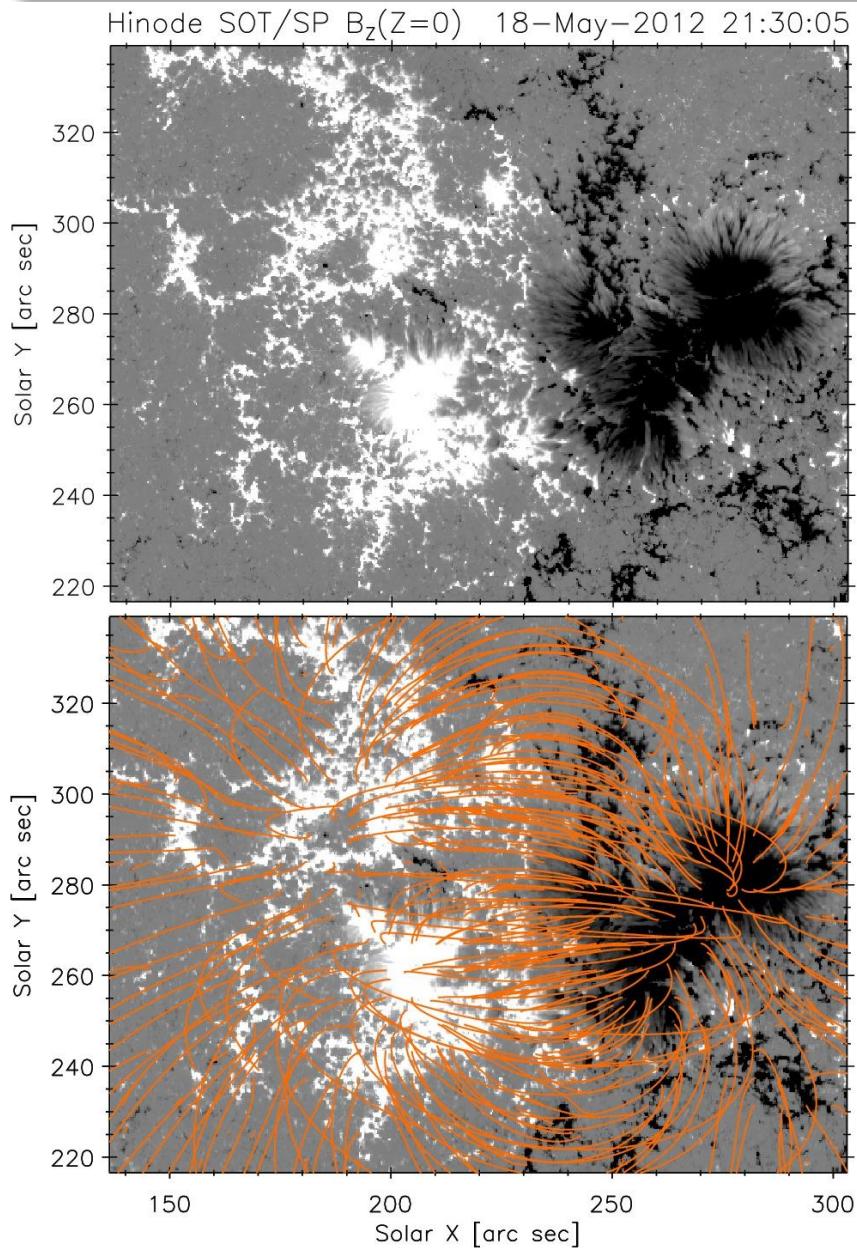
Expanding Loop: Thermal Struct.



Peter & Bingert (2012),
A&A 457, A1

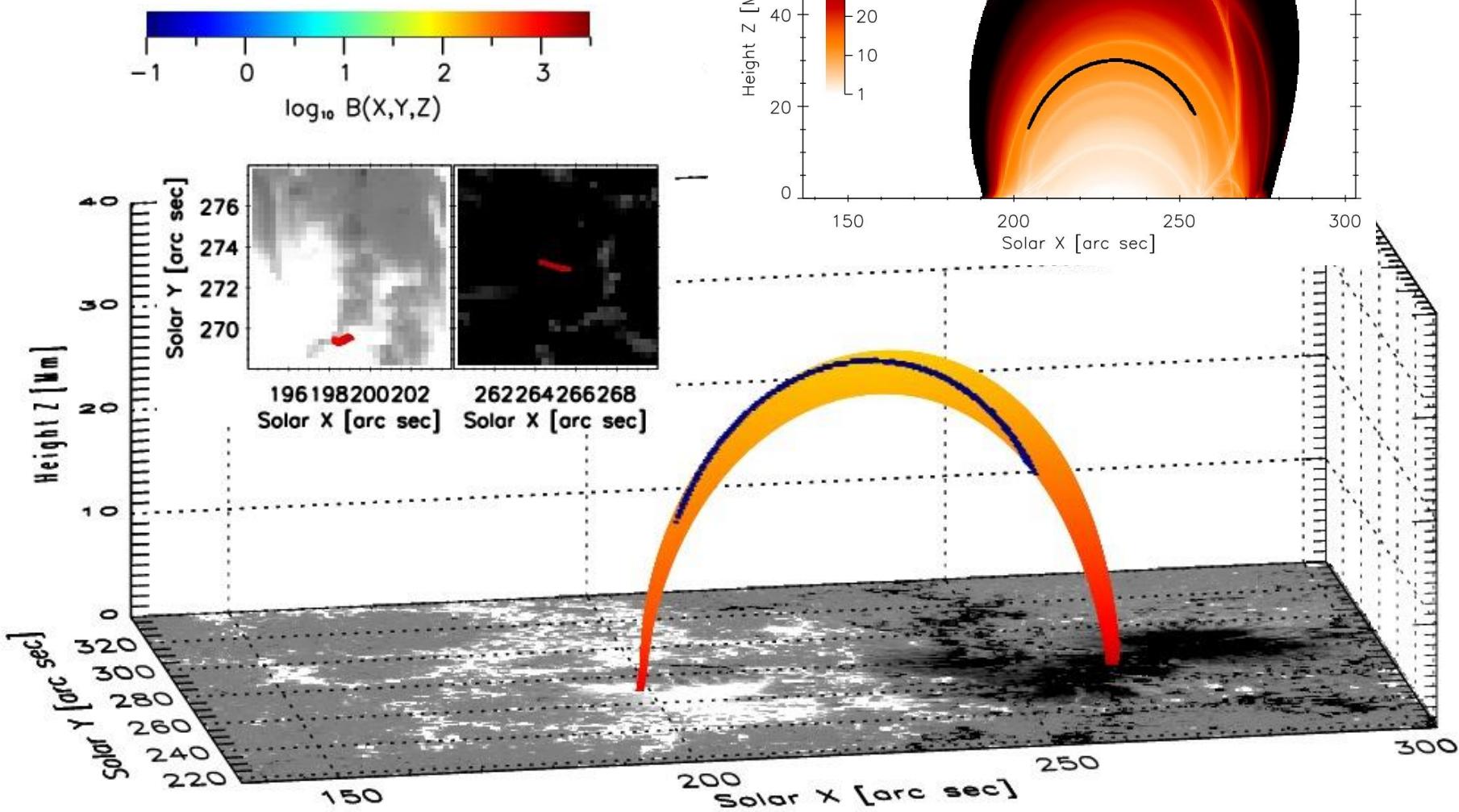
- MHD model of the solar corona
- Magnetic flux-tube with expanding area (cross-section)
- Interplay between temperature and density structure
- Leads to *apparently non-expanding AIA loop*
- Even if well-resolved

Hinode/SOT and SDO/AIA



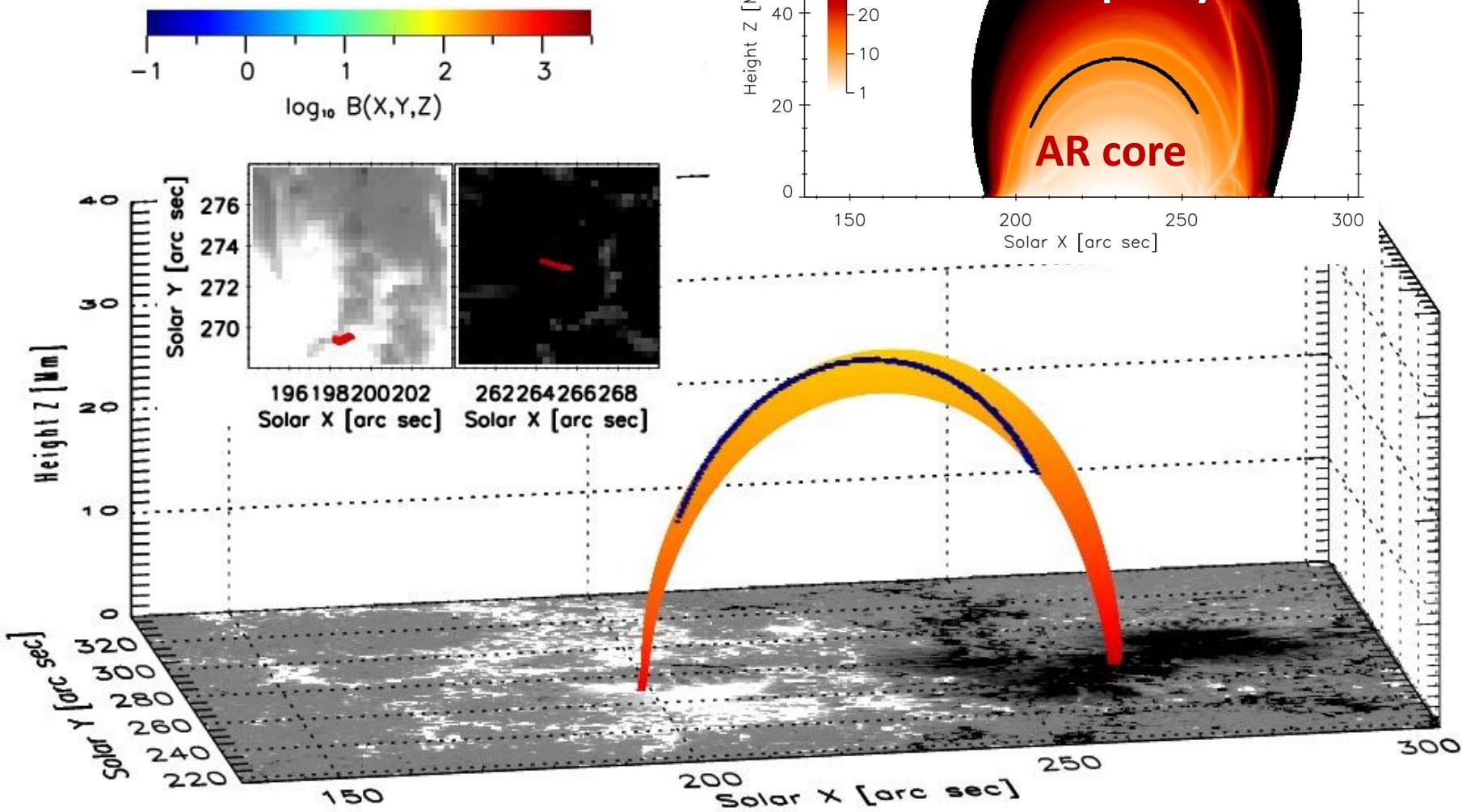
“Fundamental Flux-tubes”

Dudík et al. (2014), ApJ, 796, 20

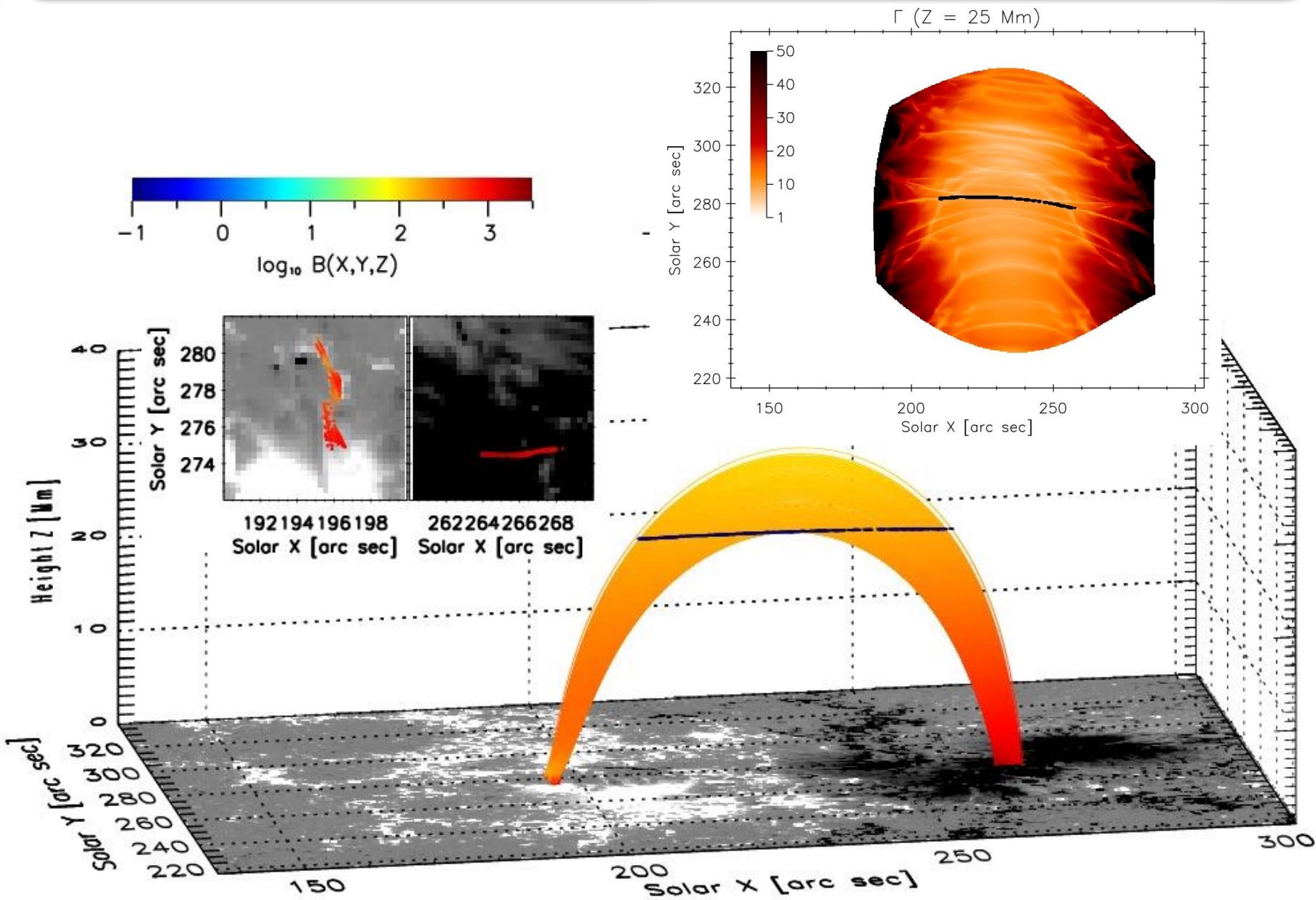


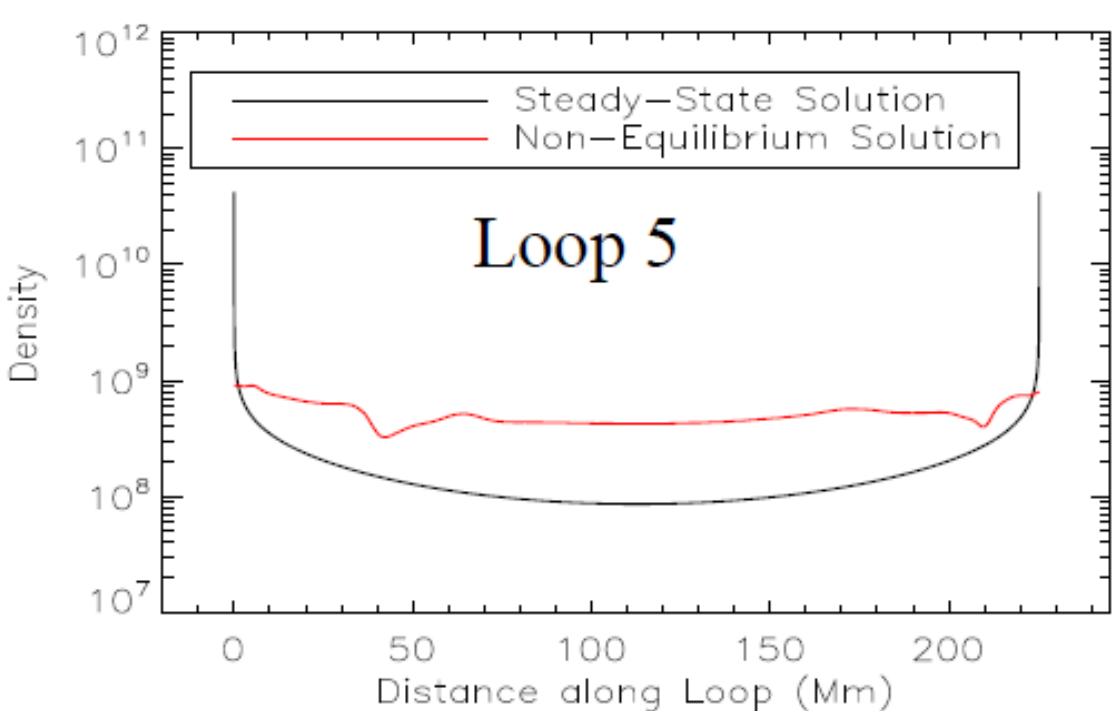
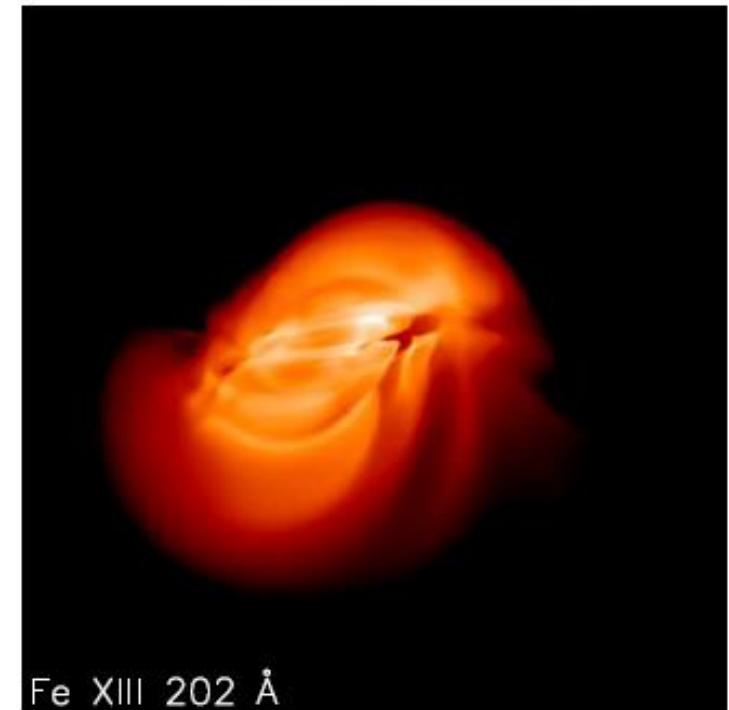
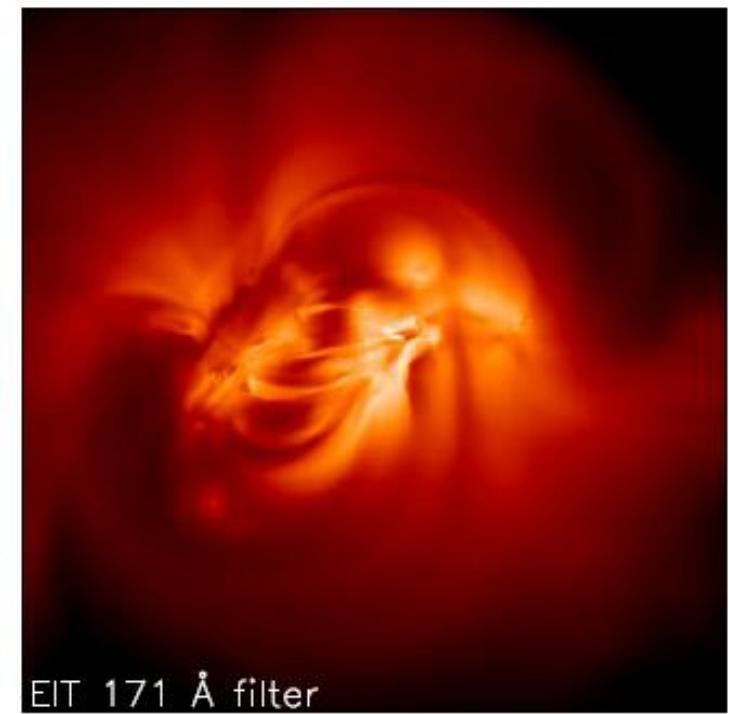
“Fundamental Flux-tubes”

Dudík et al. (2014), ApJ, 796, 20



Highly Squashed Cross-sections

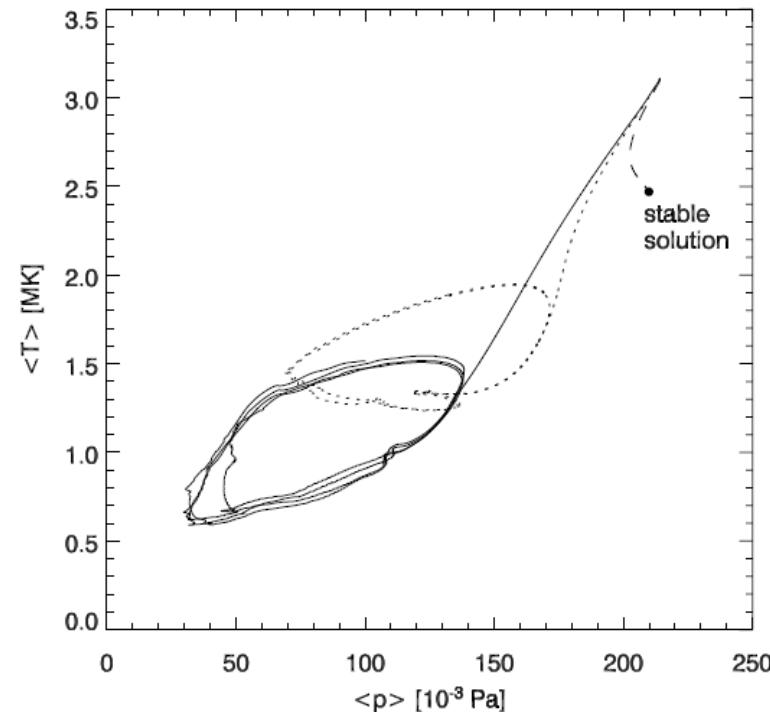
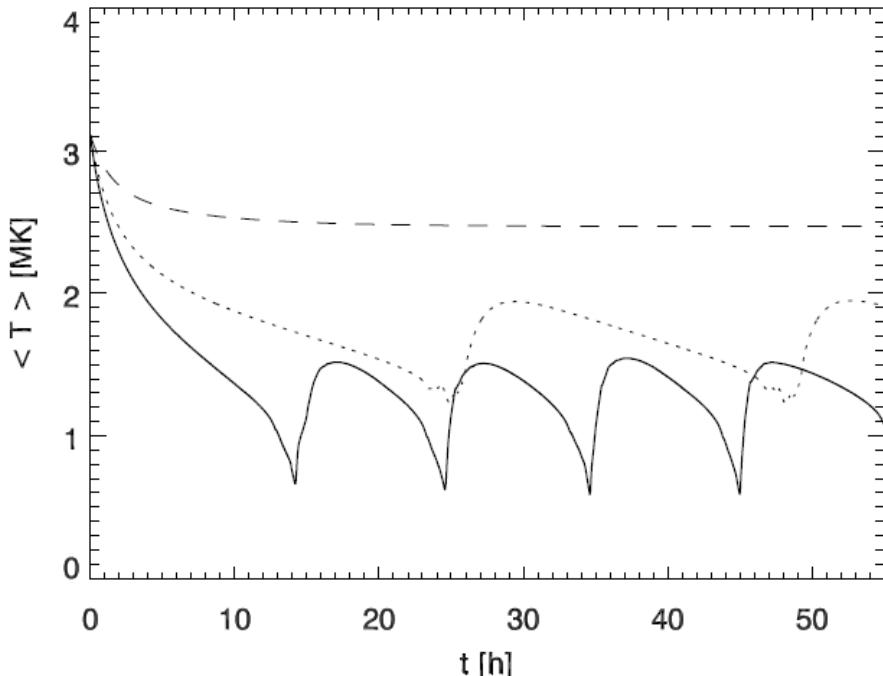




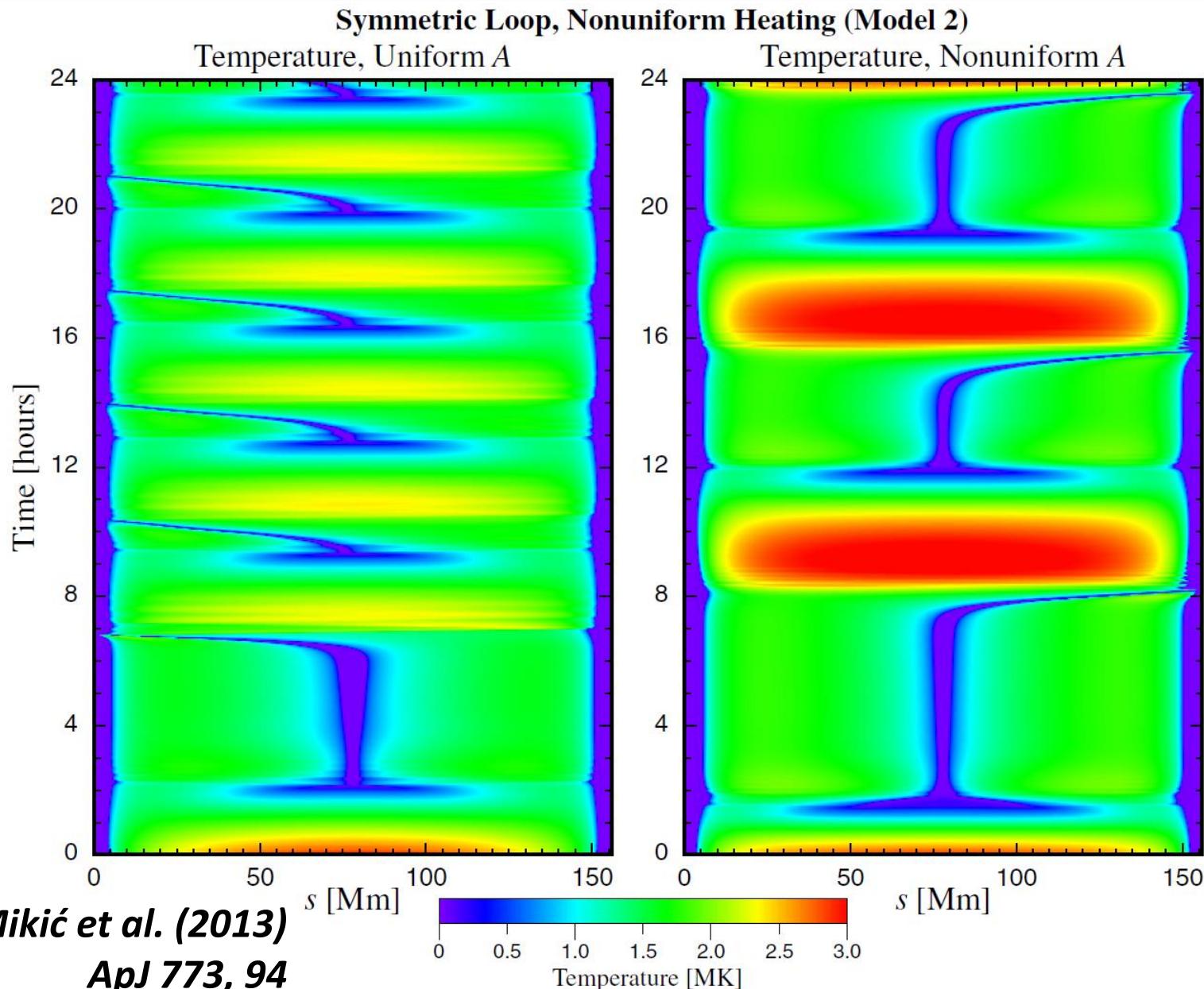
Thermal Non-Equilibrium

$$E_H - n_e^2 Q(T) = -\nabla \cdot F_C$$

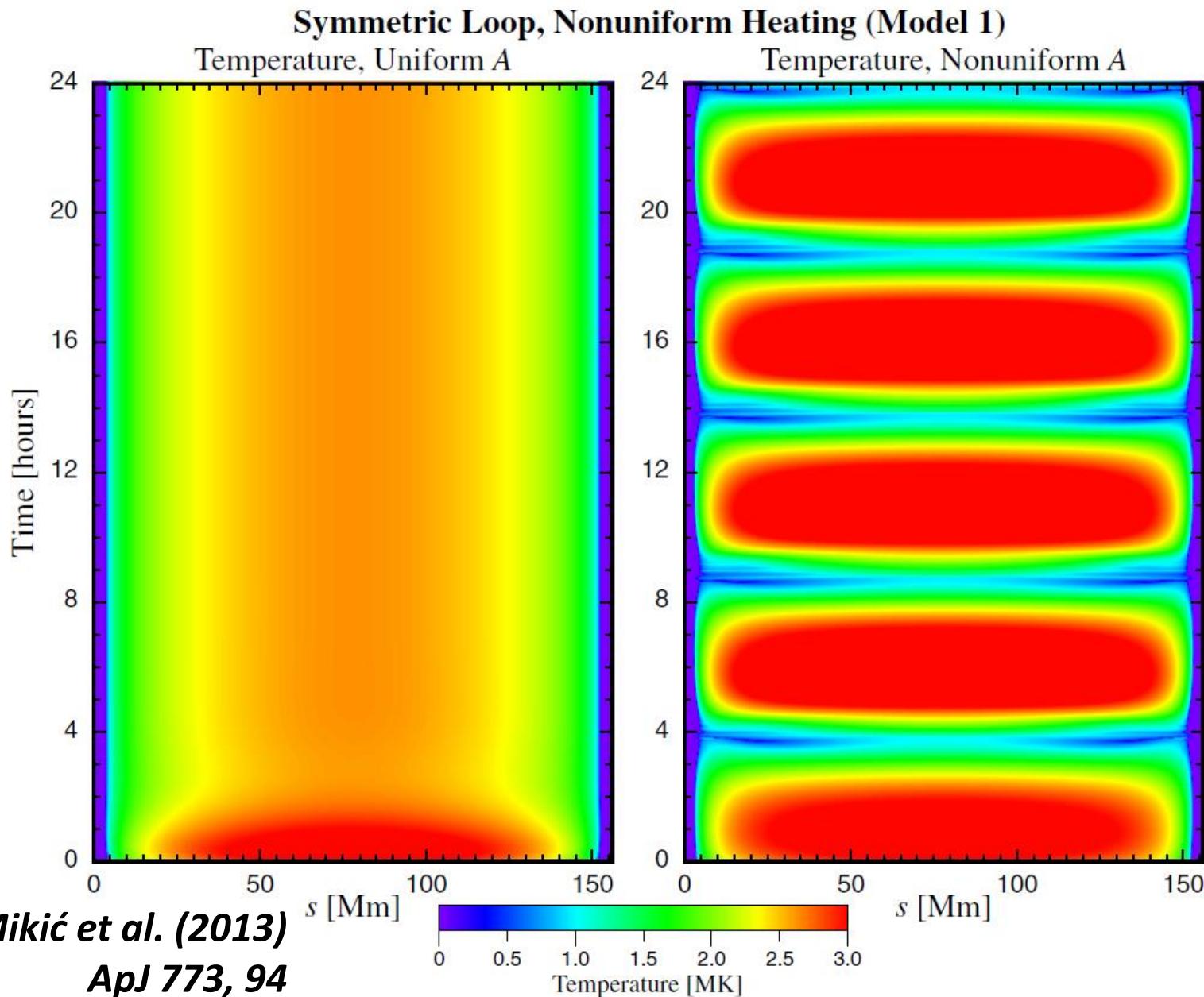
1. If the heating is too localized near the footpoints, thermal conduction cannot balance the radiative losses near the apex.
2. As a result, loop apex cools
3. Cooling increases radiative losses!
4. Condensation develops, grows and falls down. Loop empties
5. Empty loop is heated, resulting in chromospheric evaporation. Cycle renews.



Complete Condensations



(In)Complete Condensations

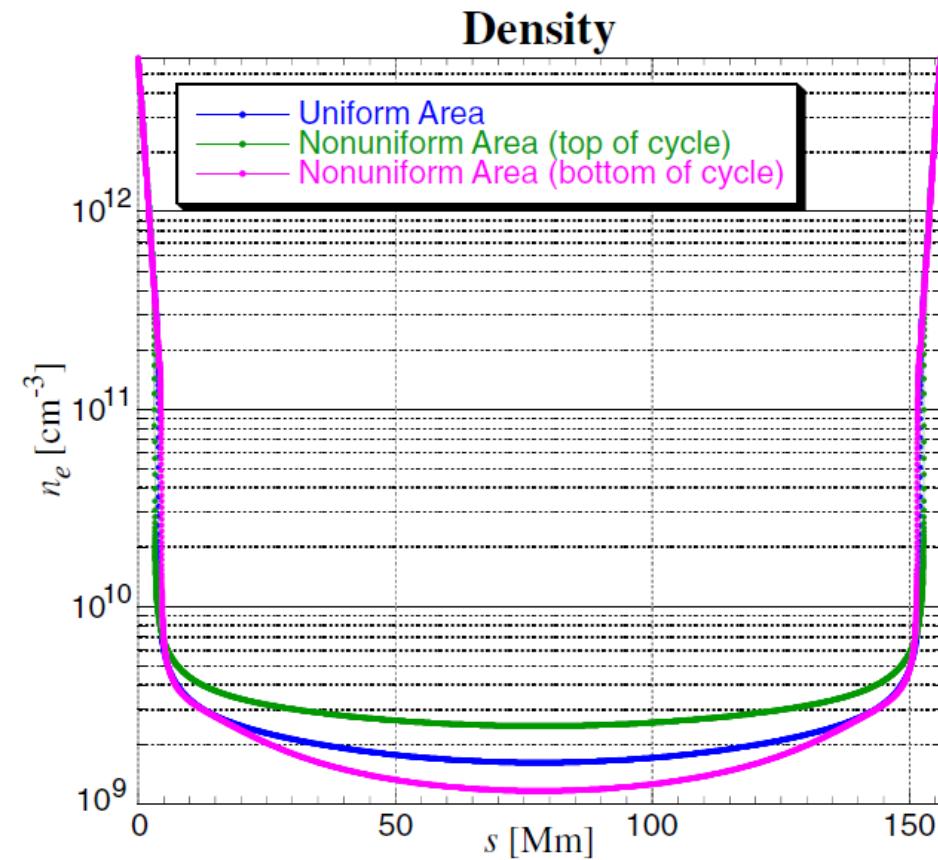
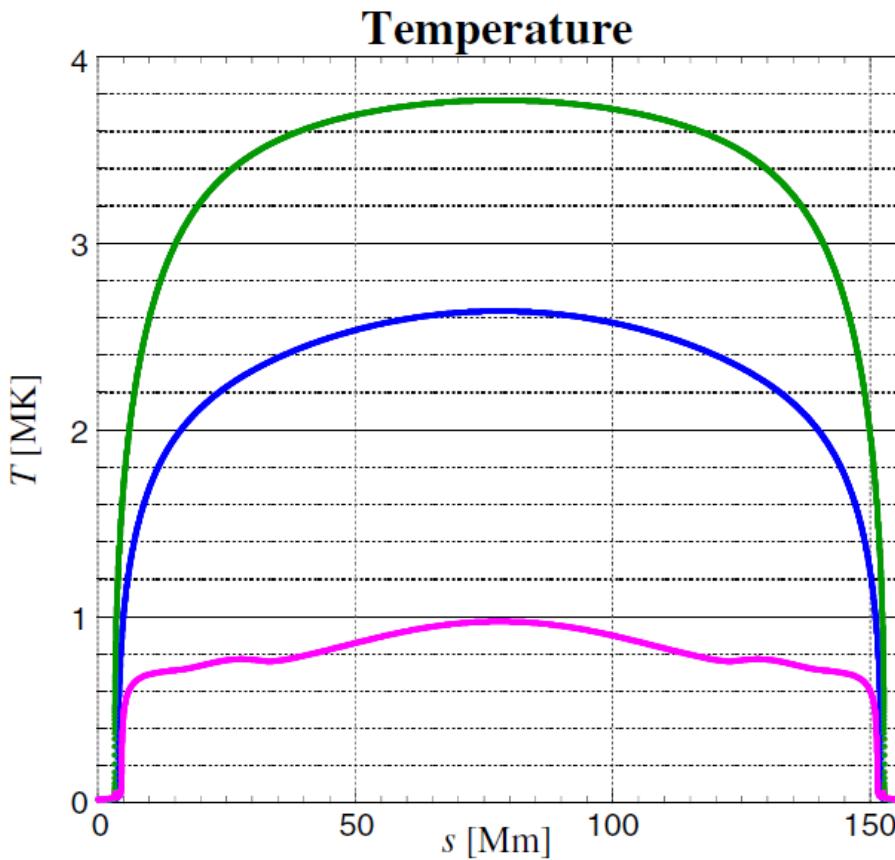


Mikić et al. (2013)

ApJ 773, 94

(In)Complete Condensations

Symmetric Loop, Nonuniform Heating (Model 1)

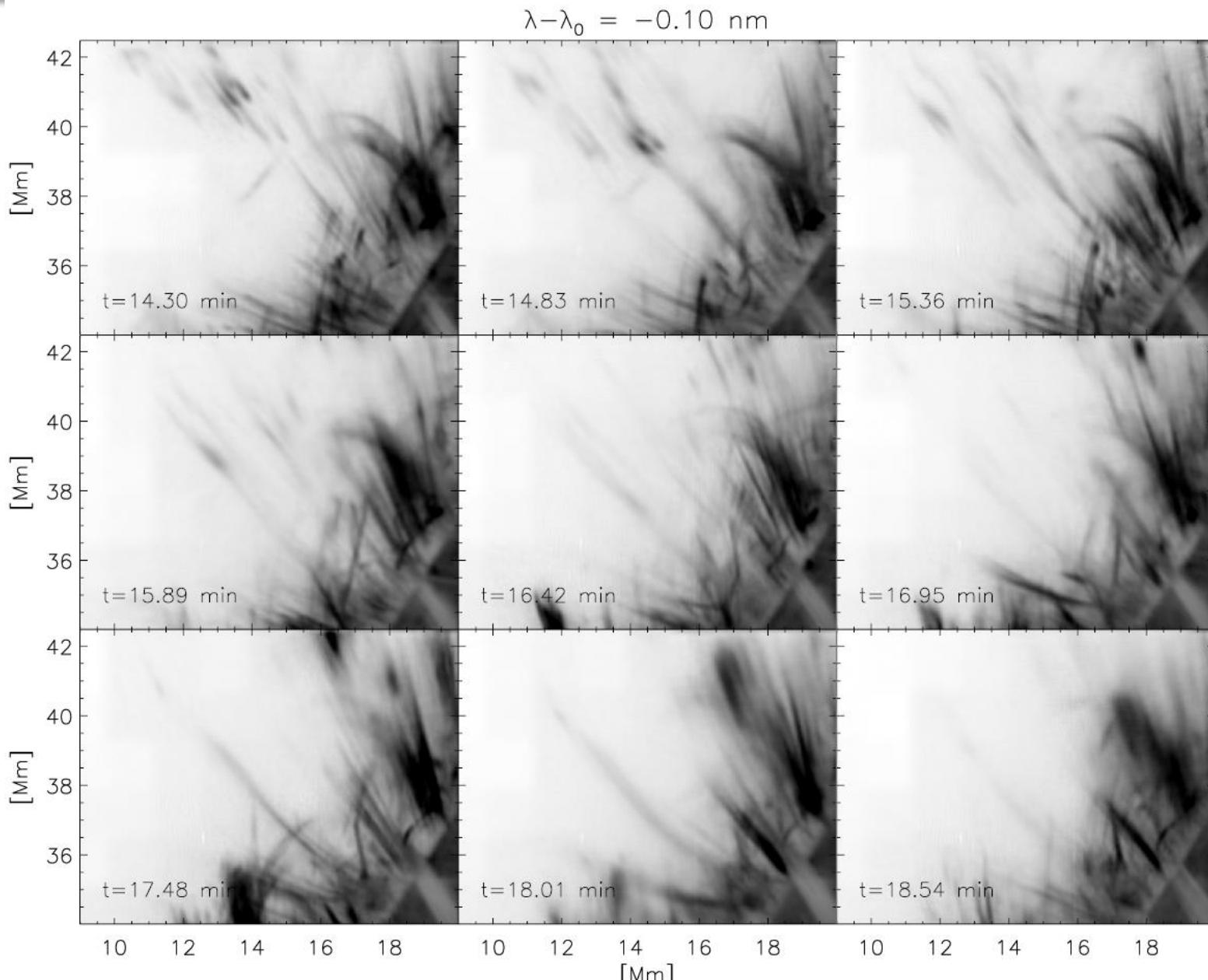


Mikić et al. (2013)

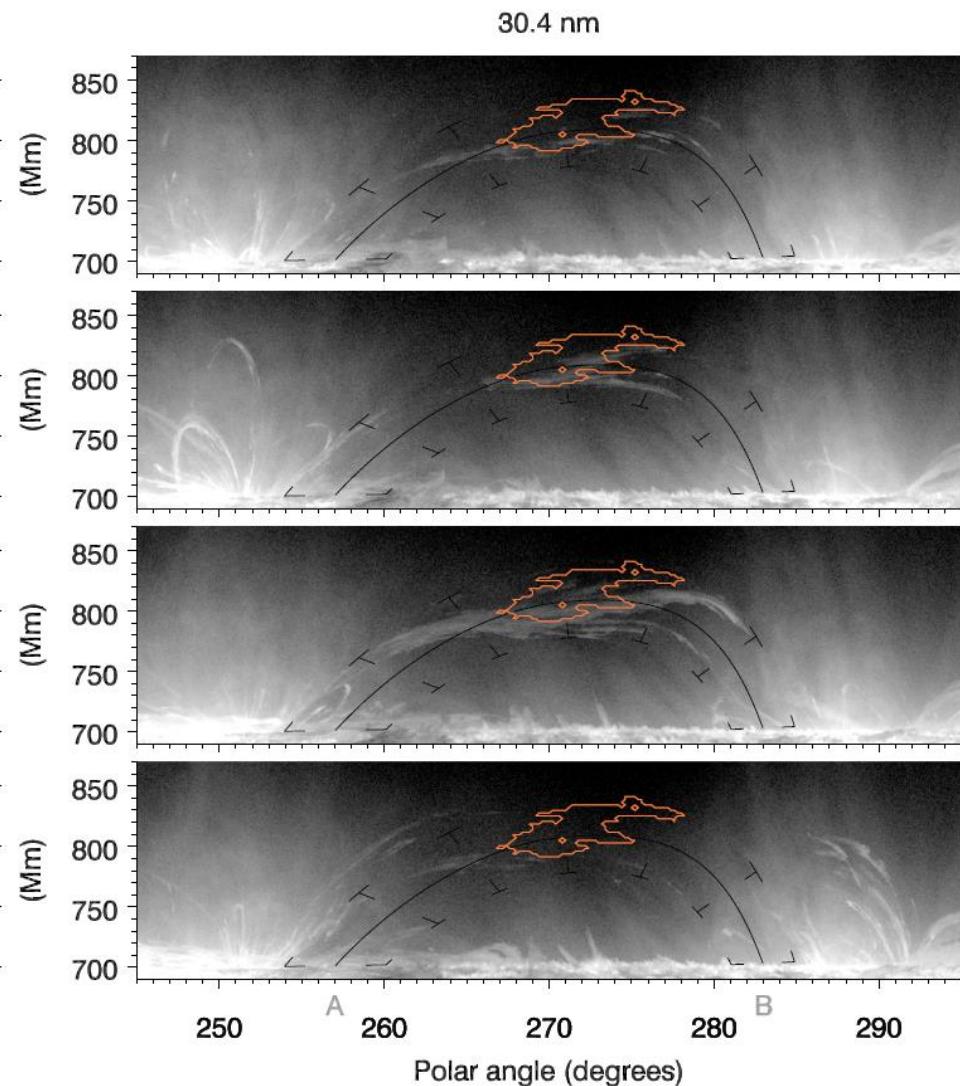
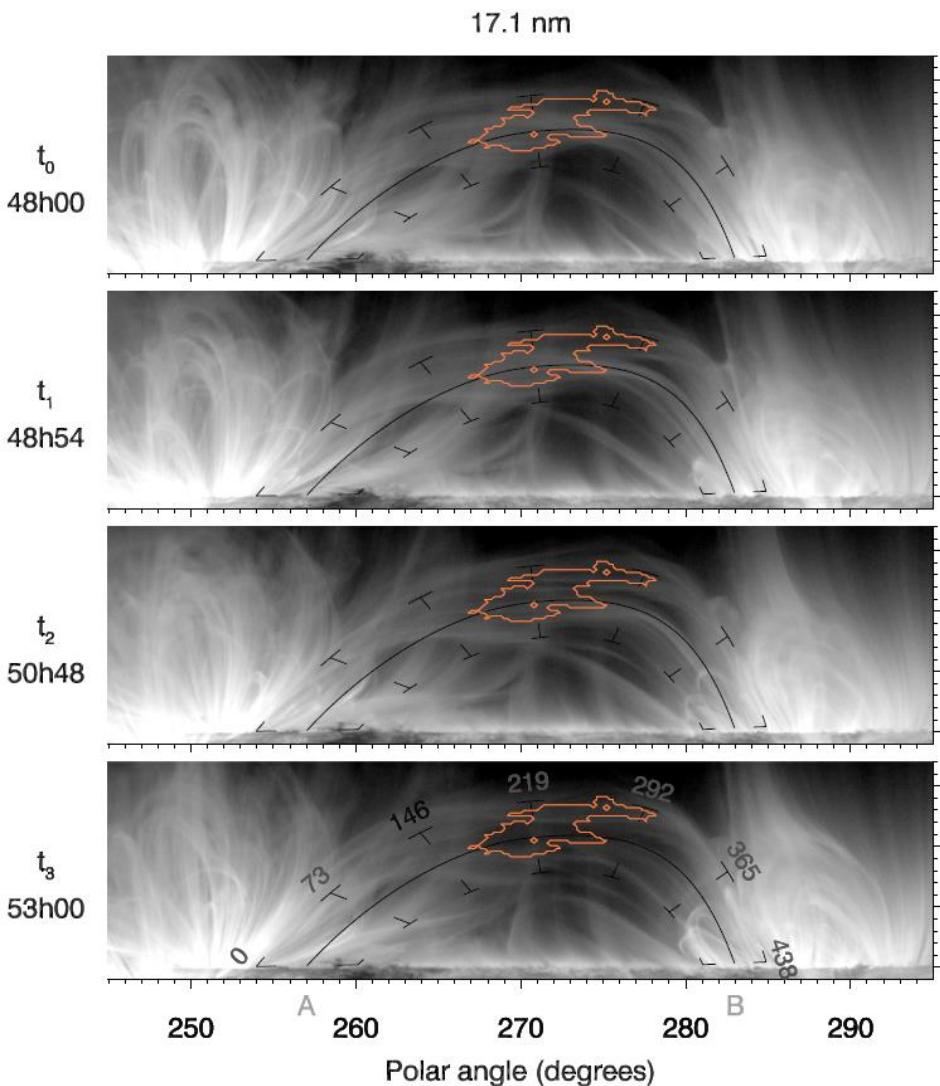
ApJ 773, 94

Coronal Rain

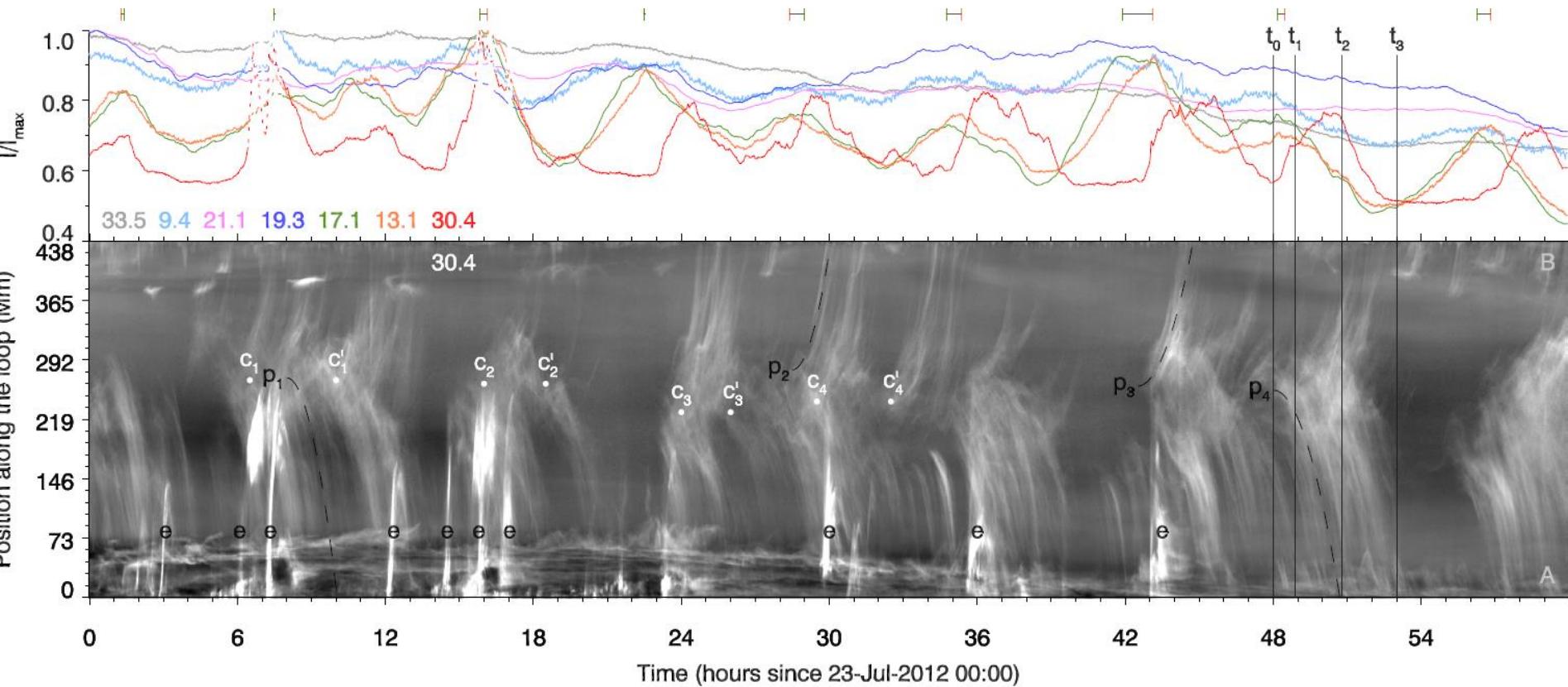
Antolin & Roupe van der Voort
(2012), ApJ, 745, 152



Thermal Non-Eq.: Recent Obs.



Thermal Non-Eq.: Recent Obs.



Auchère et al. (2018), ApJ, 853, 176

- Co-spatial and periodic (6.6 hr) showers
- Complete condensations seen at transition-region temperatures (0.1 MK)
- “It is raining as usual”: Most of the trails follow parabolas (constant acceleration)
- Evidence for steady footpoint heating